

# Differential analysis of RNA-Seq data: design, describe, explore and model

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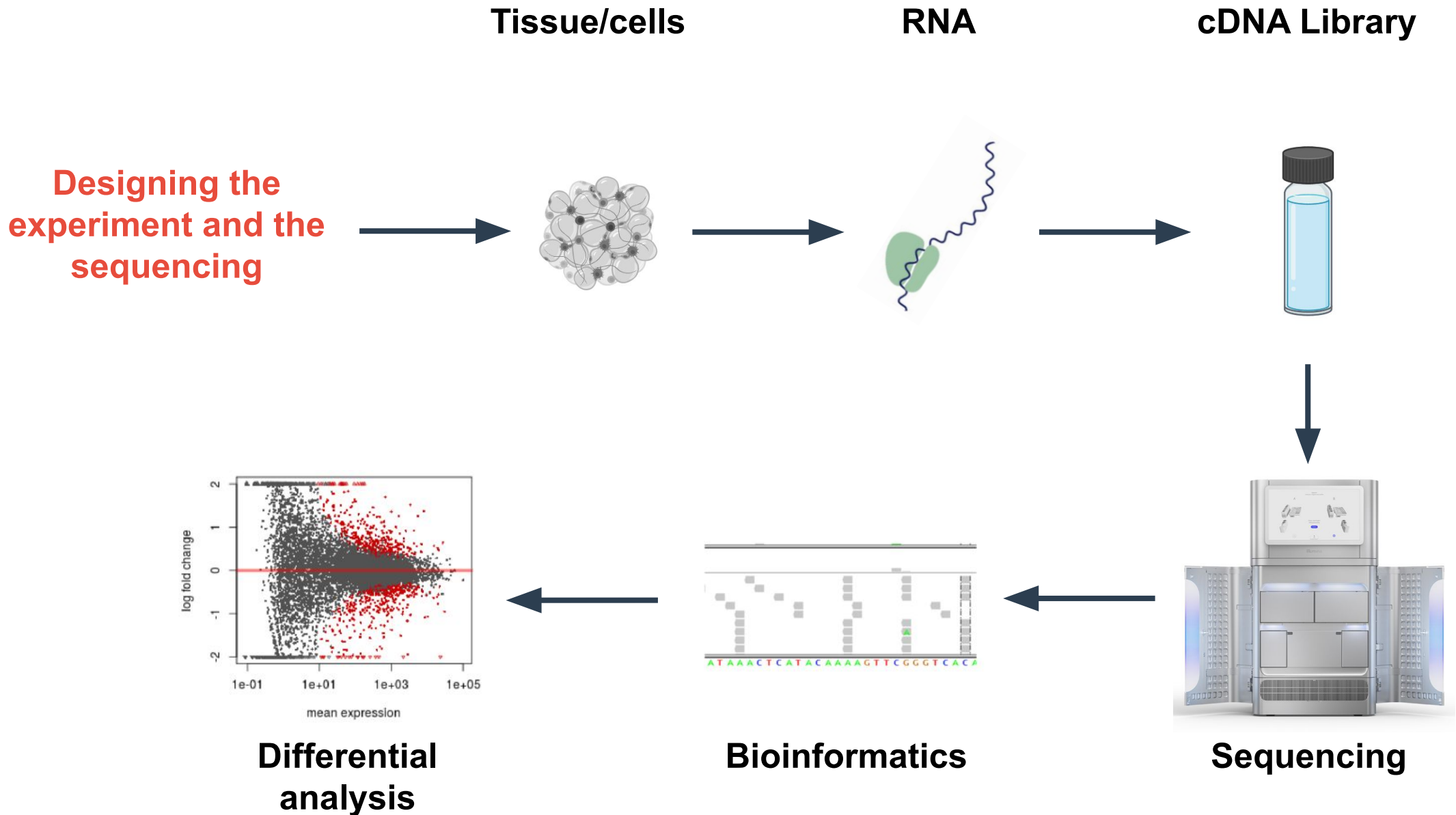


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Station Biologique  
de Roscoff



**Inserm**

# Main RNA-Seq steps

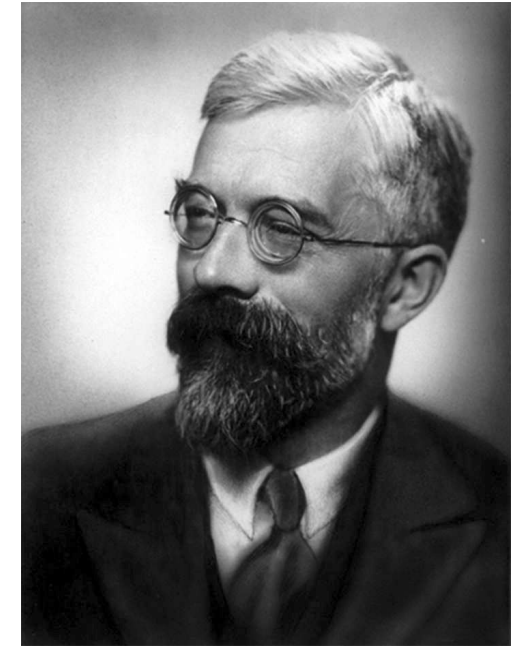


# Citations

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*"To consult a statistician after an experiment is finished is often merely to ask him to conduct a post-mortem examination. He can perhaps say what the experiment died of."*

Ronald A. Fisher, Indian Statistical Congress, 1938, vol. 4, p 17



*"While a good design does not guarantee a successful experiment, a suitably bad design guarantees a failed experiment"*

Kathleen Kerr, Atelier Inserm 145, 2003

# Statistical modeling

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**Goal of an experiment:** address **one** biological question

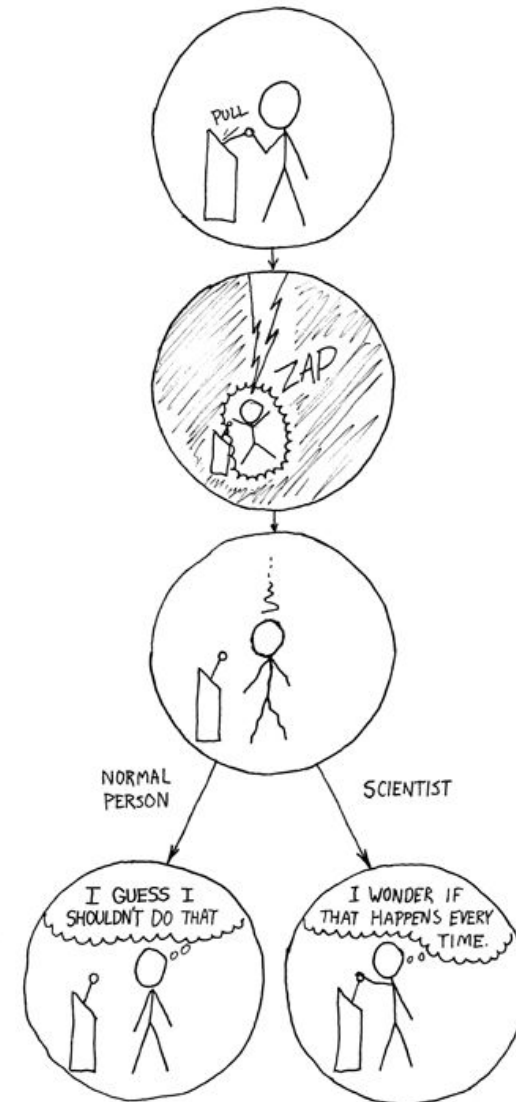
**Result of an experiment:** many numerical values

**Statistical modeling consists in using a mathematical formula involving:**

- Experimental conditions  $X$
- Numerical values measured  $Y$
- Parameters  $\beta$  linking  $X$  and  $Y$  (to be estimated), e.g.:

$$Y \sim X\beta + \varepsilon$$

- Some hypotheses on the data variability/law, e.g.:
- $$\varepsilon \sim \text{Gaussian}(0, \sigma^2)$$



# Starting point of the differential analysis

	T0-1	T0-2	T0-3	T4-1	T4-2	T4-3	T8-1	T8-2	T8-3
gene1	151	131	183	31	35	44	19	31	18
gene2	142	134	153	650	629	783	136	241	151
gene3	157	147	166	7	10	20	8	10	8
gene4	275	249	342	70	44	91	75	64	62
gene5	4	5	2	0	0	1	2	2	3
gene6	2	0	1	0	1	2	7	3	3
gene7	4	7	3	0	0	0	0	0	0
gene8	10	16	10	28	12	10	16	33	23
gene9	12	20	24	74	84	77	10	10	9
gene10	269	262	379	112	132	138	44	33	48
gene11	10065	9593	11955	4076	3739	4137	2736	3311	2749
gene12	651	566	819	101	86	74	97	87	96
gene13	118	116	150	18	24	42	15	8	5
...	...	...	...	...	...	...	...	...	...
geneN	18	31	39	4	4	7	2	6	2

**Goal:** find **genes** differentially expressed between biological conditions

# Outline

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1. Introduction
2. **Designing the experiment**
3. Description/exploration
4. Normalization
5. Modeling
6. SARTools

# Why an experimental design?

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**To control the variability** during the experiment in order to be able to address the biological question:

1. What is the biological question?
2. How to estimate the associated biological variabilities?
3. How to control the technical variabilities (day, lane, run, etc.)?

**Biological or technical uncontrolled effects could:**

- Hide/cancel the biological effect of interest
- Wrongly increase the biological effect of interest

*“Ensure that the right type of data, and enough of it, is available to answer the questions of interest as clearly and efficiently as possible”*

<http://www.stats.gla.ac.uk/steps/glossary/anova.html#expdes>

# Why an experimental design?


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PLOS COMPUTATIONAL BIOLOGY

 OPEN ACCESS

EDITORIAL

## Ten simple rules for providing effective bioinformatics research support

Judit Kumuthini , Michael Chimenti, Sven Nahnsen, Alexander Peltzer, Rebone Meraba, Ross McFadyen, Gordon Wells, Deanne Taylor, Mark Maienschein-Cline, Jian-Liang Li, Jyothi Thimmapuram, Radha Murthy-Karuturi, Lyndon Zass

Published: March 26, 2020 • <https://doi.org/10.1371/journal.pcbi.1007531>

“A good experimental design starts with a **well-defined hypothesis** [...]. The experimental design should aim to reduce the types and sources of variability, increase the **generalizability** of the experiment, and make it **replicable** and reusable. It is both easier and more cost efficient to identify and correct experimental design issues ahead of time than to address deficiencies thereafter. Thus, discussion between data-generating researchers and bioinformaticians is highly desirable and should occur as early as possible during project development and experimental design.”



# Basic comparison

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I want to study differences in the transcriptome of cystic fibrosis patients

<b>id</b>	<b>state</b>
h1	healthy
h2	healthy
h3	healthy
cf1	CF
cf2	CF
cf3	CF

- one **factor** of interest :  
the state of the patients
- this factor has two **levels**:  
healthy and CF



**mRNA sequencing of lung cells.**

# Paired samples

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I want to study differences in the transcriptome of cystic fibrosis patients

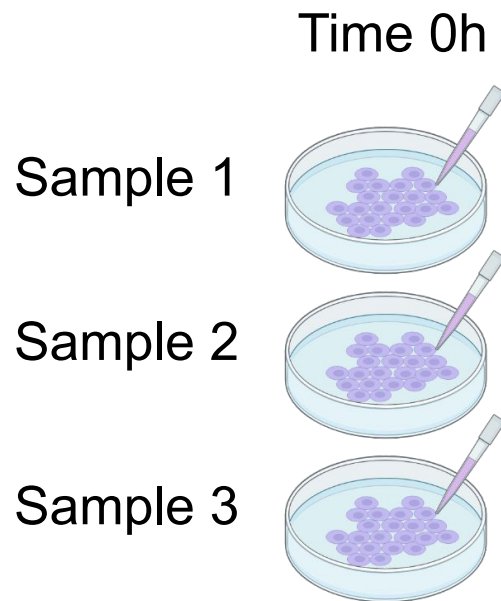
<b>id</b>	<b>state</b>	<b>RNA extraction date</b>
h1	healthy	June 12 <sup>th</sup> , 2019
h2	healthy	June 20 <sup>th</sup> , 2019
h3	healthy	June 25 <sup>th</sup> , 2019
cf1	CF	June 12 <sup>th</sup> , 2019
cf2	CF	June 20 <sup>th</sup> , 2019
cf3	CF	June 25 <sup>th</sup> , 2019

# On the laboratory bench...

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## Time course experiment (paired)

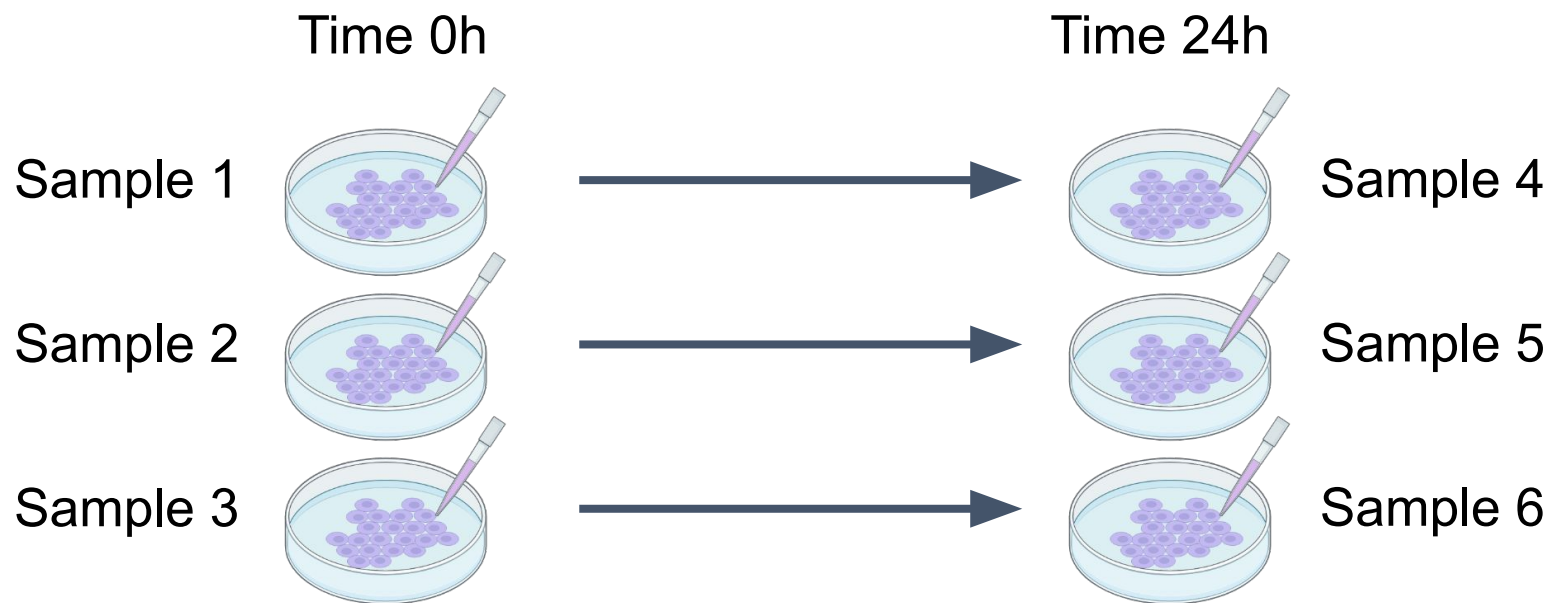
I want to find differentially expressed genes between time 0 and time 24h on cultures of E. Coli



# On the laboratory bench...

## Time course experiment (paired)

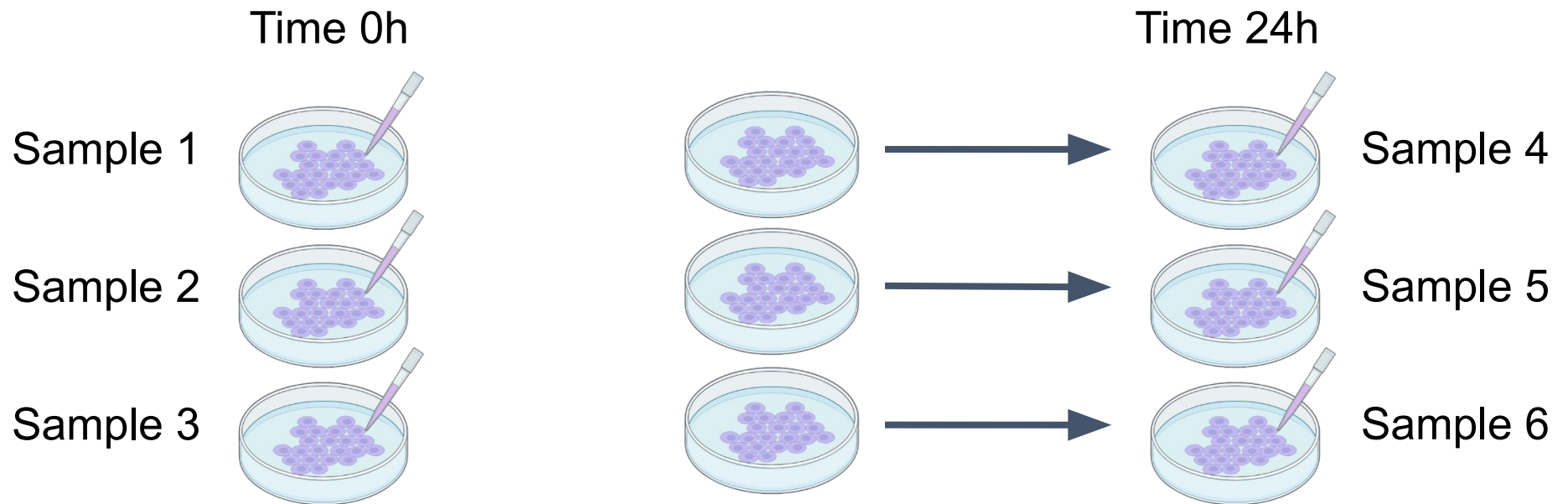
I want to find differentially expressed genes between time 0 and time 24h on cultures of E. Coli



# On the laboratory bench...

## Time course experiment (unpaired)

I want to find differentially expressed genes between time 0 and time 24h on cultures of E. Coli



# Complex design

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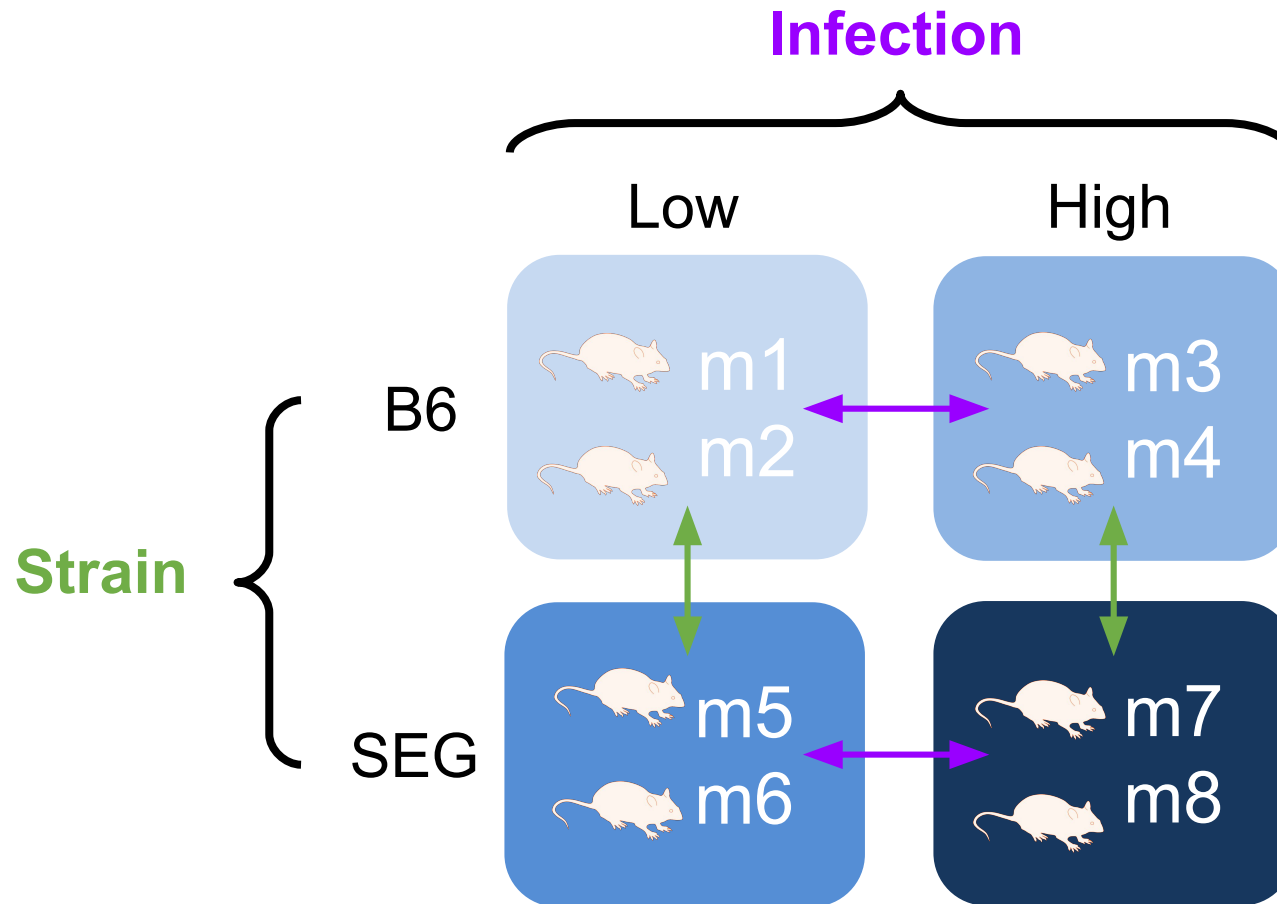
I want to study the effect of a virus infection level (high vs. low) on the transcriptome of two mouse strains (B6 vs. SEG).

<b>id</b>	<b>strain</b>	<b>infection</b>
m1	B6	low
m2	B6	low
m3	B6	high
m4	B6	high
m5	SEG	low
m6	SEG	low
m7	SEG	high
m8	SEG	high

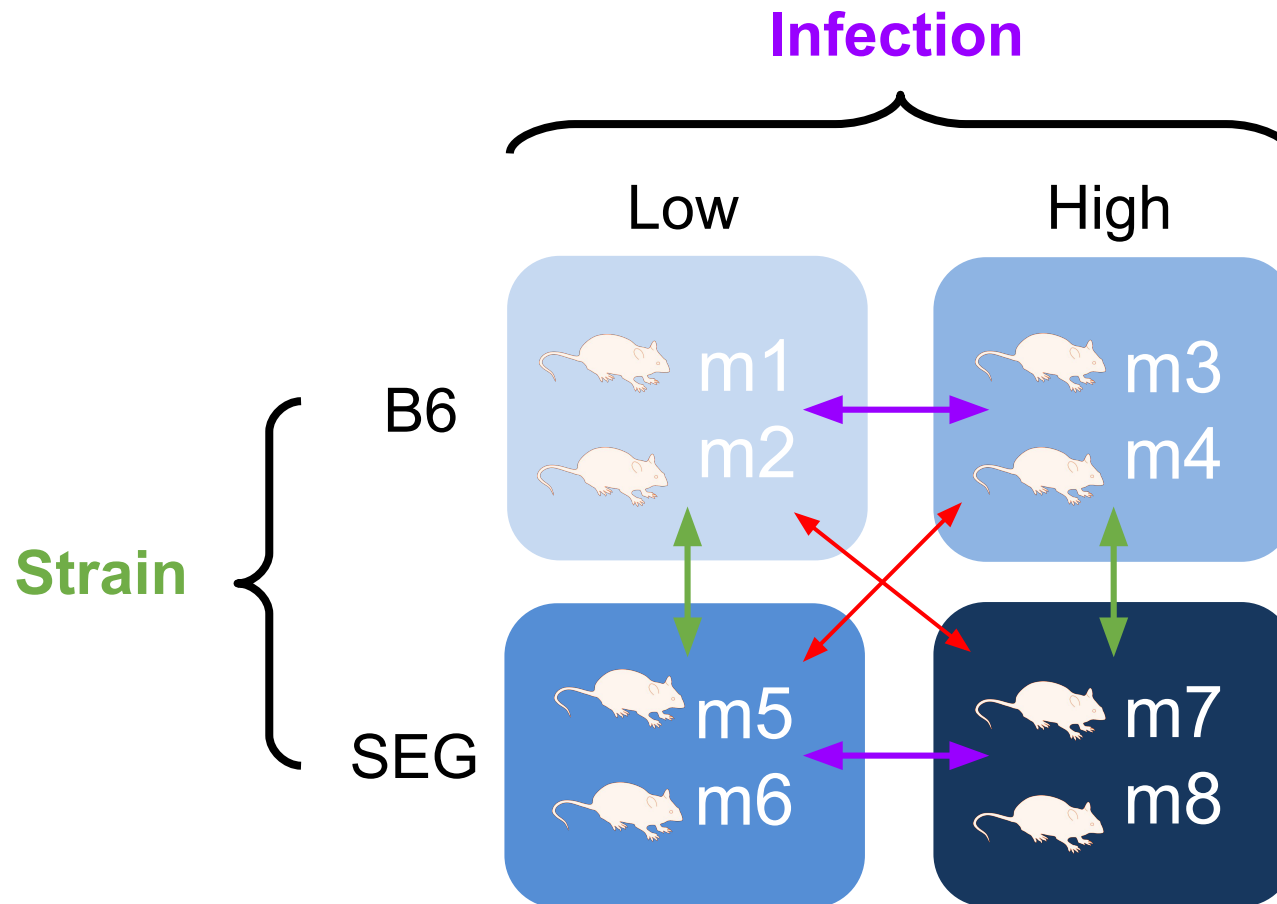
**Two factors** of interest with **two levels** each :

- the infection level of the patients (low or high)
- the mouse strain (SEG and B6)

# Interaction between two factors/variables



# Interaction between two factors/variables



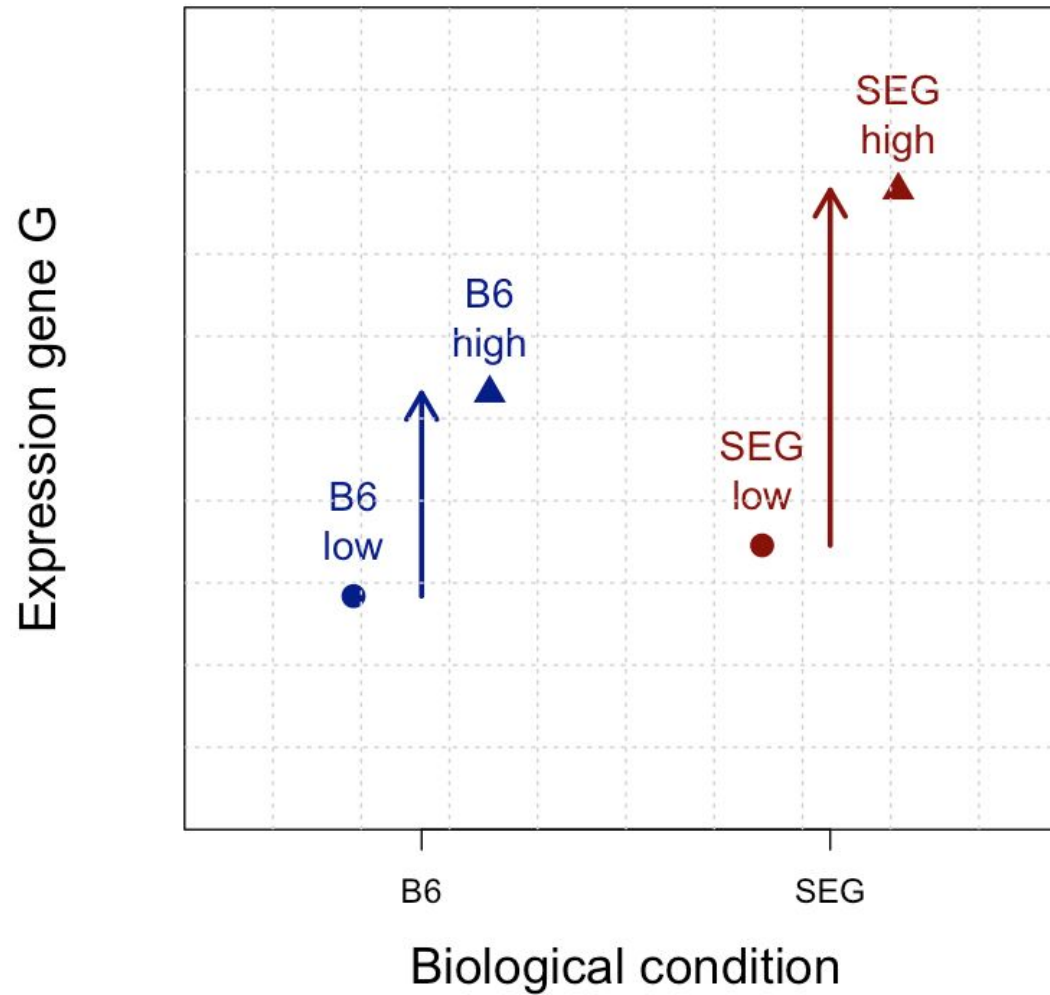
## Interaction:

- Is the infection effect different between the two strains?
- Does the difference between the strains change according to the infection?



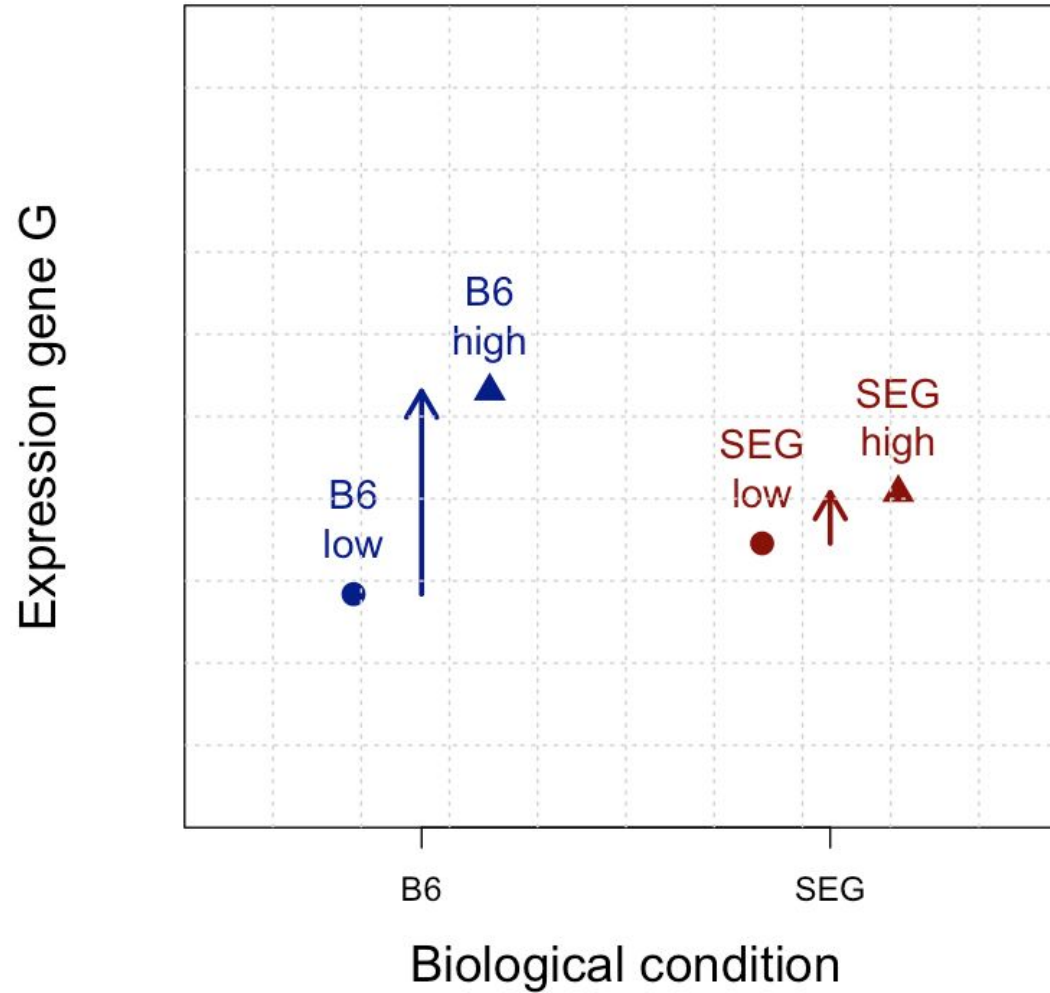
# Examples of interactions

## Reinforcement of the infection effect



# Examples of interactions

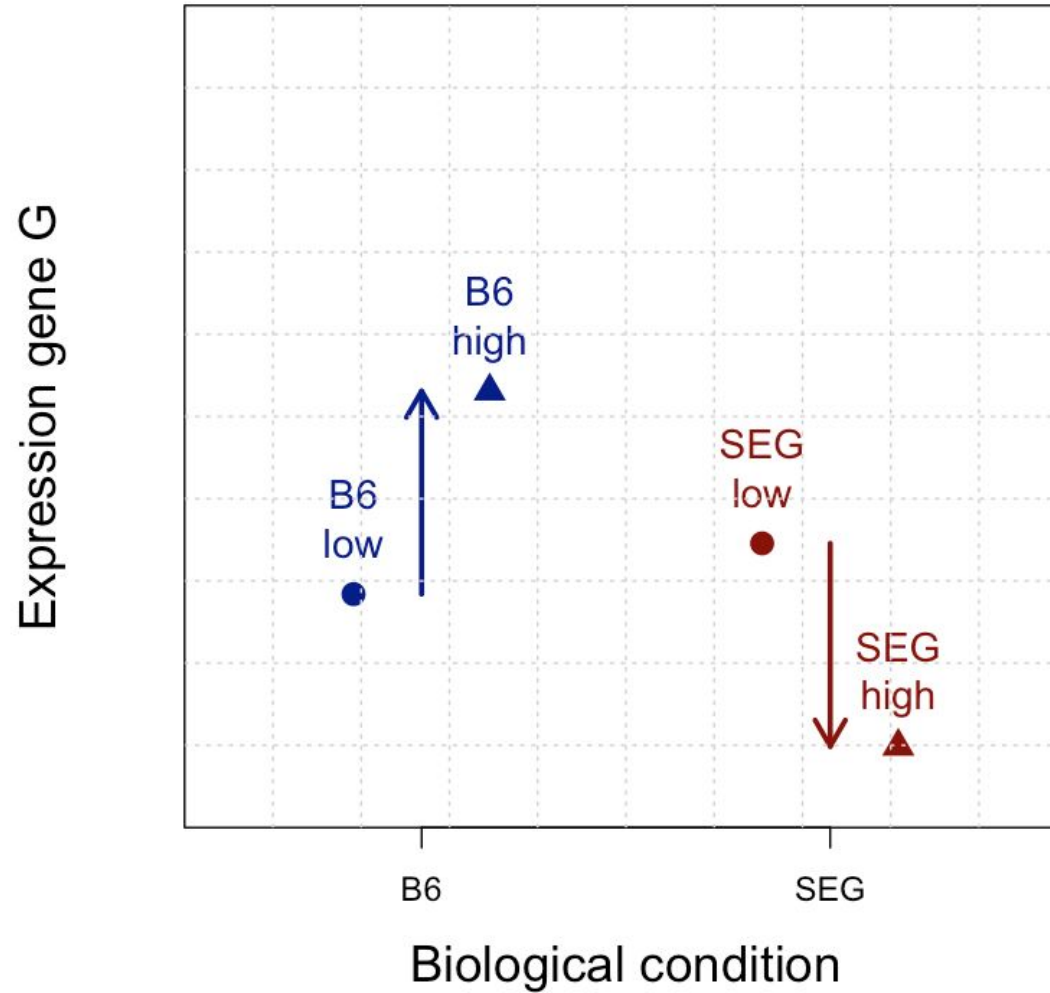
## Decreasing of the infection effect



# Examples of interactions

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## Inversion of the infection effect



# Complex design with nested factors

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A treatment T is applied to two CF patients and two healthy people. We study the initial transcriptome and after 4h of treatment.

<b>id</b>	<b>state</b>	<b>time</b>	<b>patient</b>
h1-0	healthy	0h	h1
h2-0	healthy	0h	h2
h1-4	healthy	4h	h1
h2-4	healthy	4h	h2
cf1-0	CF	0h	cf1
cf2-0	CF	0h	cf2
cf1-4	CF	4h	cf1
cf2-4	CF	4h	cf2

The "patient" effect need to be taken into account, but it is nested into the "state" effect.

# Be careful with confounding effects !

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## Comparison of lung cells in healthy and cystic fibrosis patients

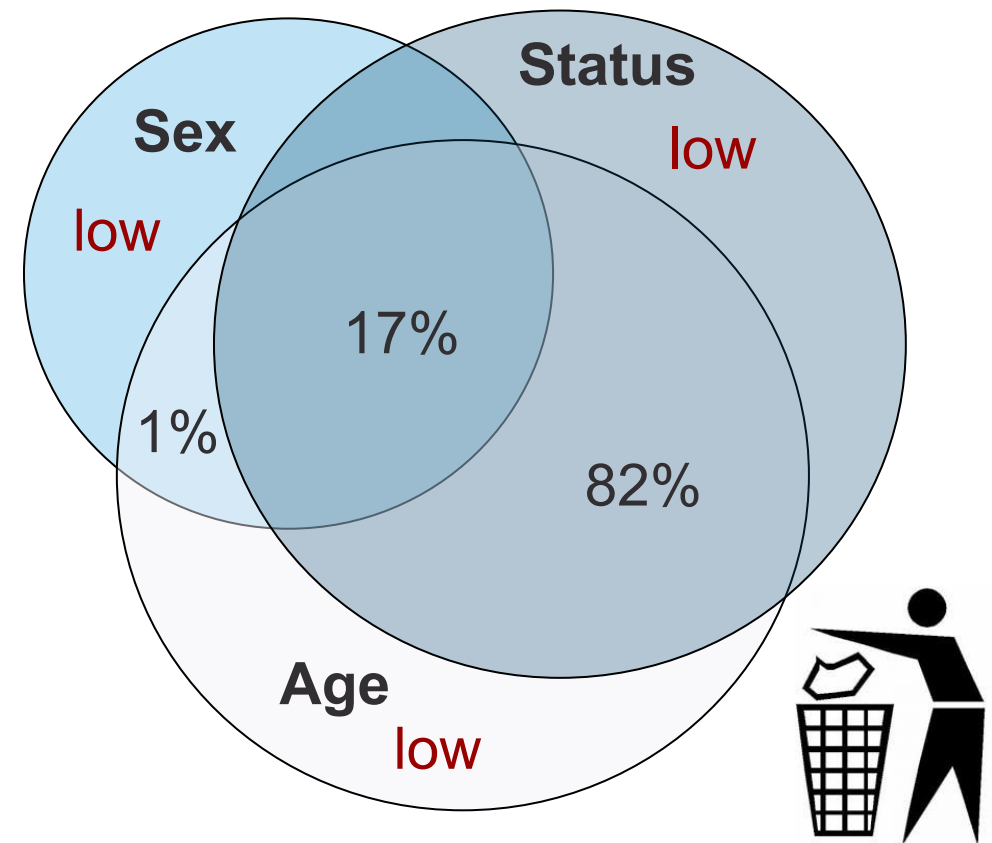
id	state	age	sex	RNA extraction day	experimentalist
h1	healthy	45	female	July 9 <sup>th</sup> , 2019	Louis
h2	healthy	52	female	July 12 <sup>th</sup> , 2019	Louis
h3	healthy	48	female	July 15 <sup>th</sup> , 2019	Louis
cf1	CF	31	male	Feb 20 <sup>th</sup> , 2019	Françoise
cf2	CF	25	male	Feb 24 <sup>th</sup> , 2019	Françoise
cf3	CF	27	male	Feb 29 <sup>th</sup> , 2019	Françoise

# Be careful with confounding effects !

→ A gene is detected as being differentially expressed between healthy and CF patients. Is it due to:

- The disease?
- The sex effect?
- The age effect?
- The date effect?
- The technician effect?

## Flawed design



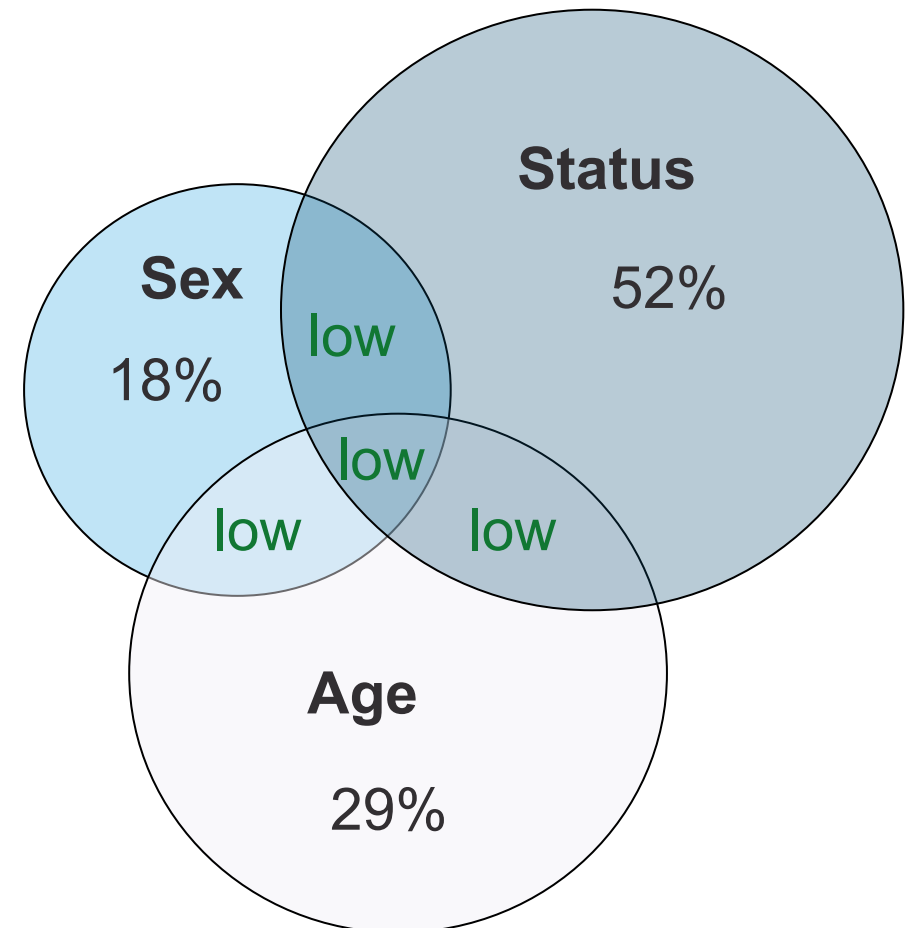
# Be careful with confounding effects !

→ Re-doing the experiment but making sure all levels of all factors are **crossed** to avoid any confusion

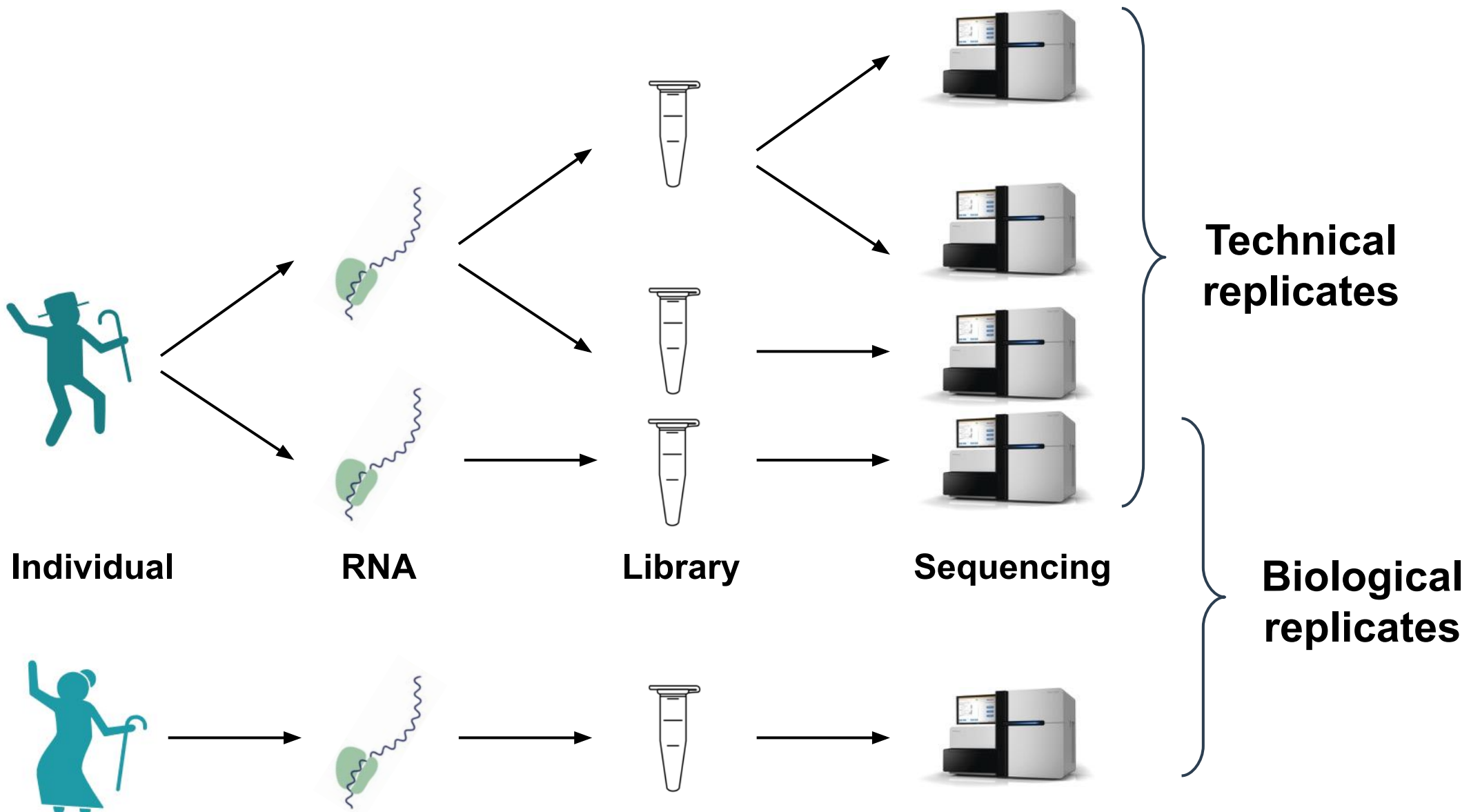
## Crossed design

Possibility to distinguish every source of variability & their interaction :

- The disease
- The sex effect
- The age effect
- The date effect
- The technician effect



# Biological vs. technical replicates





# Biological vs. technical replicates in RNAseq

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## Technical replicates:

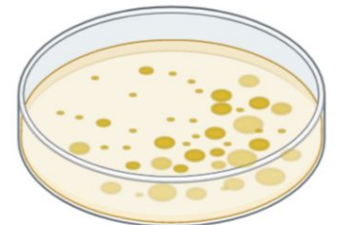
- Several extractions of the same RNA
- Several libraries built from the same RNA extraction
- A library sequenced several times

Allow to get more sequencing depth and a better coverage. Need to sum the counts associated to each technical replicates.

## Biological replicates:

- Parallel measurements of biologically **distinct samples**
- Correspond to the variability visible in the real life

**Comment:** what happens when studying fungi/yeast?



# Why replicate?

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## Perfect world:

No biological nor technical variability



Only one sample from each condition to conclude!

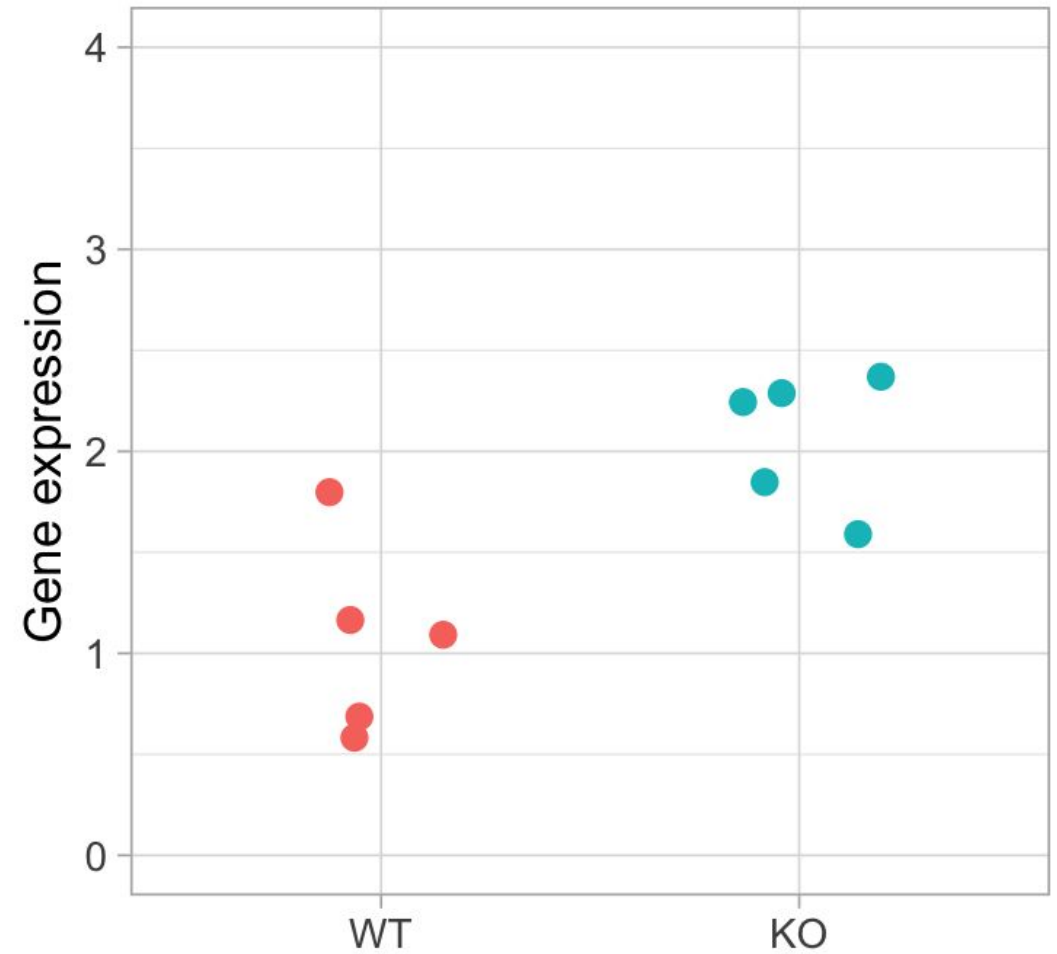
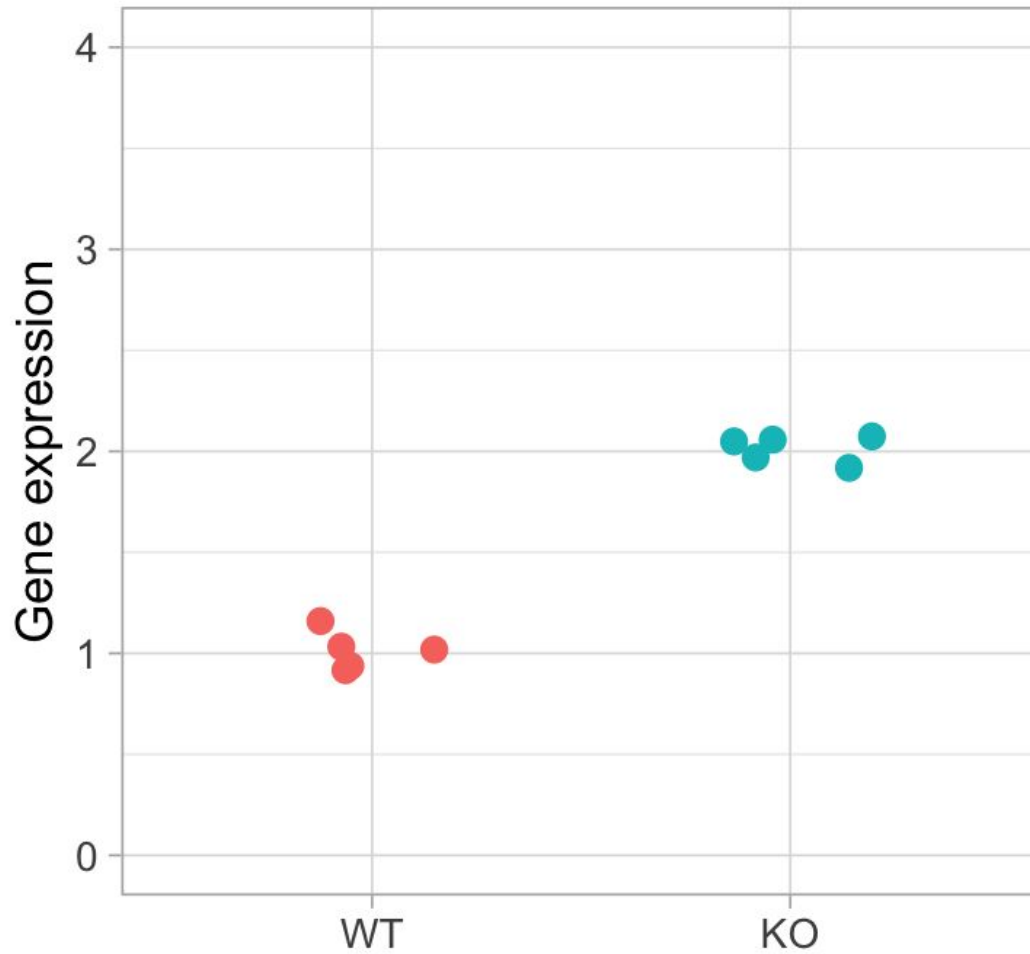
## Our world:

Each individual has its own behavior



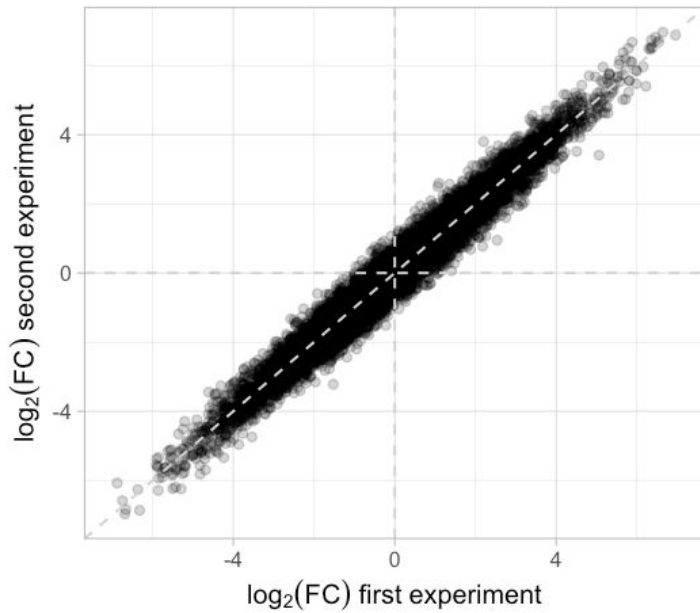
Need several biological replicates to handle variability

# Why replicate?

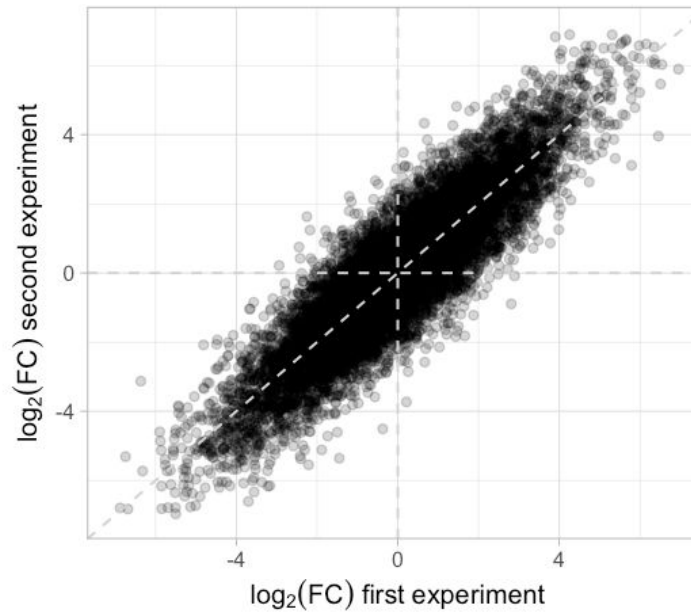


# Reproducibility of an experiment: 3 KO vs 3 WT

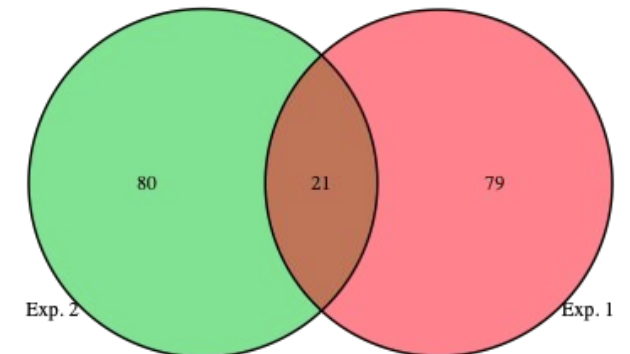
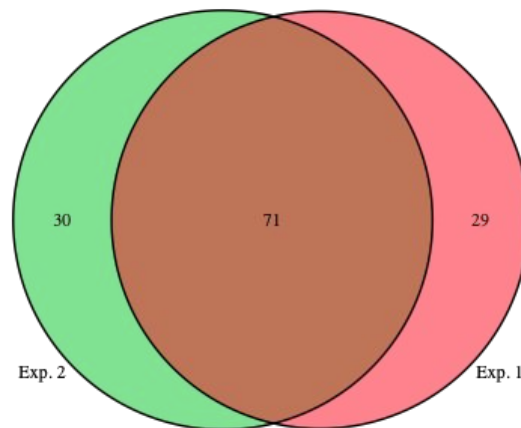
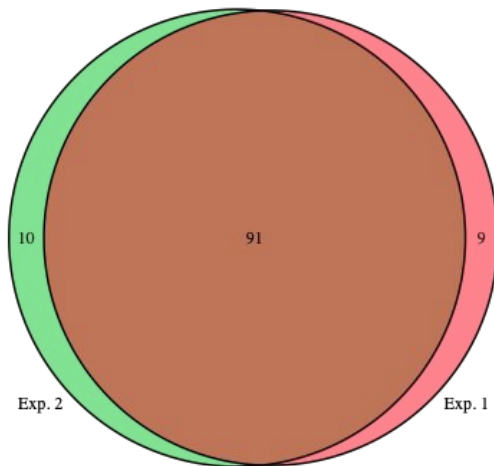
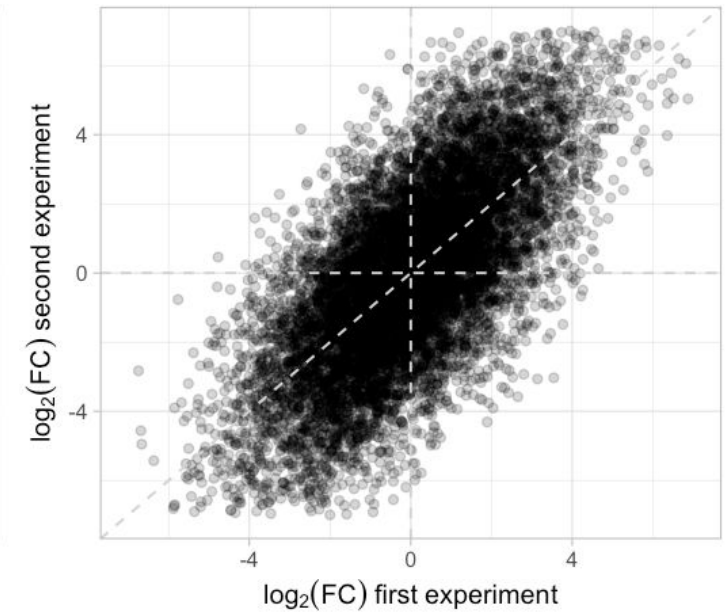
Good reproducibility



More or less good reproducibility



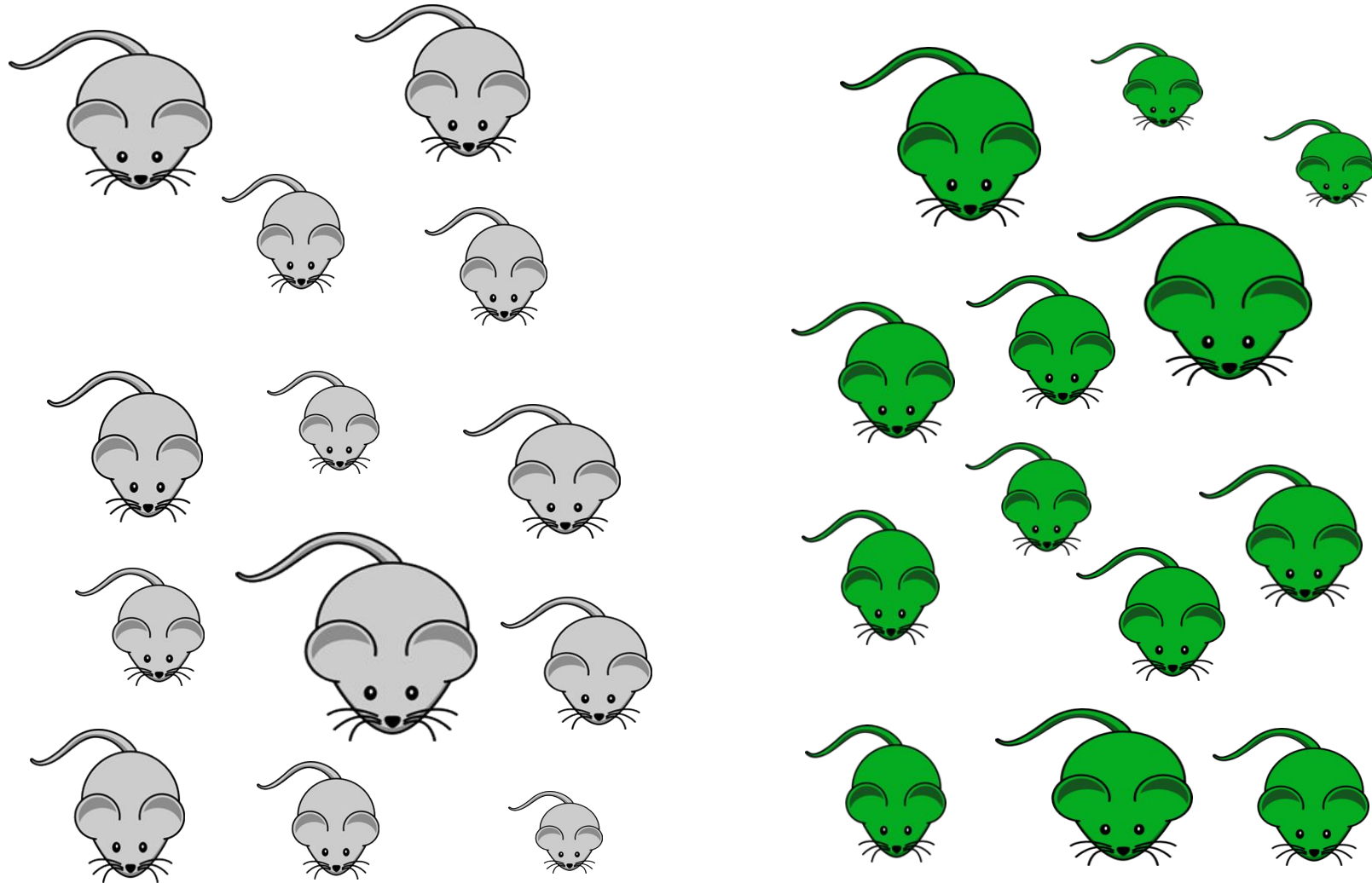
Bad reproducibility



# Population: set of all mice we could measure

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**Sampling must be representative** of the whole population under study !



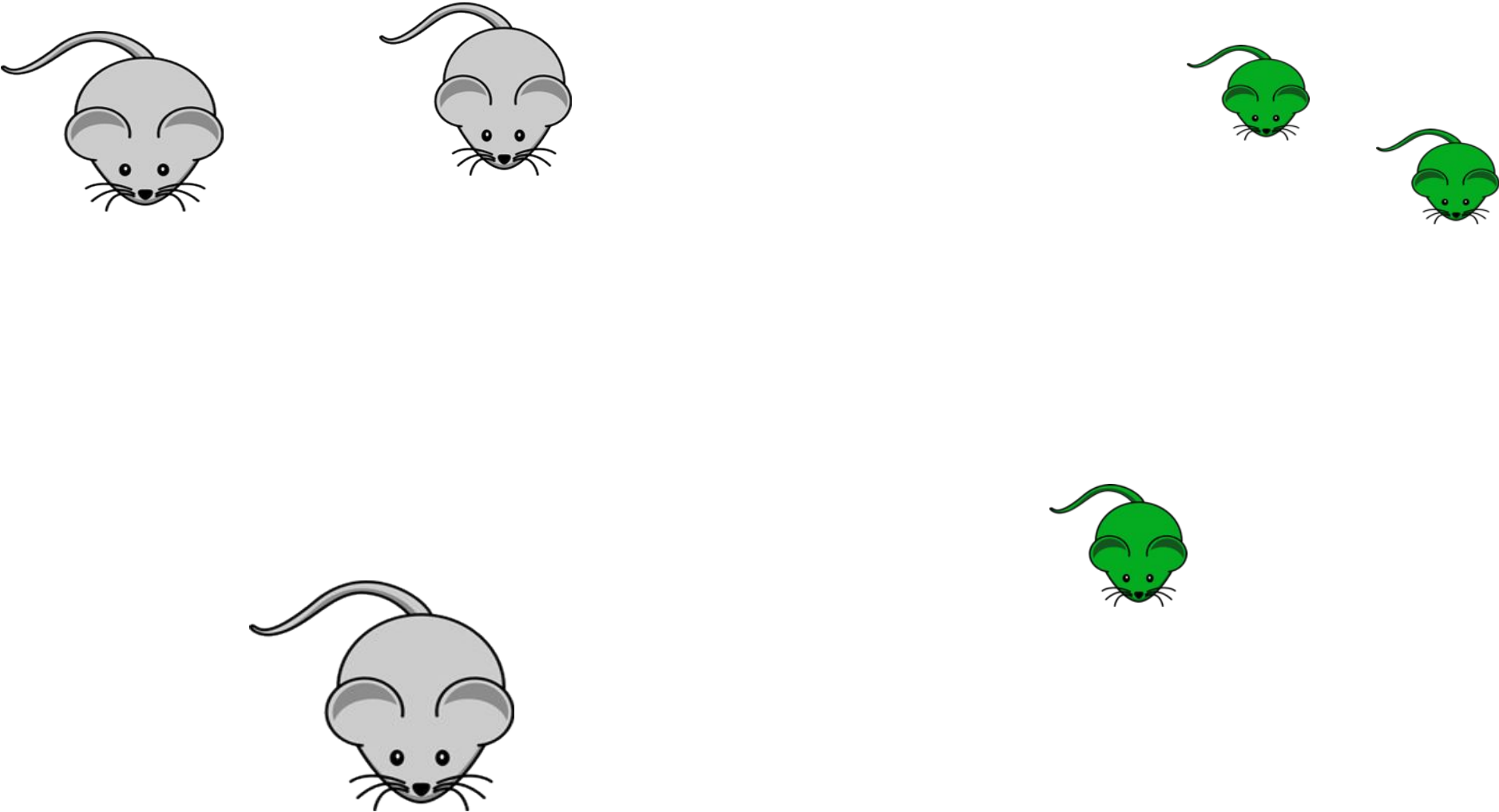
# Sampling 1: selection of 3 mice per condition

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# Sampling 2: non representative

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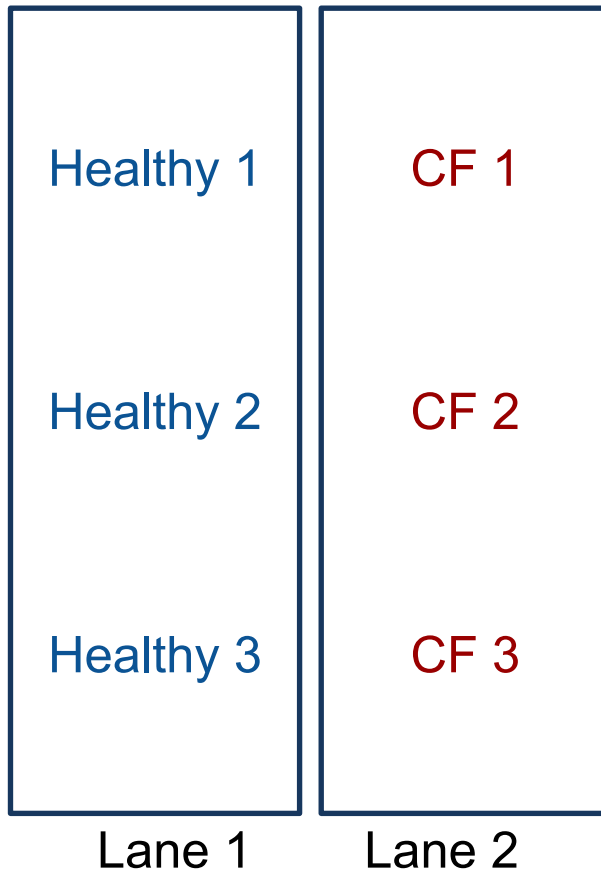


# Sequencing design

## Goal:

Do not add any confounding technical effect (day, lane, run, etc.) to the factor of interest.

Bad example ❌



Good example ✅



Good example ✅





# Sequencing design

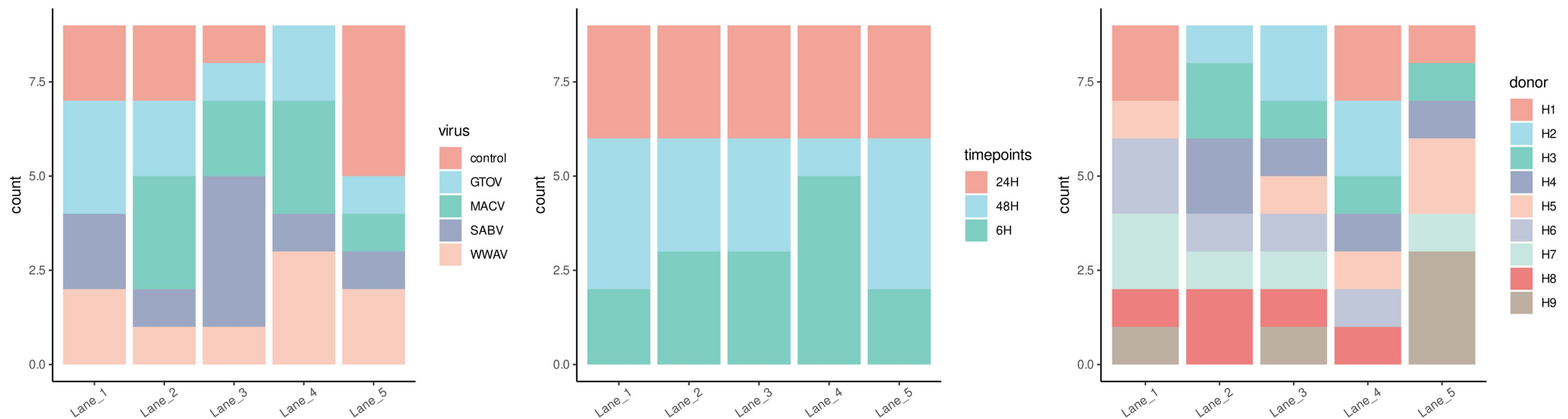
## Goal:

Do not add any confounding technical effect (day, lane, run, etc.) to the factor of interest.

Impossible to cross evenly all sources of technical variation



Randomize !



<https://mixnpick.pasteur.fr/>

# Sequencing design

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## Technical variabilities:

- Lane
- Flowcell
- Run

lane effect < flowcell effect < run effect << biological variability



Use the same multiplexing rate for all the samples!

# Experimental design : Take-home message



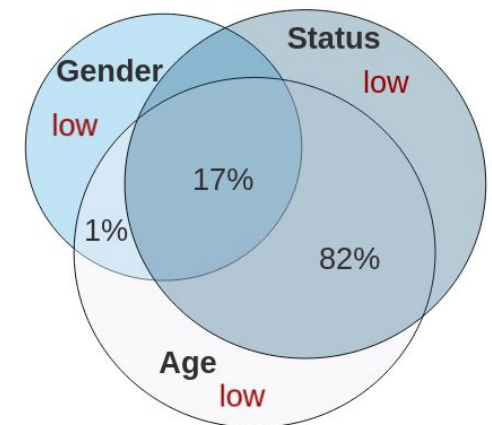
**Express the biological question as accurately as possible** to build an experimental design which will be able to address it.

**The simpler, the better** : If >2 factors, the results may be very difficult to interpret

**Identify all the sources of variability** to avoid confounding effects

- Change of biological condition (e.g. KO vs WT)
- Within replicates variability (e.g. KO1 vs KO2 vs KO3)
- Experimentalist or day effect
- RNA: quality and extraction
- Library: PCR, concentration, random priming, rRNA removal
- Sequencing machine, flowcell and lane, ...

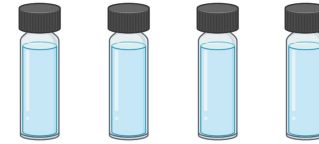
**Flawed design**



# Experimental design : Take-home message

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**Experiments must be replicated** to precisely measure the biological variability associated with the condition under study.



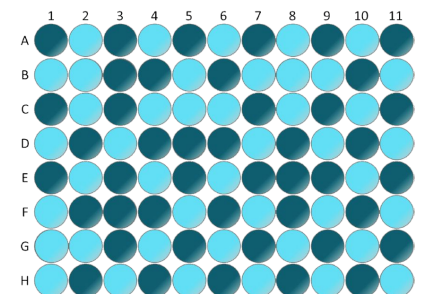
**Sampling must be representative** of the whole population under study



**The higher the within group variability ...** the higher the number of biological replicates, in order to make sure that the whole range of variation is covered

**Ideally, use blocking ...** to ensure that the biological conditions are evenly distributed among factors that are important (unwanted) sources of variability.

**... or randomization** when blocking is not possible



# Outline

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1. Introduction
2. Designing the experiment
- 3. Description/exploration**
4. Normalization
5. Modeling
6. SARTools

# Starting point of the differential analysis

	T0-1	T0-2	T0-3	T4-1	T4-2	T4-3	T8-1	T8-2	T8-3
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...	...	...	...	...	...	...	...	...	...
geneN	18	31	39	4	4	7	2	6	2

**Goal:** find **genes** differentially expressed between biological conditions

# Many plots to produce

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## QC & diagnostics

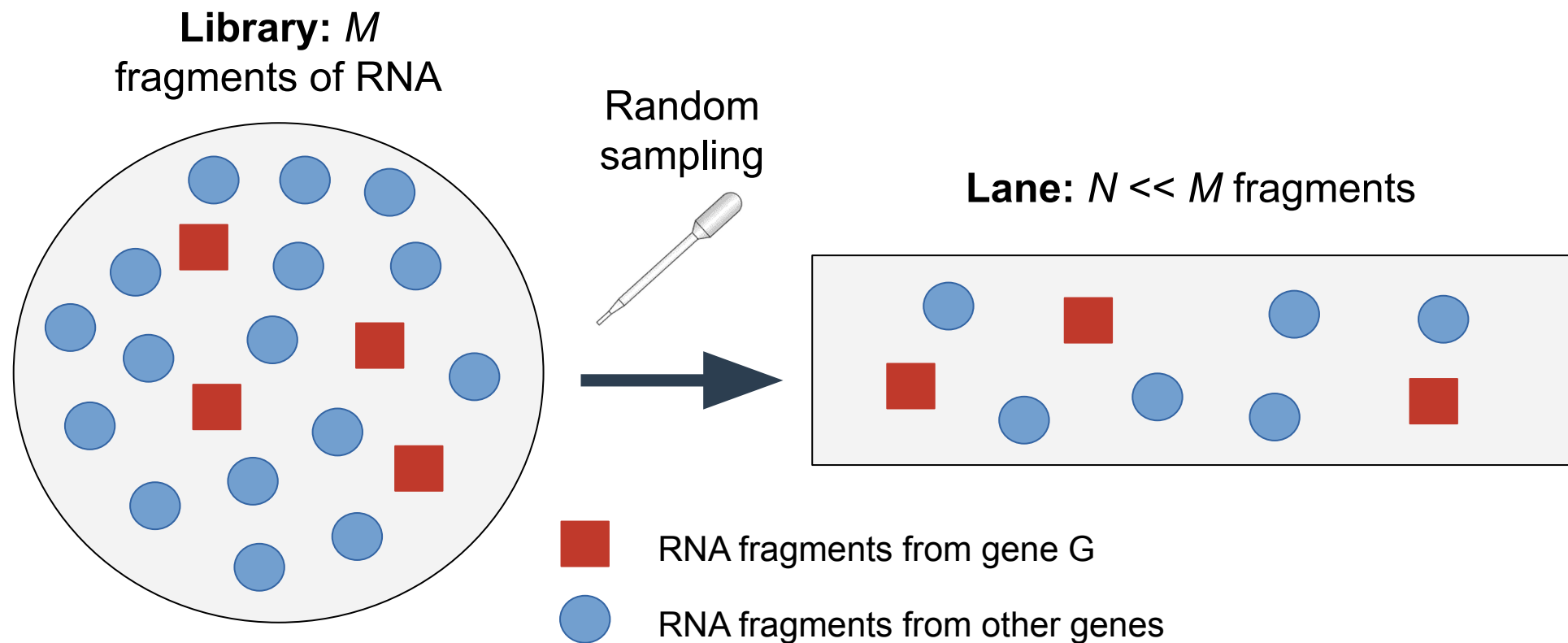
### Description sample by sample:

- Total number of reads
- Percentage of null counts
- Percentage of reads caught by the most expressed gene
- Distribution of the counts

### Multivariate description of the data:

- SERE coefficient for each pair of samples [2]
- Principal Component Analysis
- Hierarchical clustering

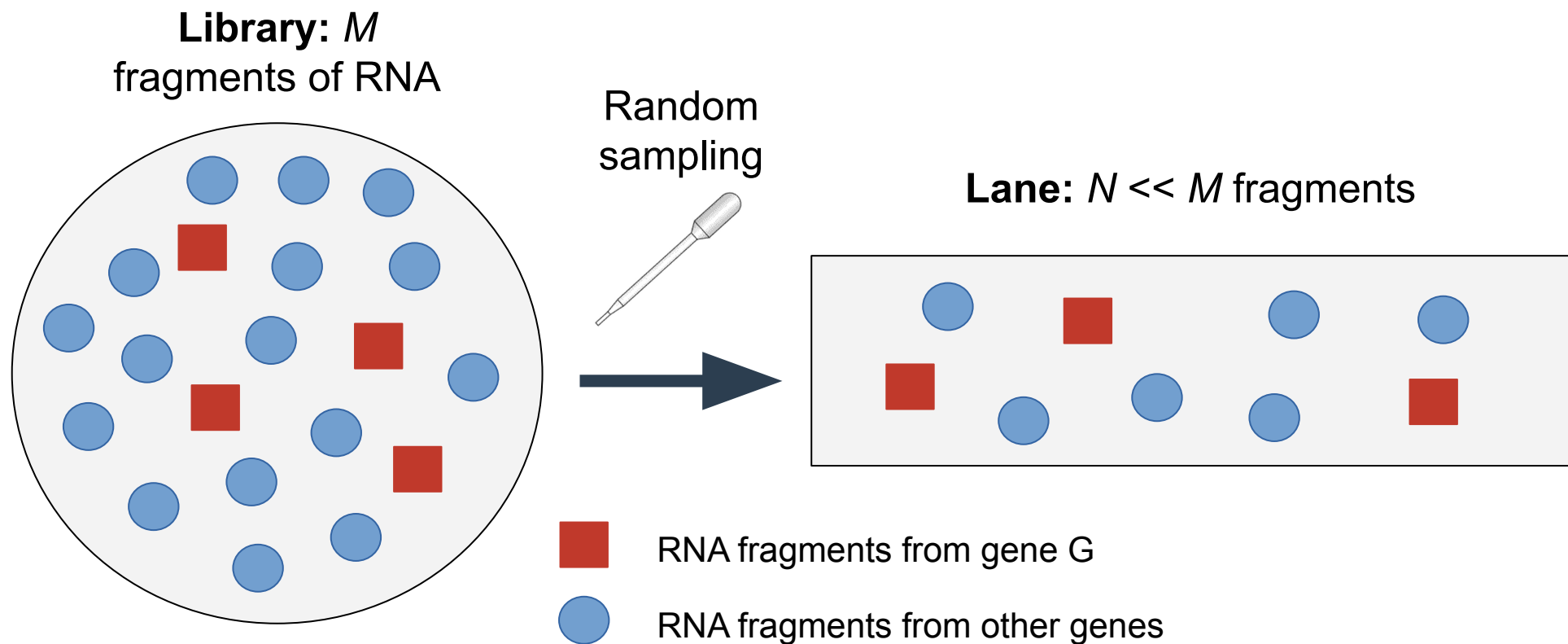
# Distribution of counts data



*“It is a good approximation to say that there is a linear relationship between read counts resulting from a sequencing experiment and the abundance of each sequence in the starting RNA material.” [1]*



# Distribution of counts data



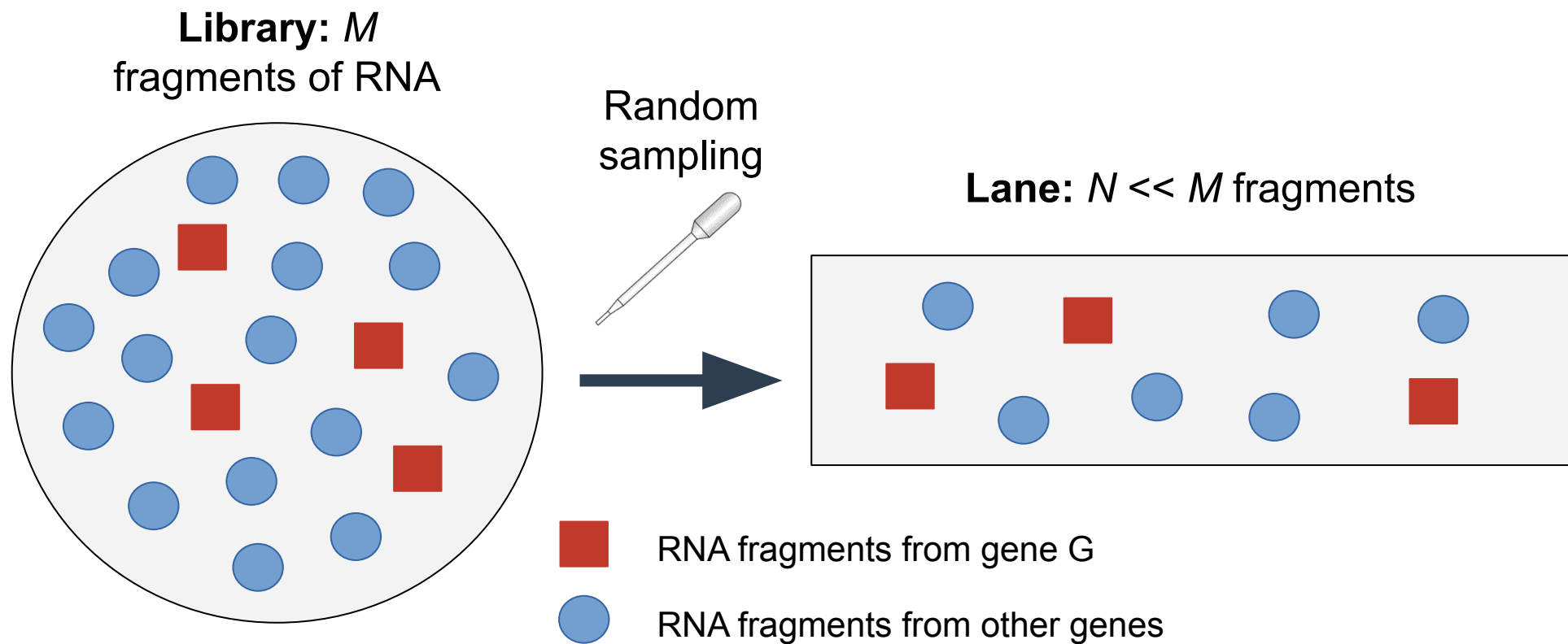
Let  $\pi_G$  = proportion of fragments of gene G:

{read  $R$  comes from gene G}  $\sim$  Bernoulli( $\pi_G$ )

Thus:

$X_G$  = nb. of reads from gene G  $\sim$  Binomial( $N, \pi_G$ )  $\approx$  Poisson( $N\pi_G$ )

# Distribution of counts data



With a deeper sequencing (i.e. larger  $N$ ):

- Higher probability to catch lowly expressed genes
- Higher precision when estimating  $\pi_G$

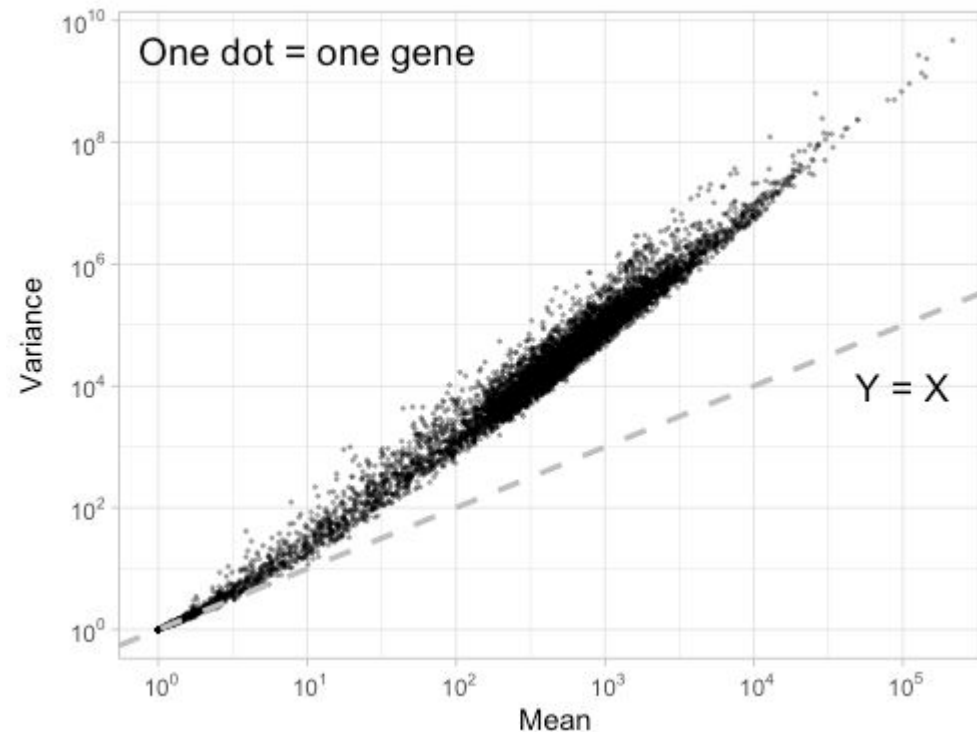
# Distribution of counts data

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If  $X_G \sim \text{Poisson}(N\pi_G)$ :

$$\text{mean}(X_G) = \text{variance}(X_G) = N\pi_G$$

Due to biological variability, we observe over-dispersion:



→ Need a statistical law with variance  $\neq$  mean.

# Distribution of counts data

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Let  $x_{ij}$  the number of reads that align on gene  $i$  for sample  $j$  (intersection row  $i$  - column  $j$  of the count matrix).

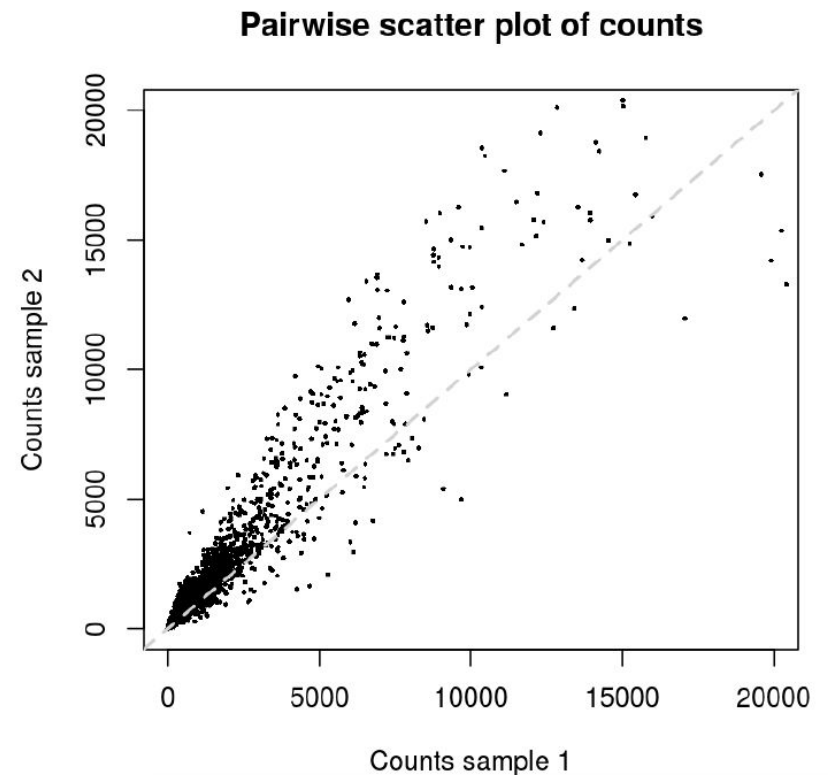
$$x_{ij} \sim \text{Negative-Binomial}(\text{mean} = \mu_{ij}, \text{variance} = \sigma_{ij}^2)$$

where:

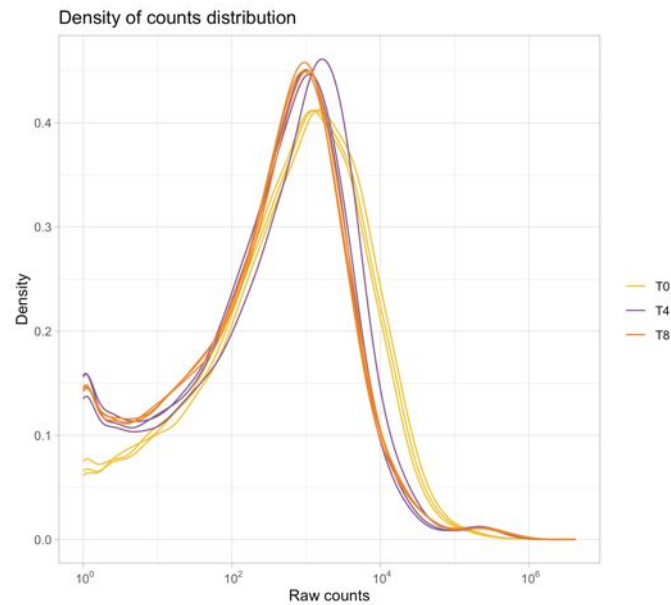
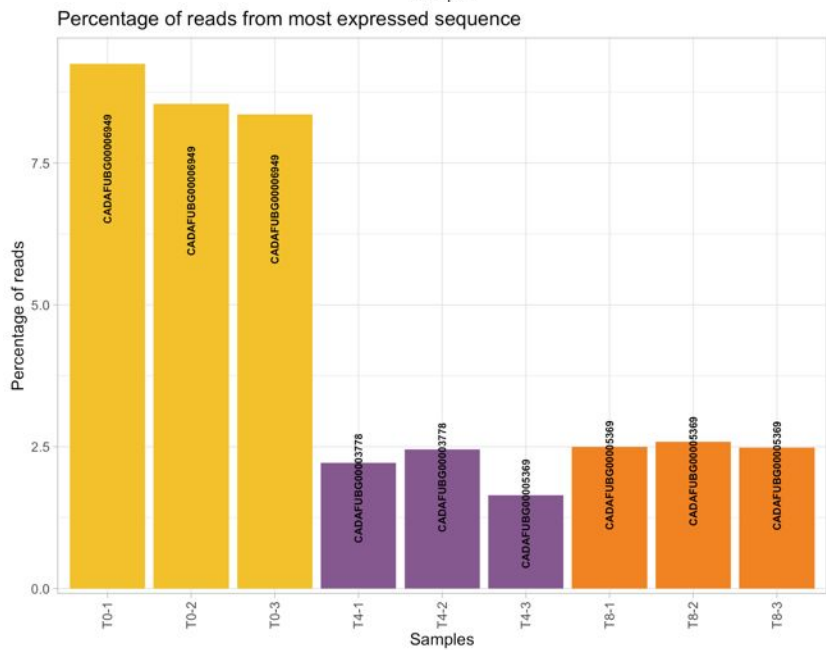
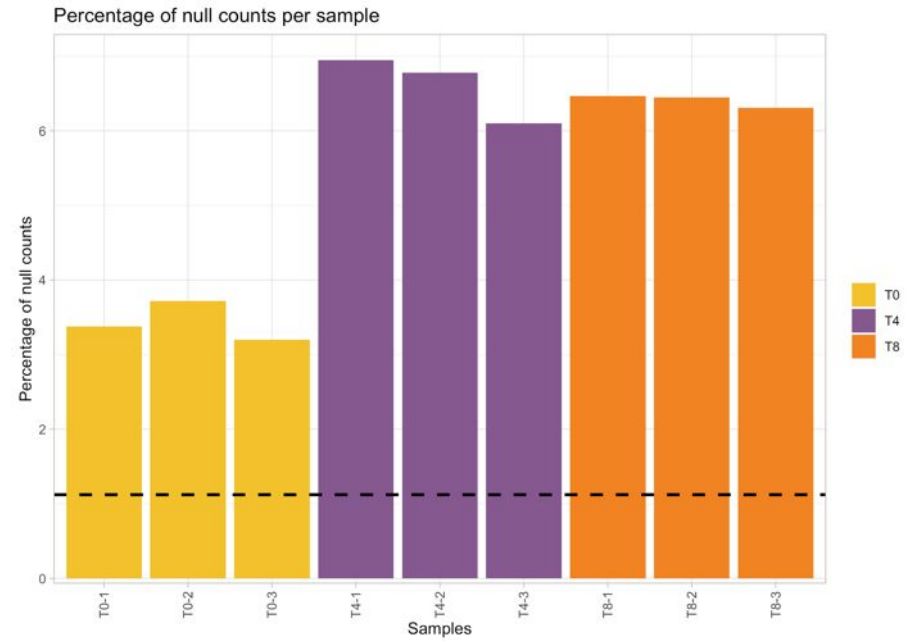
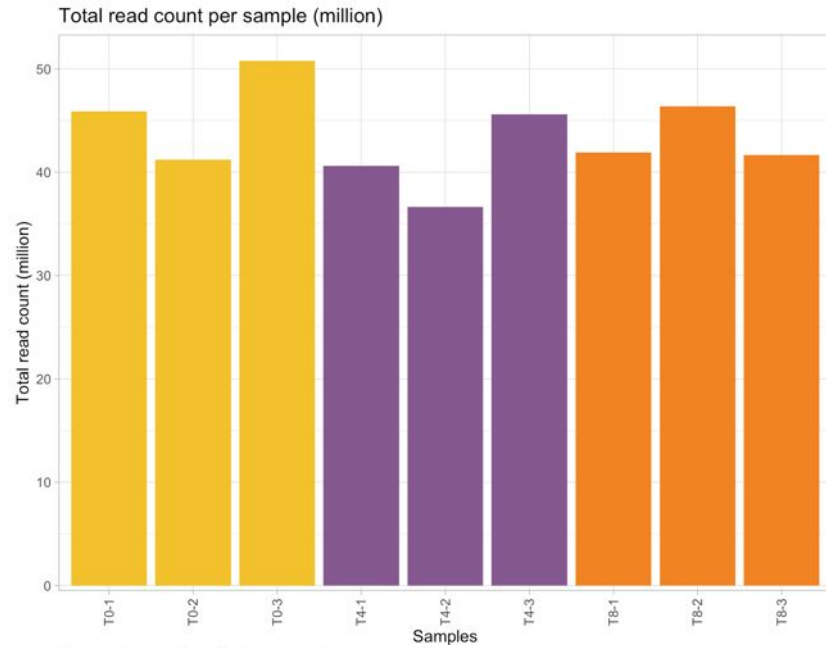
- $\sigma_{ij}^2 = \mu_{ij} + \varphi_i \mu_{ij}^2$
- $\varphi_i$ : biological dispersion of gene  $i$

Particularity:

the  $x_{ij}$ 's are **null or positive integers**.



# Descriptions sample by sample



# Exploratory data analysis (EDA)

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## Two main tools:

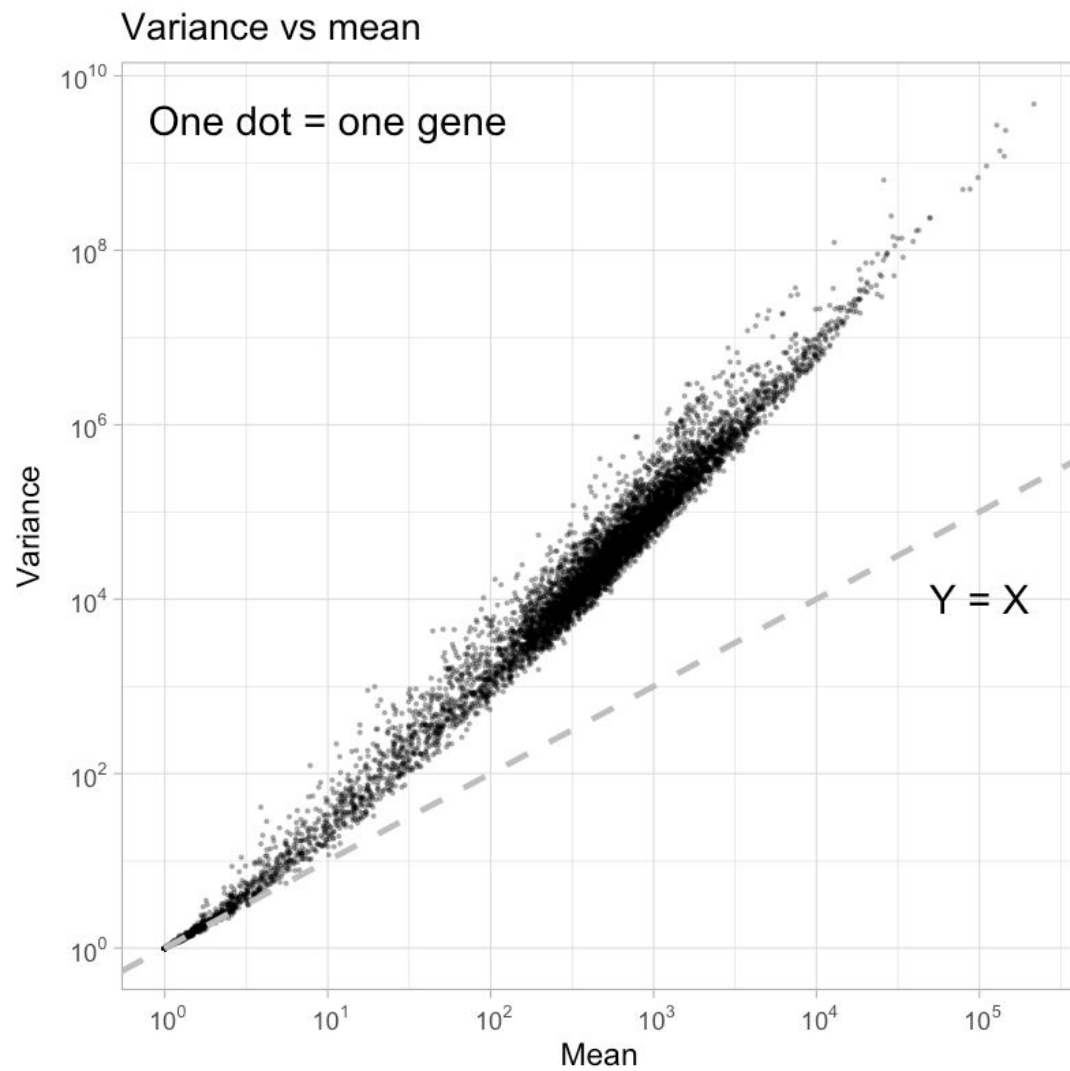
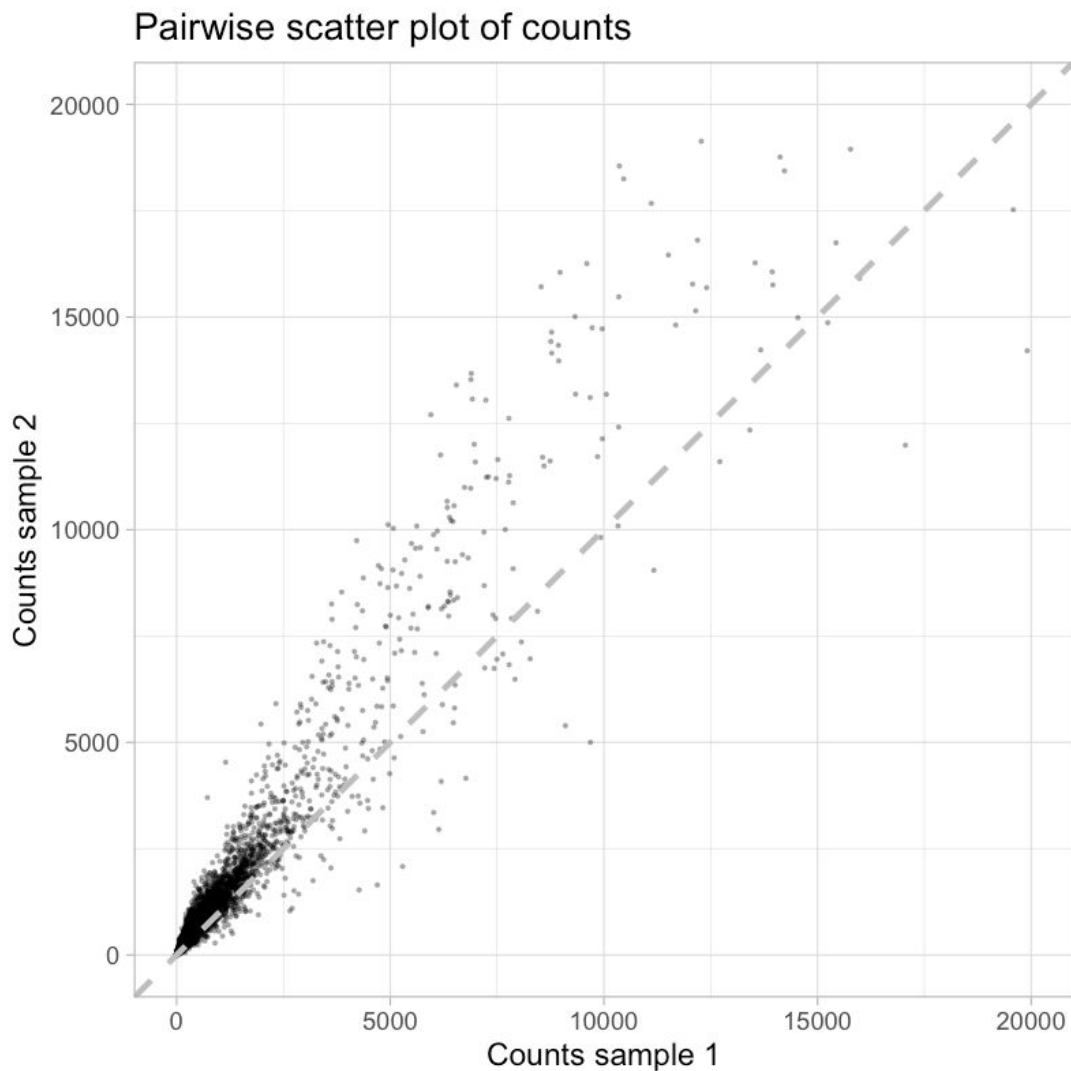
- Principal Component Analysis (PCA)
- Clustering

## Pre-requisite:

- Notion of **distance** between the samples
- Make the data homoscedastic (=homogeneous variance)

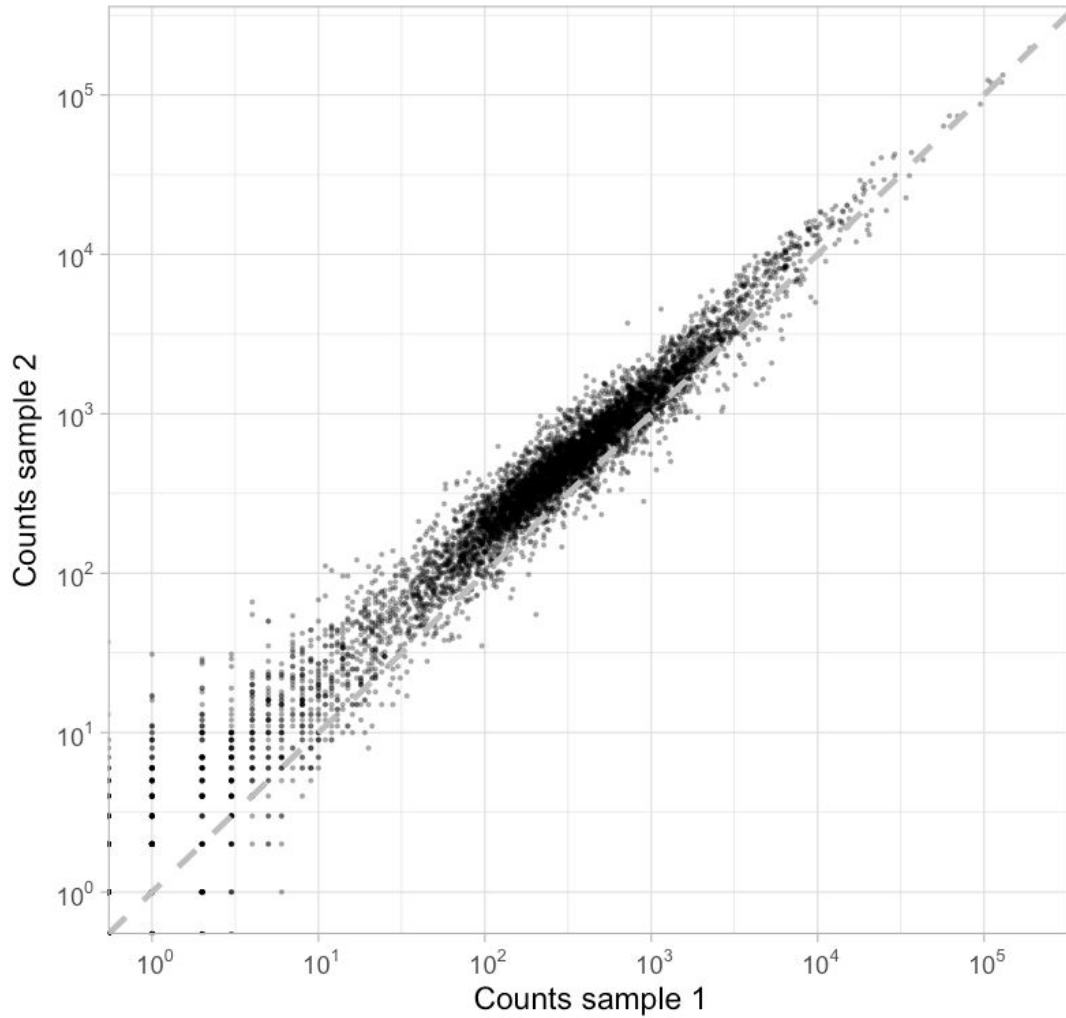
**variance must be independent of the mean**

# Variance increases with intensity

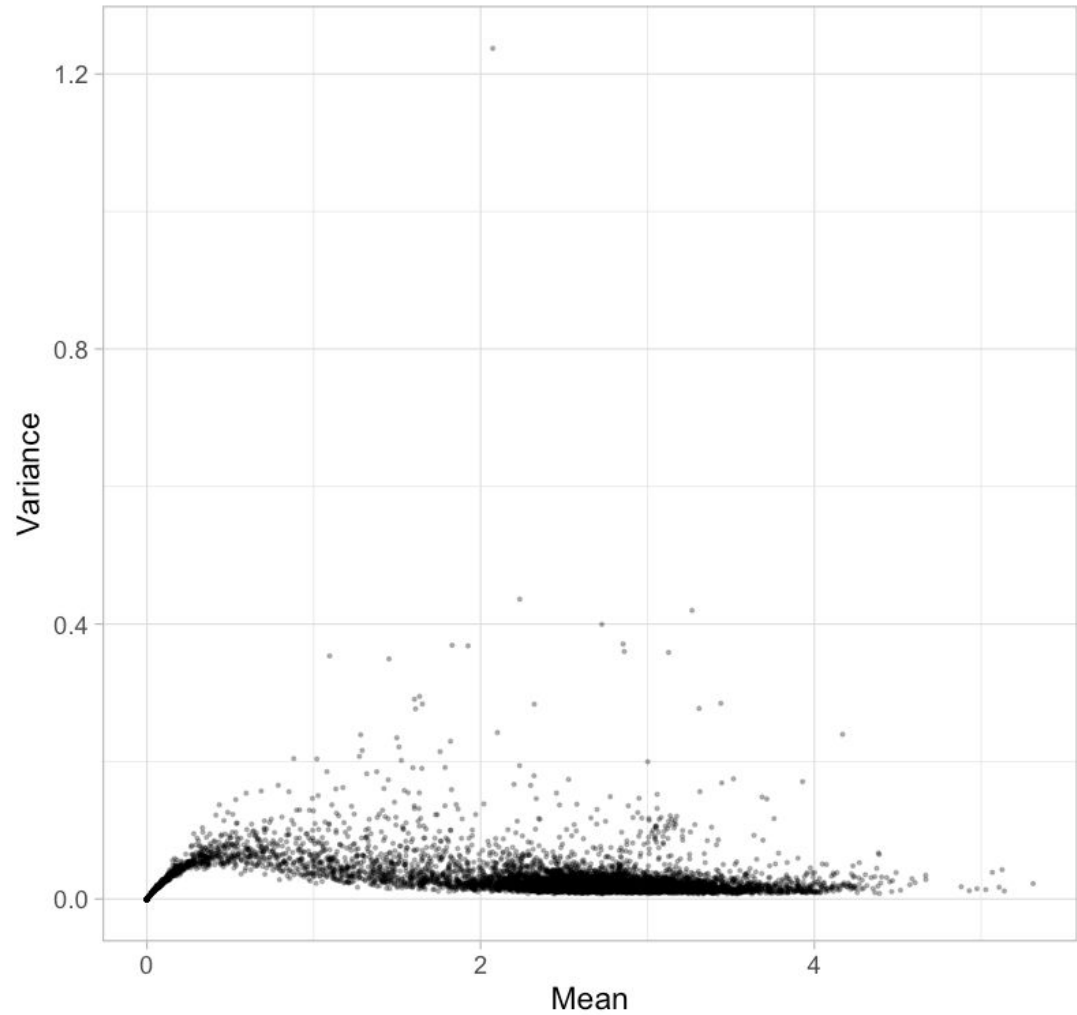


# Log-transformation

Pairwise scatter plot of log-transformed counts



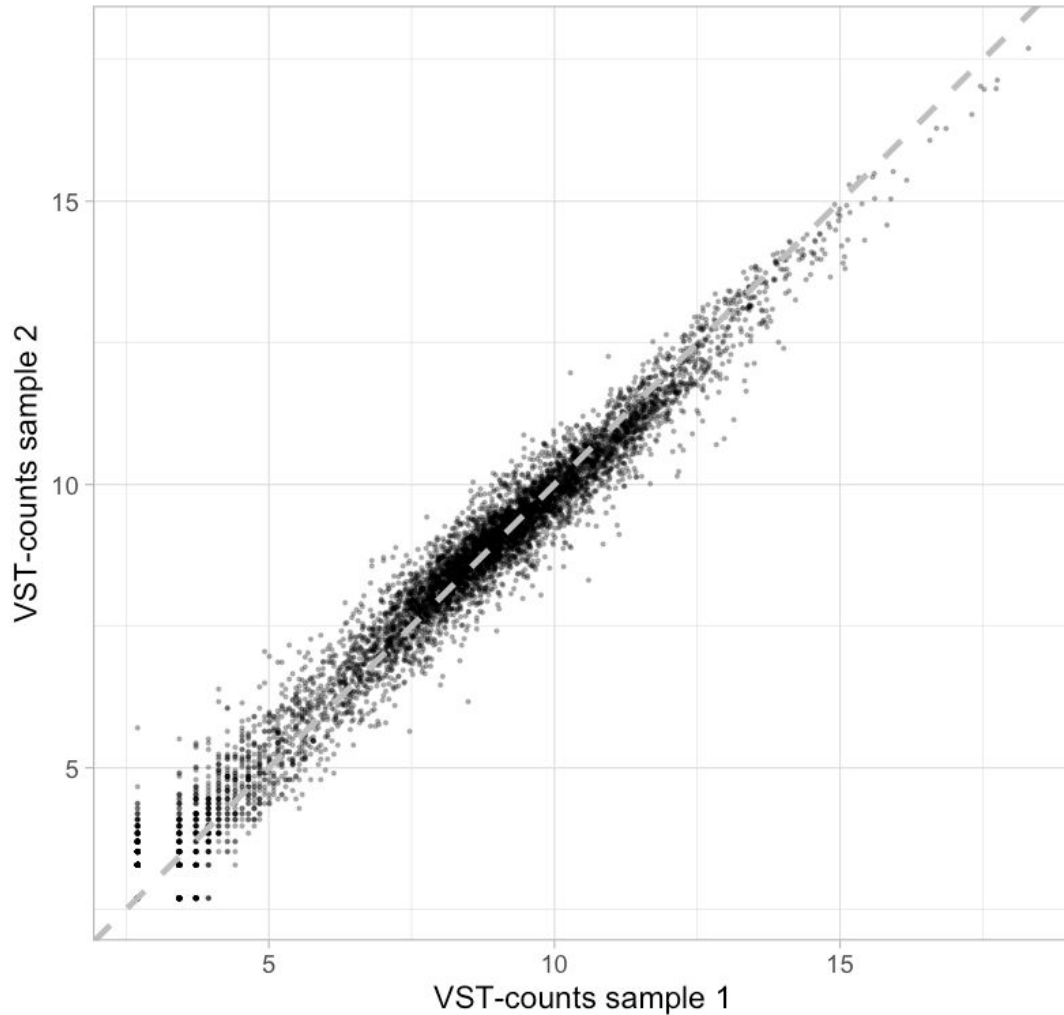
Variance vs mean of log-transformed counts



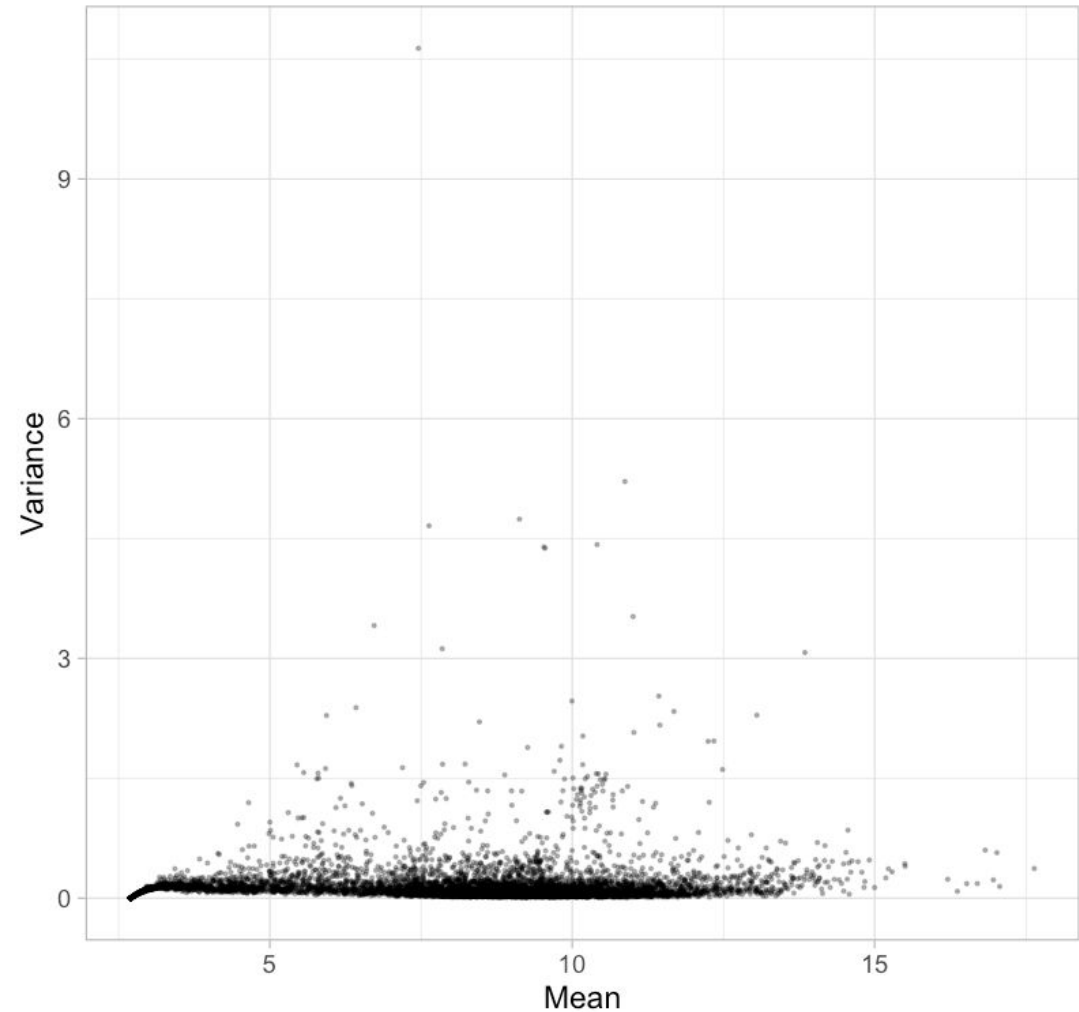


# Variance-Stabilizing Transformation [3]

Pairwise scatter plot of VST-counts



Variance vs mean of VST-counts



**Use these data to perform Exploratory Data Analysis ONLY !**

# Principal Component Analysis (PCA)

---

## Goal:

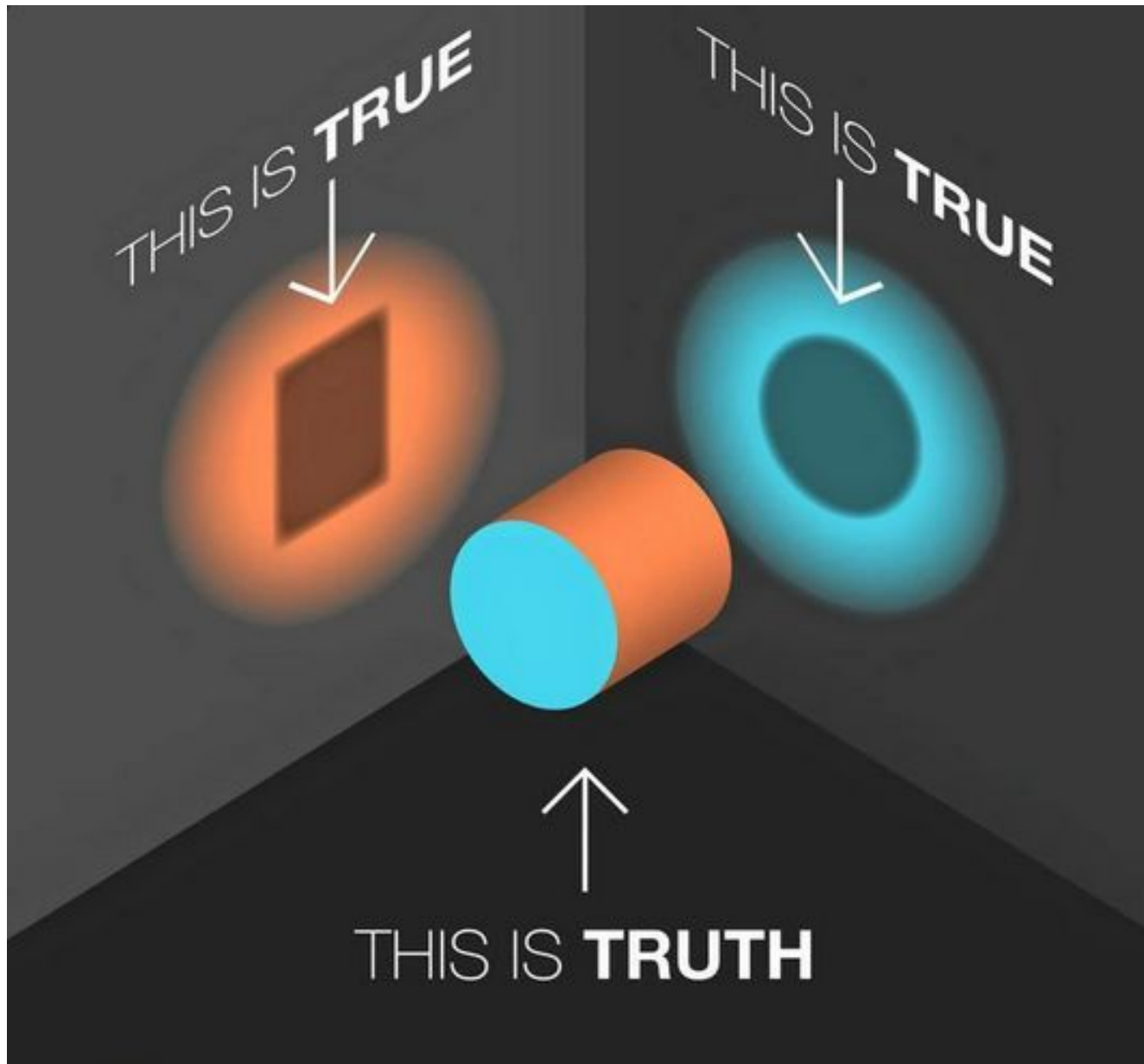
Facilitate the vision of a large (high dimensional) data set.

## Method:

Project a cloud of  $P$  dots (samples) of dimension  $N$  (genes) on a subspace (e.g. a line or a plan) while conserving most of its structure.

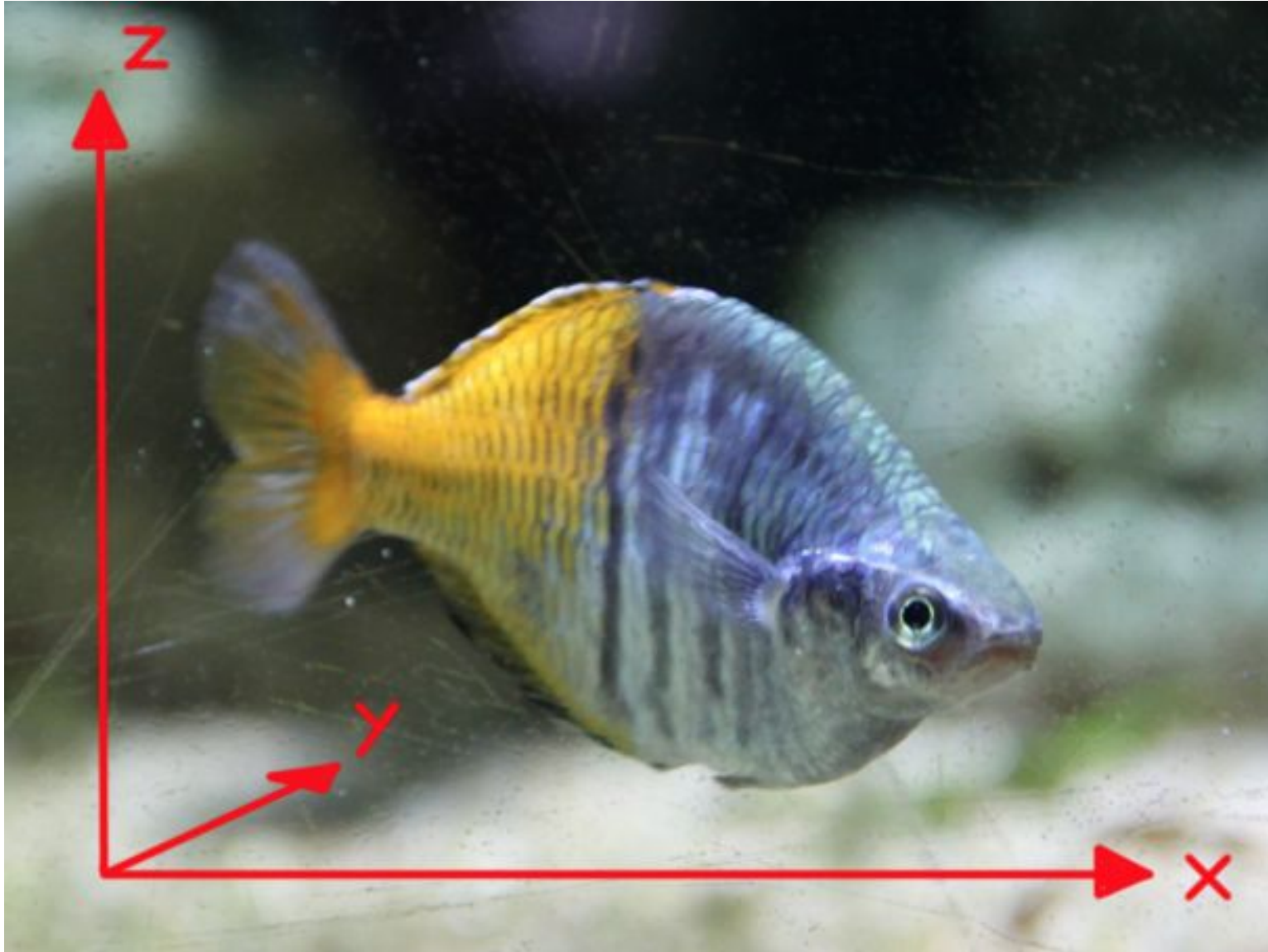


# Projection: loss of information



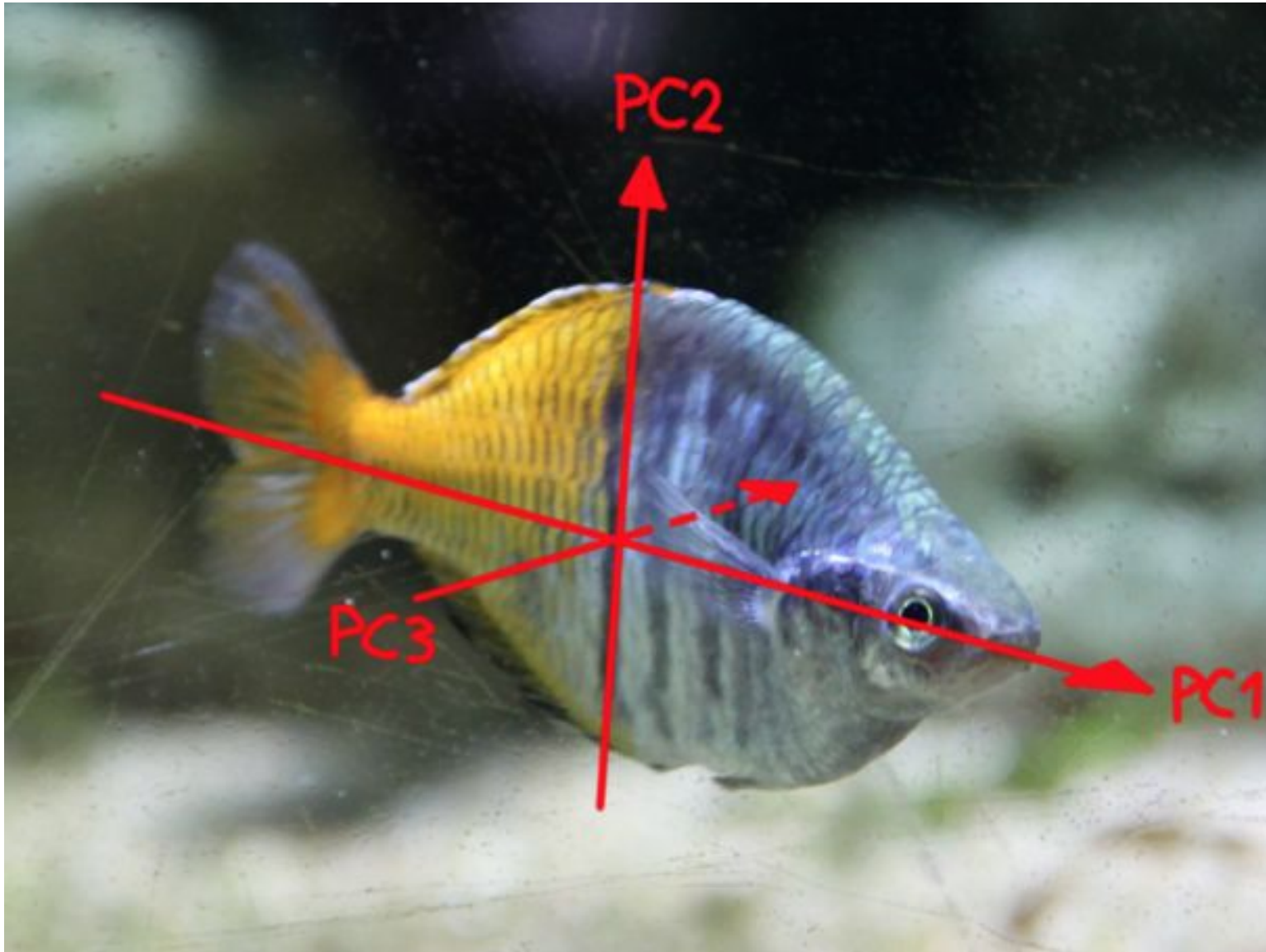
# PCA on a fish (source: bioinfo-fr.net)

---



# PCA on a fish (source: bioinfo-fr.net)

---



# PCA: important scores

---

## Percentage of inertia associated with an axis:

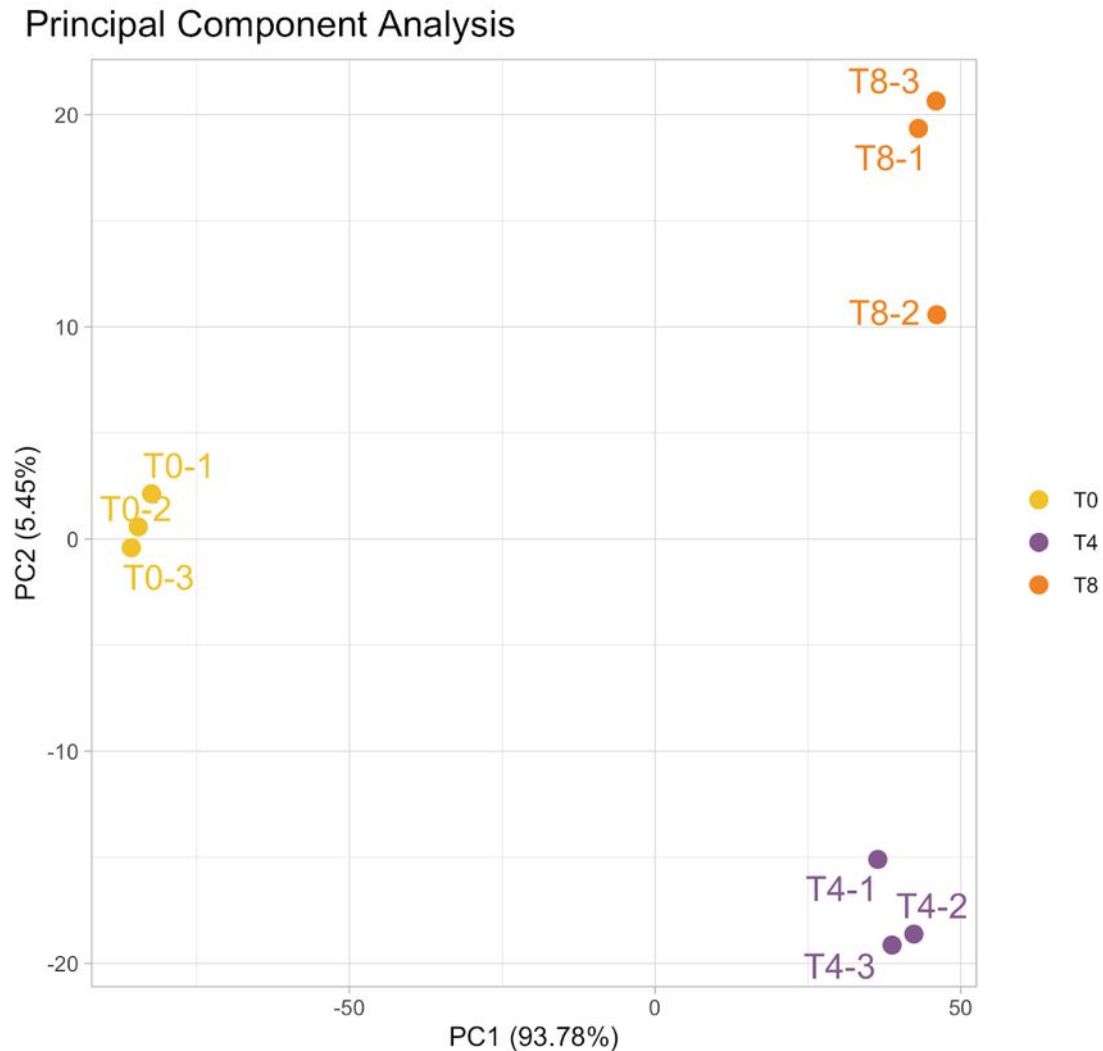
- Proportion of the total information supported by this axis
- Decreases with the axis rank (by construction)

## Number of axes to interpret:

- Such as the sum of the percentages of inertia is  $\geq x\%$
- Elbow criterion
- And many other methods

**Comment:** the data structure is (supposed to be) known in a differential analysis framework.

# PCA: RNA-Seq example



**Pre-requisite:** counts must be transformed (made homoscedastic) before building the PCA.

# PCA: dimensionality reduction

	T0-1	T0-2	T0-3	T4-1	T4-2	T4-3	T8-1	T8-2	T8-3
<b>gene1</b>	6.41	6.35	6.47	5.36	5.54	5.38	5.03	5.41	4.96
<b>gene2</b>	7.07	7.10	7.02	9.21	9.24	9.05	7.69	8.19	7.77
<b>gene3</b>	6.21	6.24	6.12	3.71	4.06	4.32	3.93	4.05	3.91
<b>gene4</b>	7.35	7.34	7.44	6.51	6.12	6.44	6.71	6.47	6.50
<b>gene5</b>	1.04	1.24	0.62	0.16	0.17	0.50	1.02	0.97	1.26
<b>gene6</b>	0.69	0.04	0.36	0.12	0.67	0.80	2.02	1.28	1.32
<b>gene7</b>	0.24	0.69	-0.01	-0.76	-0.74	-0.79	-0.72	-0.74	-0.72
...	3.29	3.76	3.18	4.74	3.98	3.47	4.31	4.95	4.65
<b>geneN</b>	3.65	4.17	4.13	5.96	6.17	5.65	4.09	4.02	3.98

From genes/variables to principal components

<b>PC1</b>	-60.1	-61.0	-61.5	25.9	30.4	28.8	31.0	33.1	33.3
<b>PC2</b>	1.3	0.5	-0.1	-11.9	-14.0	-15.0	15.1	7.9	16.3
<b>PC3</b>	0.4	0.3	0.1	-0.1	-0.2	-0.3	0.1	0	-0.1
<b>PC4</b>	-0.2	0	-0.1	0.1	0.1	0.2	-0.1	-0.2	0.2



# PCA: confounding effect

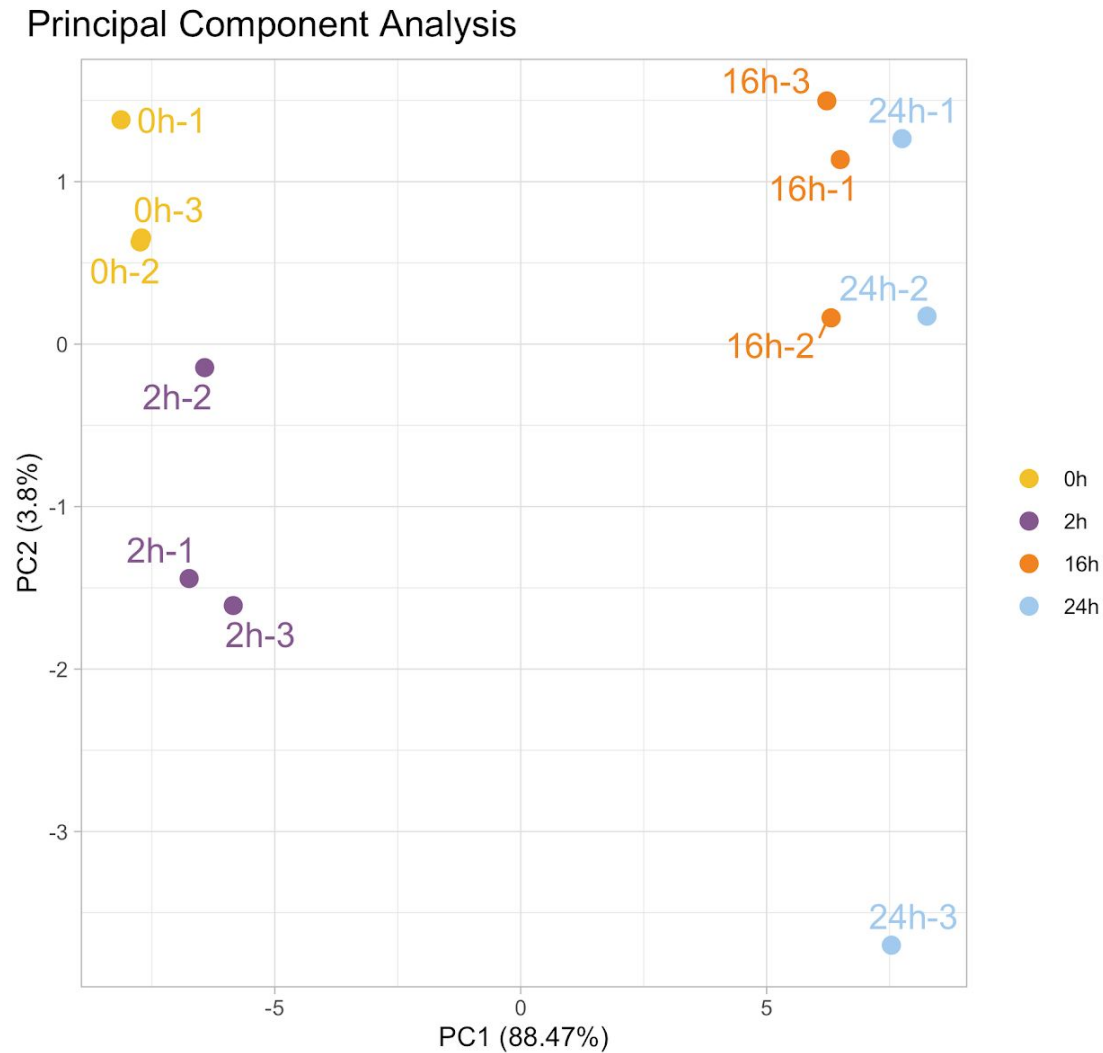
Transcriptome study of a bacteria at 0h, 2h, 16h and 24h:



label	time	replicate	date	libraries_method	libraries_exp	libraries_date
0h-1	0h	r1	oct18	robot	Bob	nov18
0h-2	0h	r2	oct18	robot	Bob	nov18
0h-3	0h	r3	oct18	robot	Bob	nov18
2h-1	2h	r1	oct18	robot	Bob	nov18
2h-2	2h	r2	oct18	robot	Bob	nov18
2h-3	2h	r3	oct18	robot	Bob	nov18
16h-1	16h	r1	oct18	robot	Bob	nov18
16h-2	16h	r2	oct18	robot	Bob	nov18
16h-3	16h	r3	oct18	robot	Bob	nov18
24h-1	24h	r1	oct18	robot	Bob	nov18
24h-2	24h	r2	oct18	robot	Bob	nov18
24h-3	24h	r3	oct18	robot	Bob	nov18

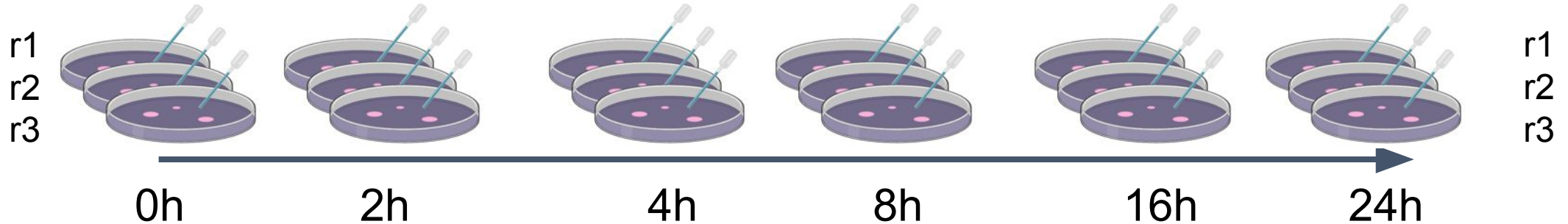
# PCA: confounding effect

Transcriptome study of a bacteria at 0h, 2h, 16h and 24h:



# PCA: confounding effect

Add samples 4h and 8h from the same cultures:



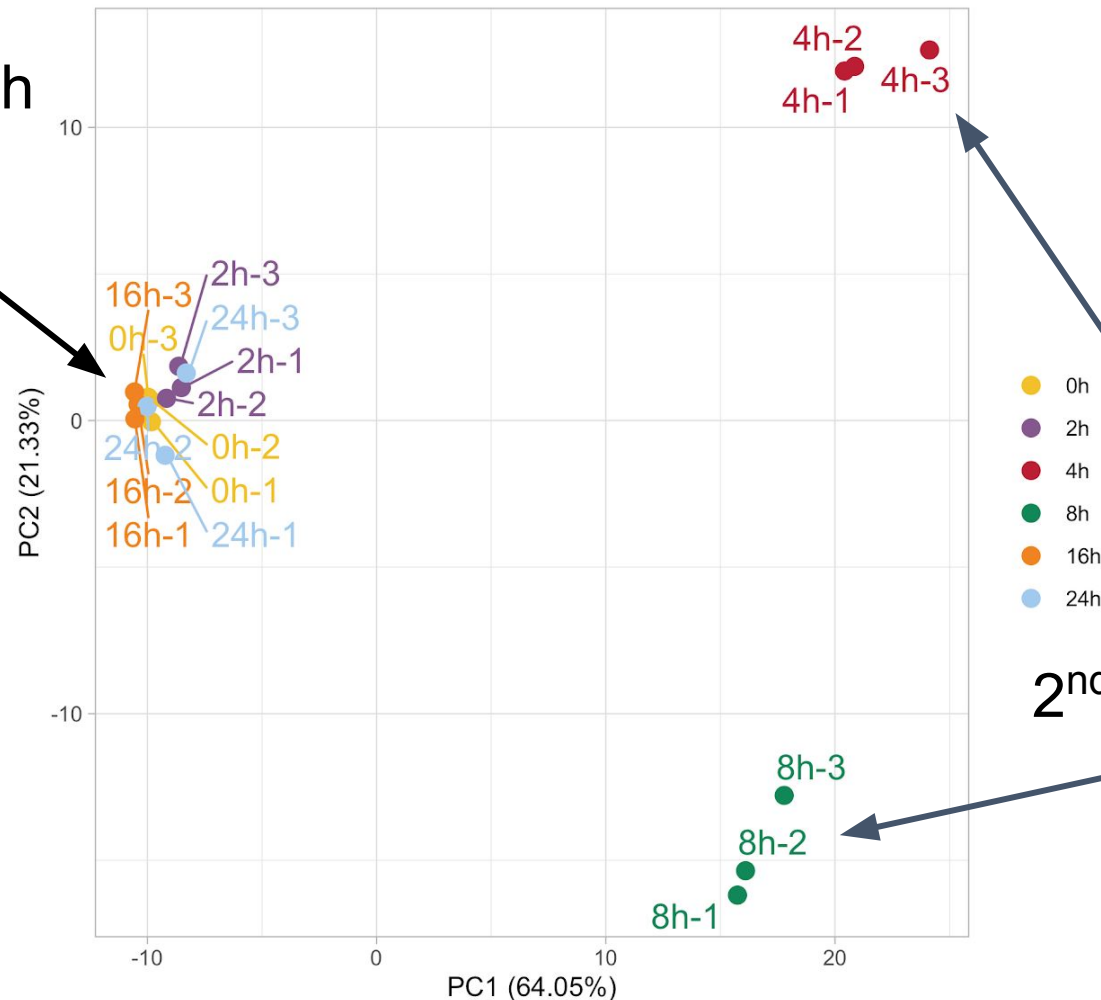
label	time	replicate	date	libraries_method	libraries_exp	libraries_date
0h-1	0h	r1	oct18	robot	Bob	nov18
0h-2	0h	r2	oct18	robot	Bob	nov18
0h-3	0h	r3	oct18	robot	Bob	nov18
2h-1	2h	r1	oct18	robot	Bob	nov18
2h-2	2h	r2	oct18	robot	Bob	nov18
2h-3	2h	r3	oct18	robot	Bob	nov18
<b>4h-1</b>	<b>4h</b>	<b>r1</b>	<b>oct18</b>	<b>manual</b>	<b>Donald</b>	<b>jun19</b>
<b>4h-2</b>	<b>4h</b>	<b>r2</b>	<b>oct18</b>	<b>manual</b>	<b>Donald</b>	<b>jun19</b>
<b>4h-3</b>	<b>4h</b>	<b>r3</b>	<b>oct18</b>	<b>manual</b>	<b>Donald</b>	<b>jun19</b>
<b>8h-1</b>	<b>8h</b>	<b>r1</b>	<b>oct18</b>	<b>manual</b>	<b>Donald</b>	<b>jun19</b>
<b>8h-2</b>	<b>8h</b>	<b>r2</b>	<b>oct18</b>	<b>manual</b>	<b>Donald</b>	<b>jun19</b>
<b>8h-3</b>	<b>8h</b>	<b>r3</b>	<b>oct18</b>	<b>manual</b>	<b>Donald</b>	<b>jun19</b>
16h-1	16h	r1	oct18	robot	Bob	nov18
16h-2	16h	r2	oct18	robot	Bob	nov18
16h-3	16h	r3	oct18	robot	Bob	nov18
24h-1	24h	r1	oct18	robot	Bob	nov18
24h-2	24h	r2	oct18	robot	Bob	nov18
24h-3	24h	r3	oct18	robot	Bob	nov18

# PCA: confounding effect

Global analysis of times 0h, 2h, 4h, 8h, 16h and 24h:

Principal Component Analysis

1<sup>st</sup> sequencing batch



2<sup>nd</sup> sequencing batch



# PCA: pairing factor

---

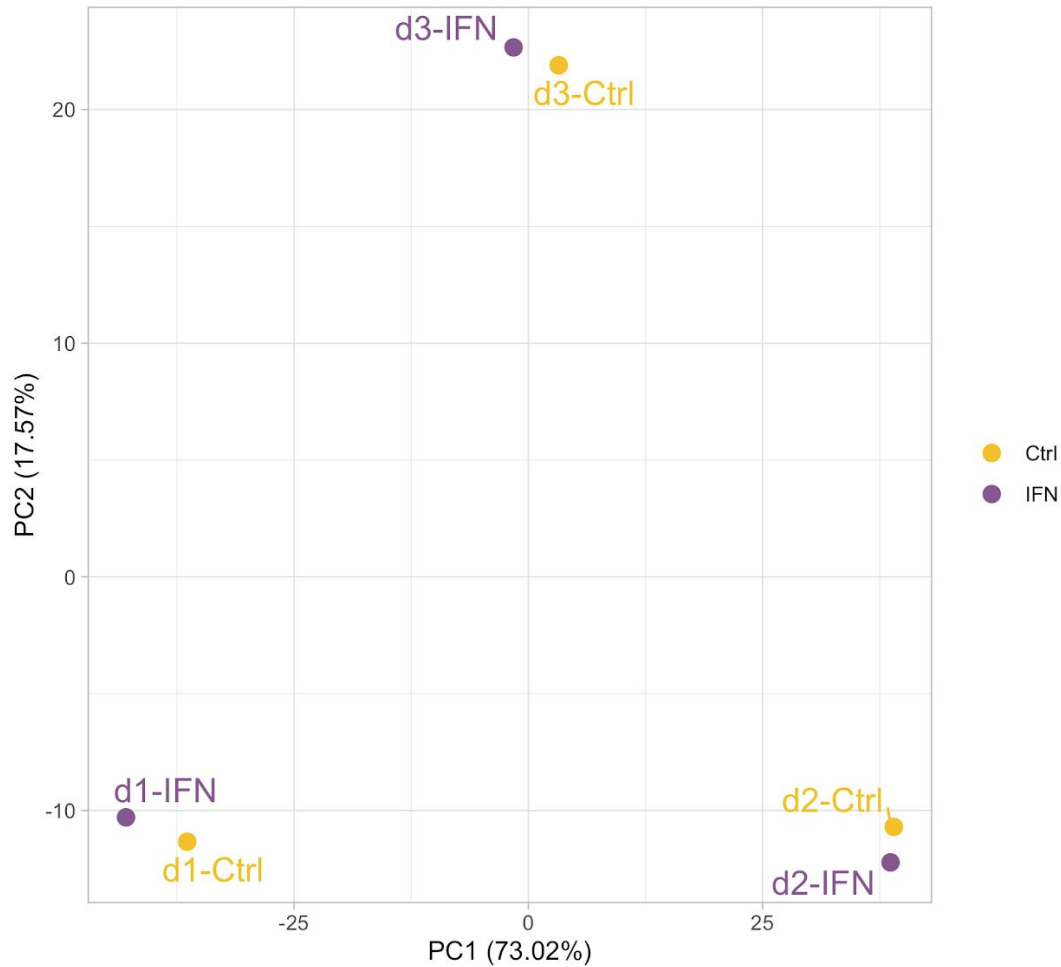
Two treatments applied to human cells coming from 3 donors:

<b>label</b>	<b>treatment</b>	<b>donor</b>
d1-IFN	IFN	d1
d1-Ctrl	Ctrl	d1
d2-IFN	IFN	d2
d2-Ctrl	Ctrl	d2
d3-IFN	IFN	d3
d3-Ctrl	Ctrl	d3

# PCA: pairing factor

Two treatments applied to human cells coming from 3 donors:

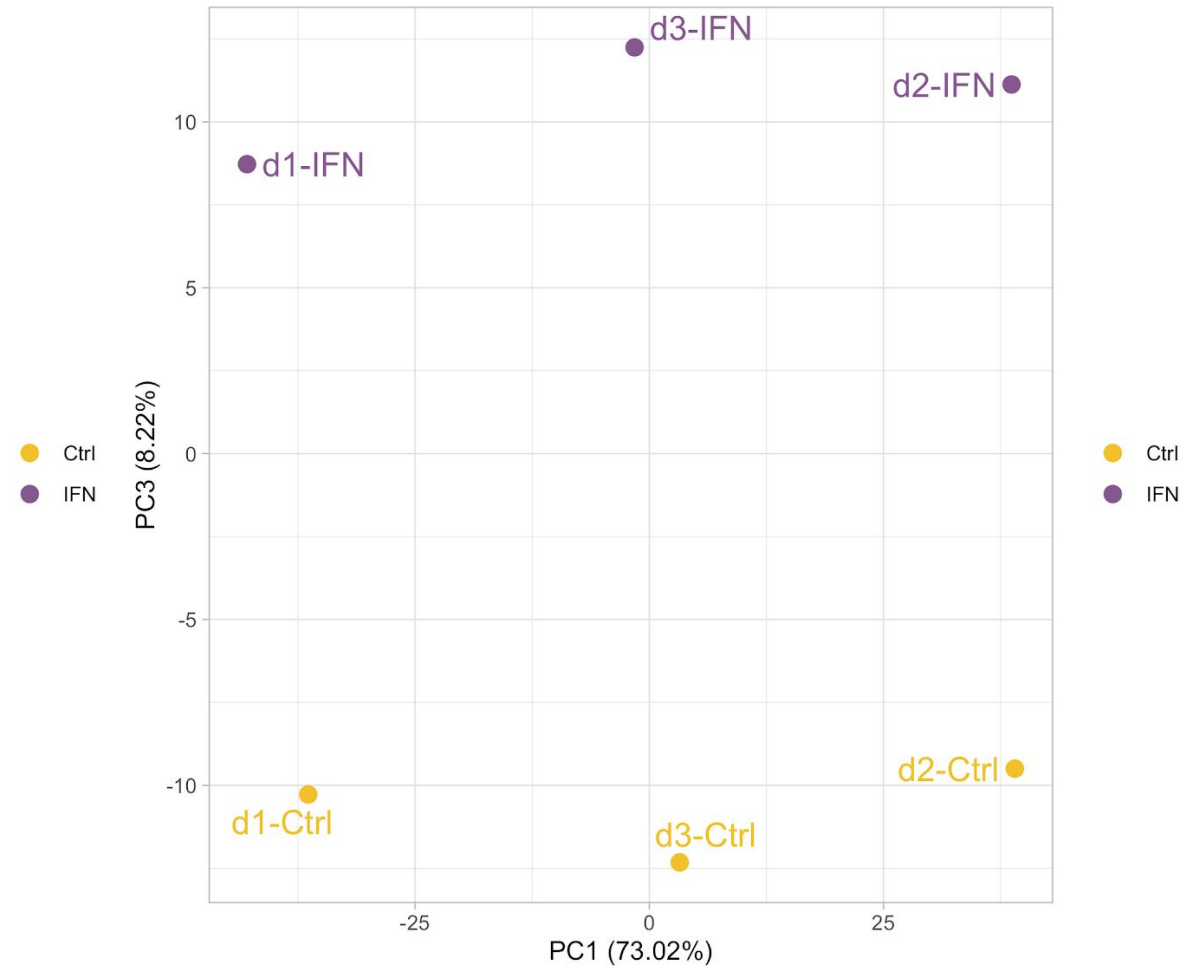
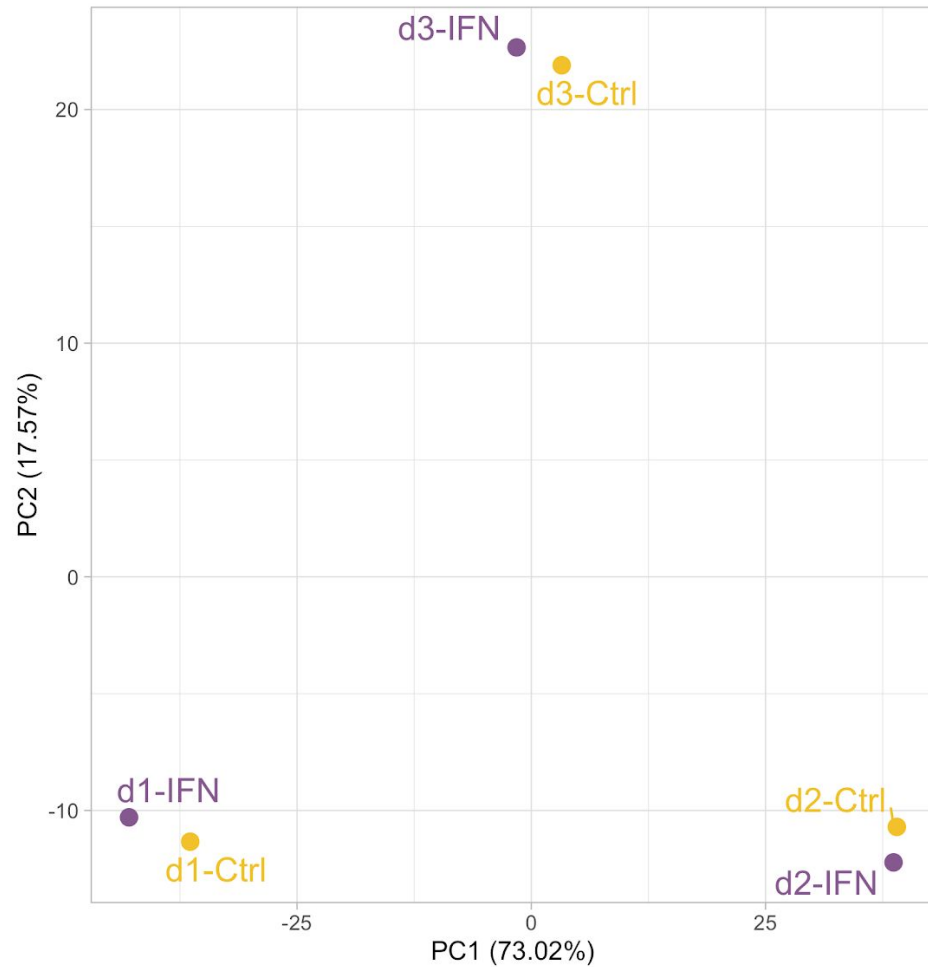
Principal Component Analysis



# PCA: pairing factor

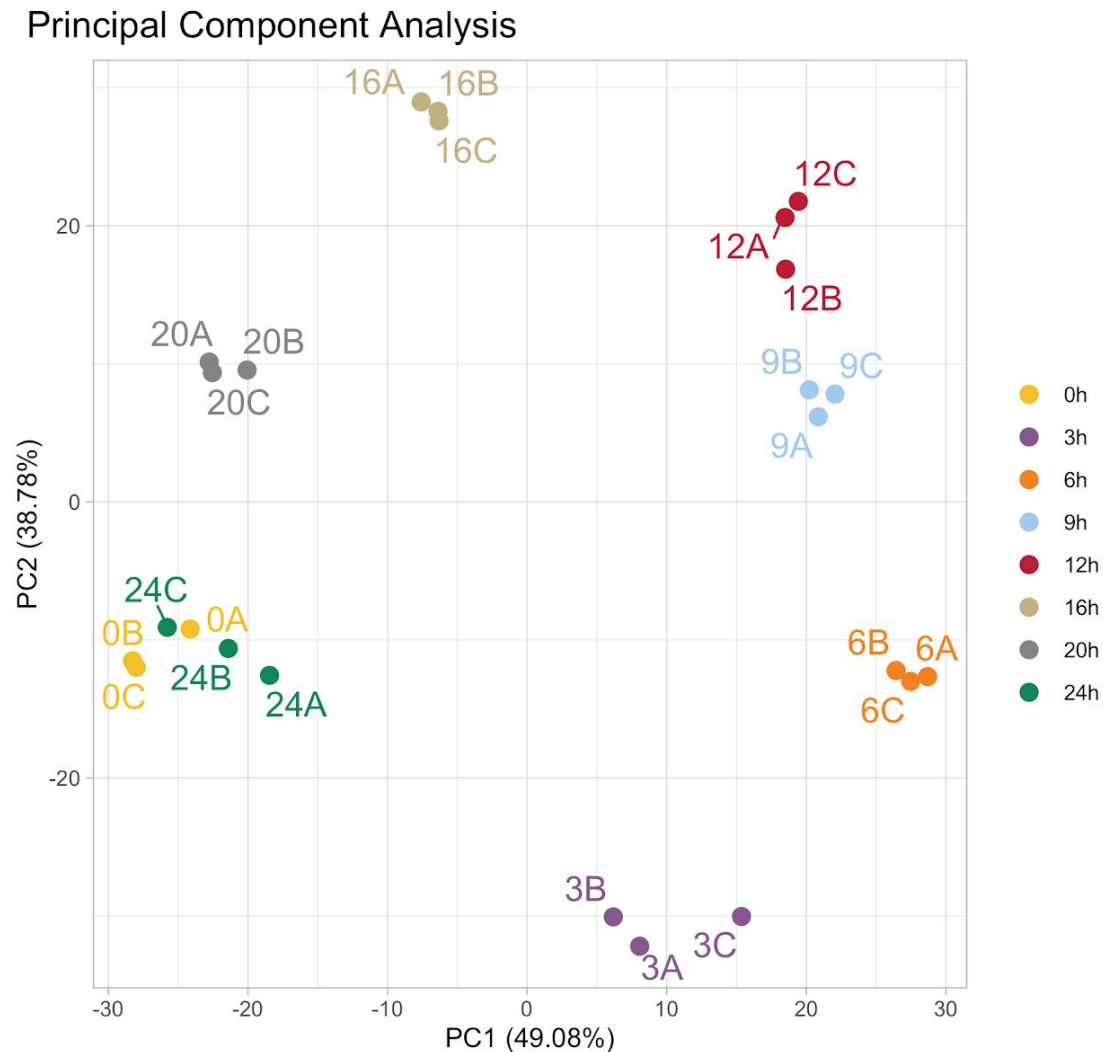
Two treatments applied to human cells coming from 3 donors:

Principal Component Analysis



# PCA: most beautiful RNA-Seq example

Transcriptome study of a cyanobacteria at 8 time points from 0h to 24h:





# SERE coefficient [2]

---

## Simple Error Ratio Estimate

**Goal:** assess the similarity/dissimilarity between samples

$$\text{SERE}(A, B) \begin{cases} = 0 & \text{if } A = B \\ \approx 1 & \text{if } A \text{ and } B \text{ are technical replicates} \\ > 1 & \text{if } A \text{ and } B \text{ are biological replicates} \\ \gg 1 & \text{if } A \text{ and } B \text{ come from different bio. conditions} \end{cases}$$



More suited to RNA-Seq data than the Pearson/Spearman correlation coefficients.

# SERE coefficient: details

---

- 2 samples (A and B) and  $N$  genes under study
- $y_{ij}$  = # of reads for gene  $i$  ( $1, \dots, N$ ) and sample  $j$  (A or B)
- $L_j$  = total # of reads (library size) for sample  $j$
- $E_i = y_{iA} + y_{iB}$  = number of reads for gene  $i$
- Expected # of reads for gene  $i$  and sample  $j$ :

$$\hat{y}_{ij} = E_i \times L_j / (L_A + L_B)$$

- **Expected variation** for each observation  $y_{ij}$ :  $(y_{ij} - \hat{y}_{ij})^2$
- **Expected variation** under Poisson assumption:  $\hat{y}_{ij}$
- Overdispersion for each gene  $i$ :  $s_i^2 = (y_{iA} - \hat{y}_{iA})^2 / \hat{y}_{iA} + (y_{iB} - \hat{y}_{iB})^2 / \hat{y}_{iB}$

$$\text{SERE}(A, B) = \text{sqrt}((\sum_{i=1..N} s_i^2) / N)$$

# SERE coefficient: details

---

## Simple Error Ratio Estimate (SERE)

Given a set of  $N$  exons and  $M$  lanes, let  $y_{ij}$  denote the number of reads covering the  $i^{\text{th}}$  exon in the  $j^{\text{th}}$  lane. Let  $L_j$  be the total read count for lane  $j$ ,  $E_i$  the total for exon  $i$ , and  $T$  the grand total count across all lanes and exons. Under the hypothesis that the lanes are simple technical replicates of each other, they will have a Poisson distribution with one parameter. This parameter can be thought of as the expected number of reads for the lane  $j$  and the exon  $i$ . Its estimate can be calculated using eq. 1.

$$\hat{y}_{ij} = \frac{E_i L_j}{T}$$

The expected variation for each observation  $y_{ij}$  is  $(y_{ij} - \hat{y}_{ij})^2$ , and the expected variation under the Poisson assumption is  $\hat{y}_{ij}$ . This gives a per exon overdispersion estimate of:

$$s_i^2 = \frac{1}{M-1} \sum_j \frac{(y_{ij} - \hat{y}_{ij})^2}{\hat{y}_{ij}}$$

The denominator is  $(M-1)$  due to the constraint that  $\sum_j (y_{ij} - \hat{y}_{ij}) = 0$  for each exon  $i$ .

Averaging over all  $N$  exons we have:

$$s^2 = \frac{1}{N} \sum_i s_i^2 \tag{3}$$

The SERE estimate is  $s = \sqrt{(s^2)}$ .

# SERE coefficient: example

---

	<b>T0-1</b>	<b>T0-2</b>	<b>T0-3</b>	<b>T4-1</b>	<b>T4-2</b>	<b>T4-3</b>	<b>T8-1</b>	<b>T8-2</b>	<b>T8-3</b>
<b>T0-1</b>	<b>0</b>	<b>2.97</b>	<b>3.88</b>	73.89	71.83	74.02	74.69	76.90	74.03
<b>T0-2</b>	<b>2.97</b>	<b>0</b>	<b>3.00</b>	72.21	70.03	72.33	72.94	75.15	72.32
<b>T0-3</b>	<b>3.88</b>	<b>3.00</b>	<b>0</b>	76.34	74.28	76.33	77.18	79.38	76.51
<b>T4-1</b>	73.89	72.21	76.34	<b>0</b>	<b>5.83</b>	<b>10.42</b>	17.27	14.93	17.99
<b>T4-2</b>	71.83	70.03	74.28	<b>5.83</b>	<b>0</b>	<b>10.89</b>	17.77	15.07	18.10
<b>T4-3</b>	74.02	72.33	76.33	<b>10.42</b>	<b>10.89</b>	<b>0</b>	19.86	18.25	20.07
<b>T8-1</b>	74.69	72.94	77.18	17.27	17.77	19.86	<b>0</b>	<b>6.72</b>	<b>4.04</b>
<b>T8-2</b>	76.90	75.15	79.38	14.93	15.07	18.25	<b>6.72</b>	<b>0</b>	<b>8.22</b>
<b>T8-3</b>	74.03	72.32	76.51	17.99	18.10	20.07	<b>4.04</b>	<b>8.22</b>	<b>0</b>

**Drawback:** not very easy to interpret with many samples.

# Clustering

---

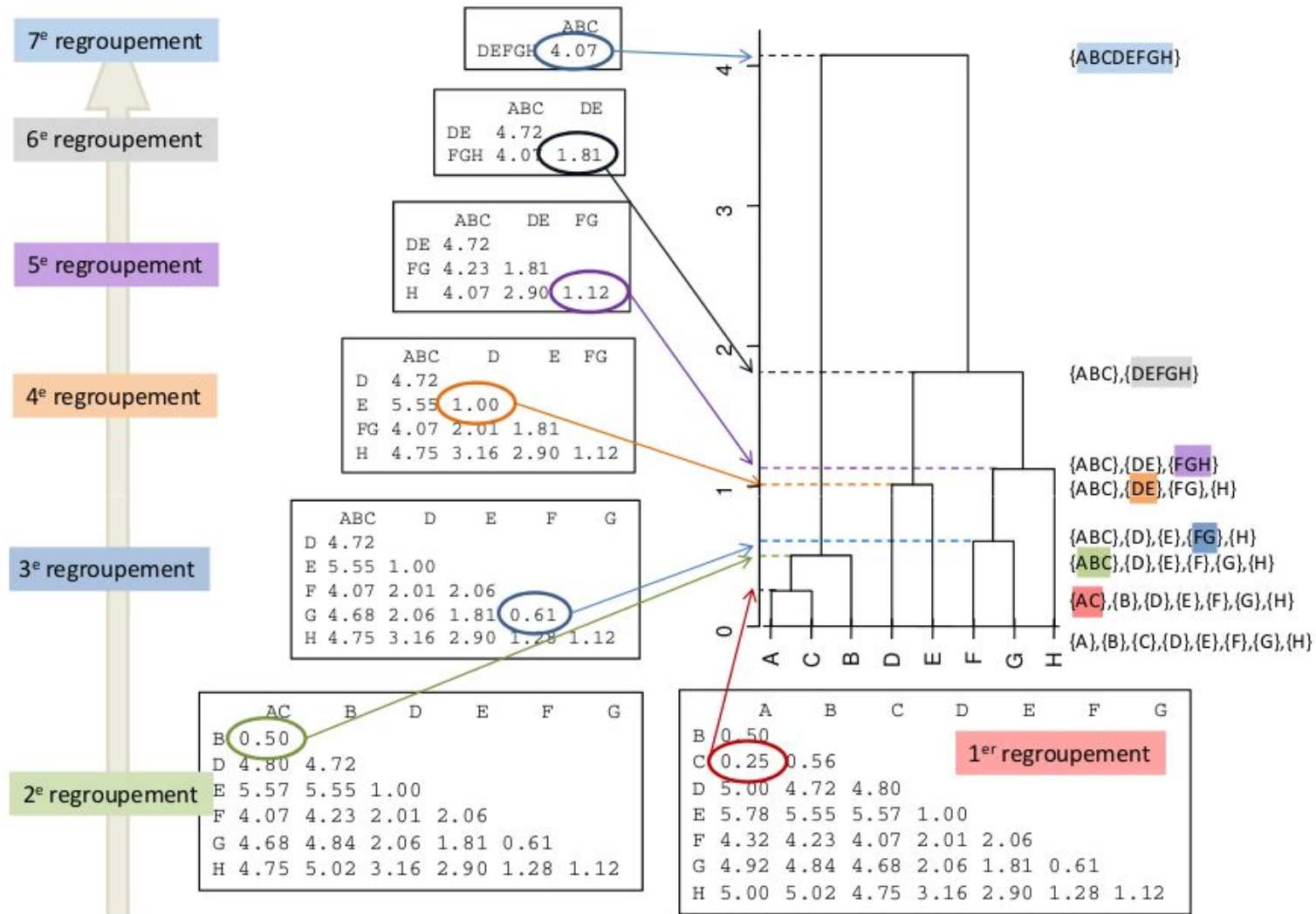
## **Goal: build groups of samples such that:**

- samples within a group are similar
- samples from distinct groups are different

## **Method (ascendant clustering):**

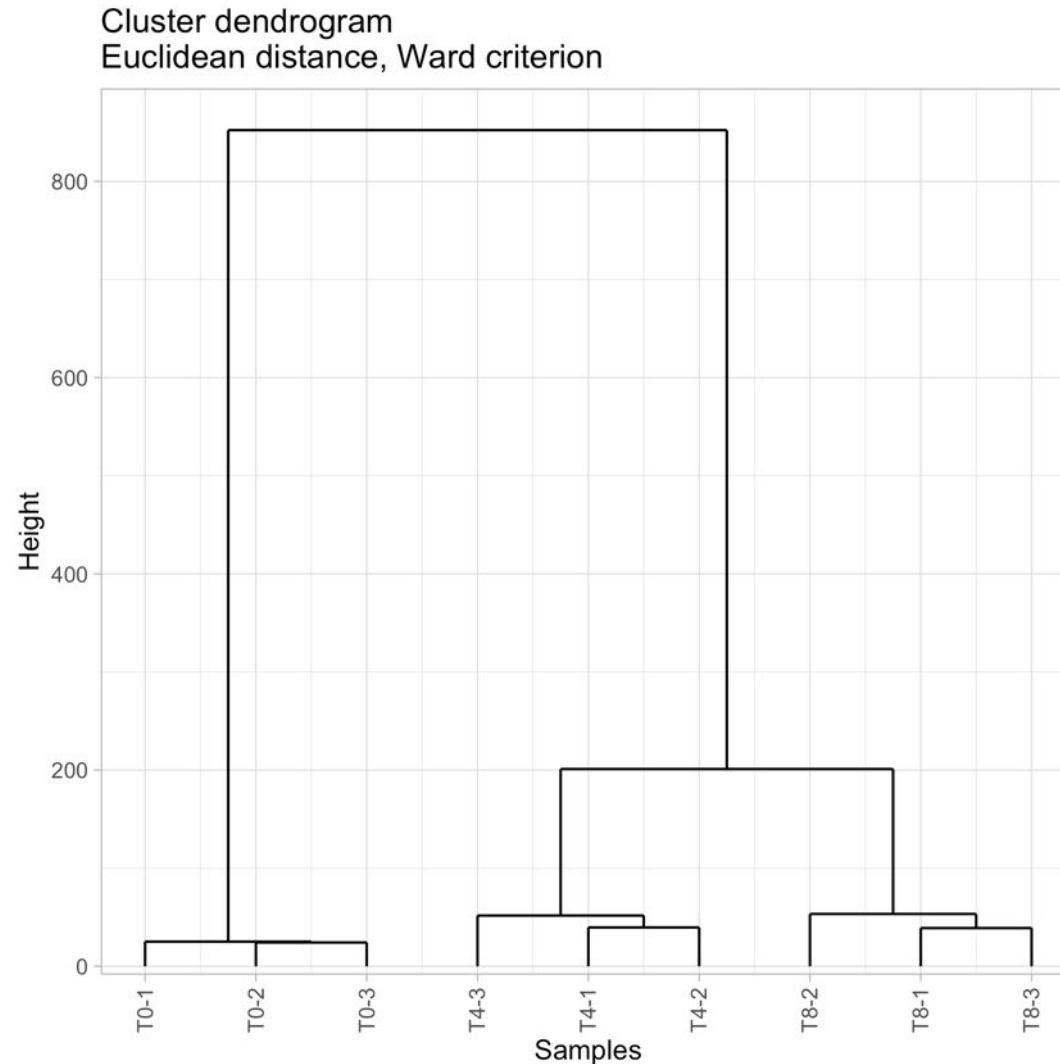
1. Calculate the distances between each pair of samples
2. Gather the two nearest samples into a cluster
3. Calculate the distance between this cluster and each sample
4. Gather the two nearest clusters/samples
5. Go back to step 3 until getting a single cluster

# Hierarchical clustering: example



Source: MOOC FUN Analyse de données 2015 – Agrocampus Ouest

# Hierarchical clustering: RNA-Seq example



**Pre-requisite:** counts must be transformed (made homoscedastic) before building the PCA.

# Clustering parameters

---

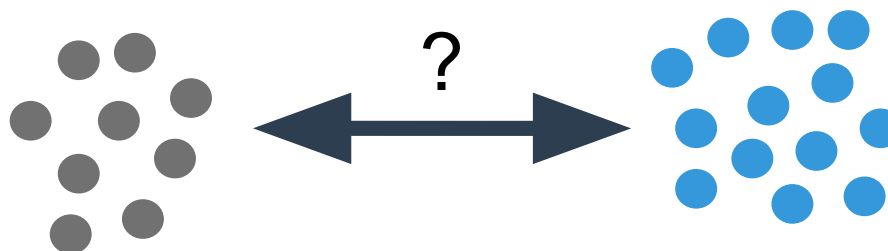


**Distance between two samples:** euclidean, correlation, Manhattan, SERE

...

**Aggregation criterion (i.e. distance between two clusters):**

- Average linkage: **average distance** between all the samples
- Single linkage: distance between the two **closest** samples
- Complete linkage: distance between the two **furthest** samples
- Ward: merge the clusters that lead to the cluster with **minimum variance**

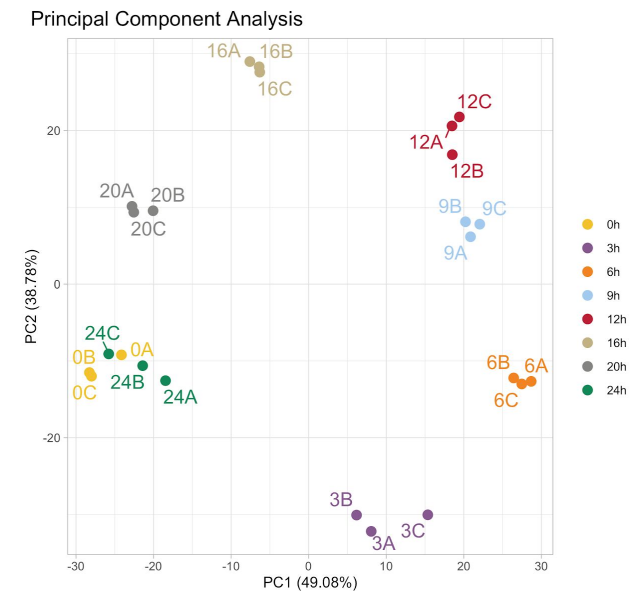




# Data exploration : Take-home message

## Always visualize your data first !

- To detect early on potential problems in the design
- To guide you through the next steps of the analysis
- To provide some biological interpretation
- To communicate your results



**Don't overlook potential breach of hypothesis** for the analysis methods, or choices of parameters

# Outline

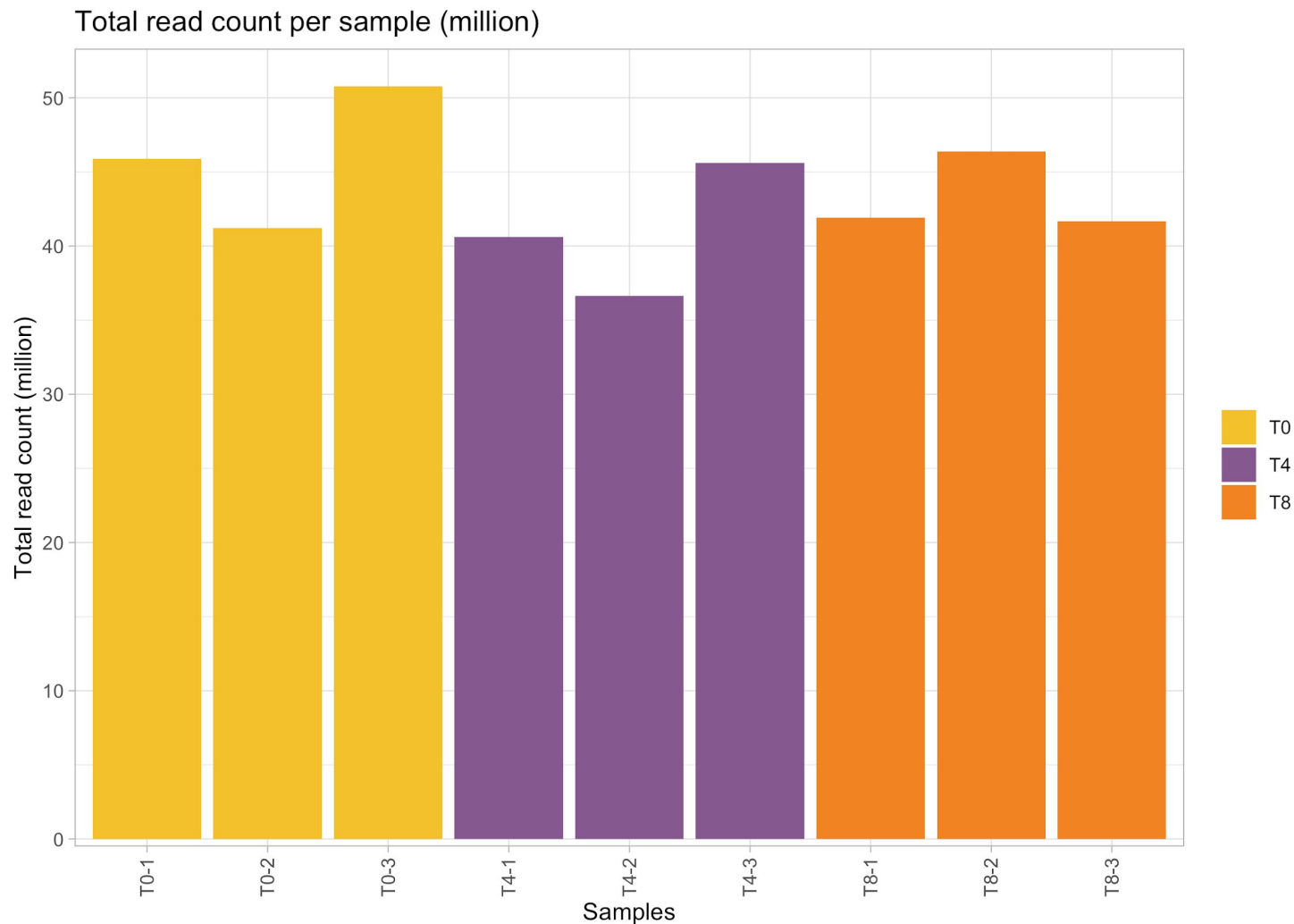
---

1. Introduction
2. Designing the experiment
3. Description/exploration
- 4. Normalization**
5. Modeling
6. SARTools

# Goal

---

Identify and correct for systematic technical bias and make the counts comparable between samples.



# Framework

---

## Normalization framework:

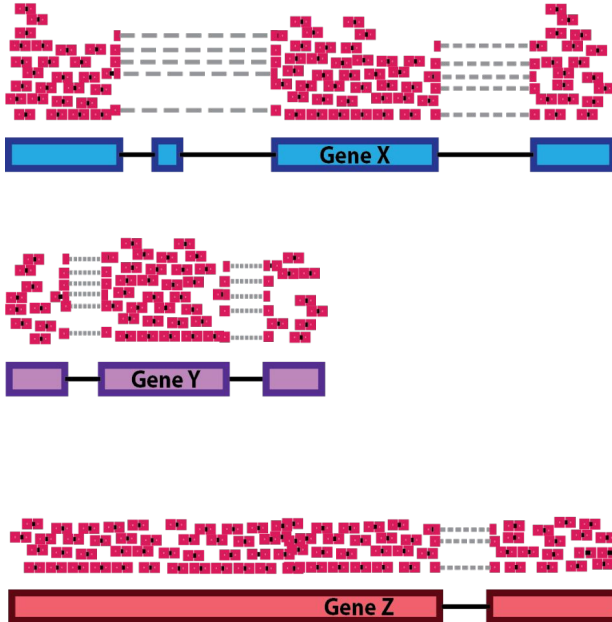
- RNA-seq data
- Differential expression experiment
- Counts data (positive integer values)

**Total number of reads (library size):** number of reads sequenced, mapped and counted for a given sample (sum over the rows for a given column of the count matrix).

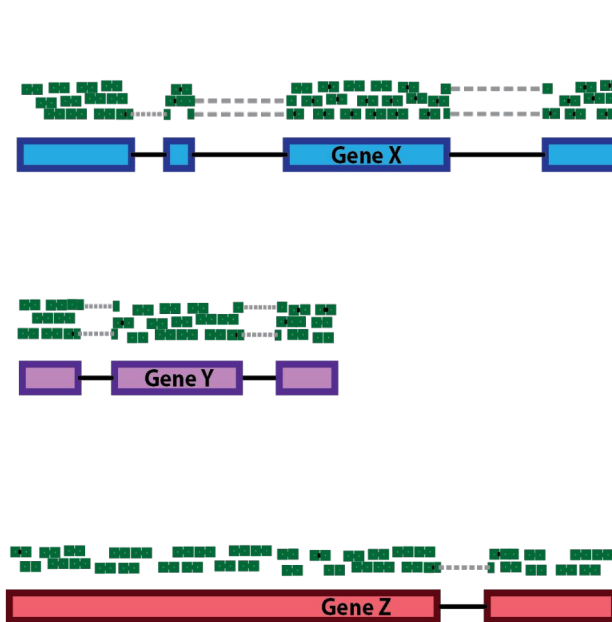
# Goal of the RNA-Seq normalizations

## 1. Correct for the differences of library sizes:

Sample A Reads



Sample B Reads

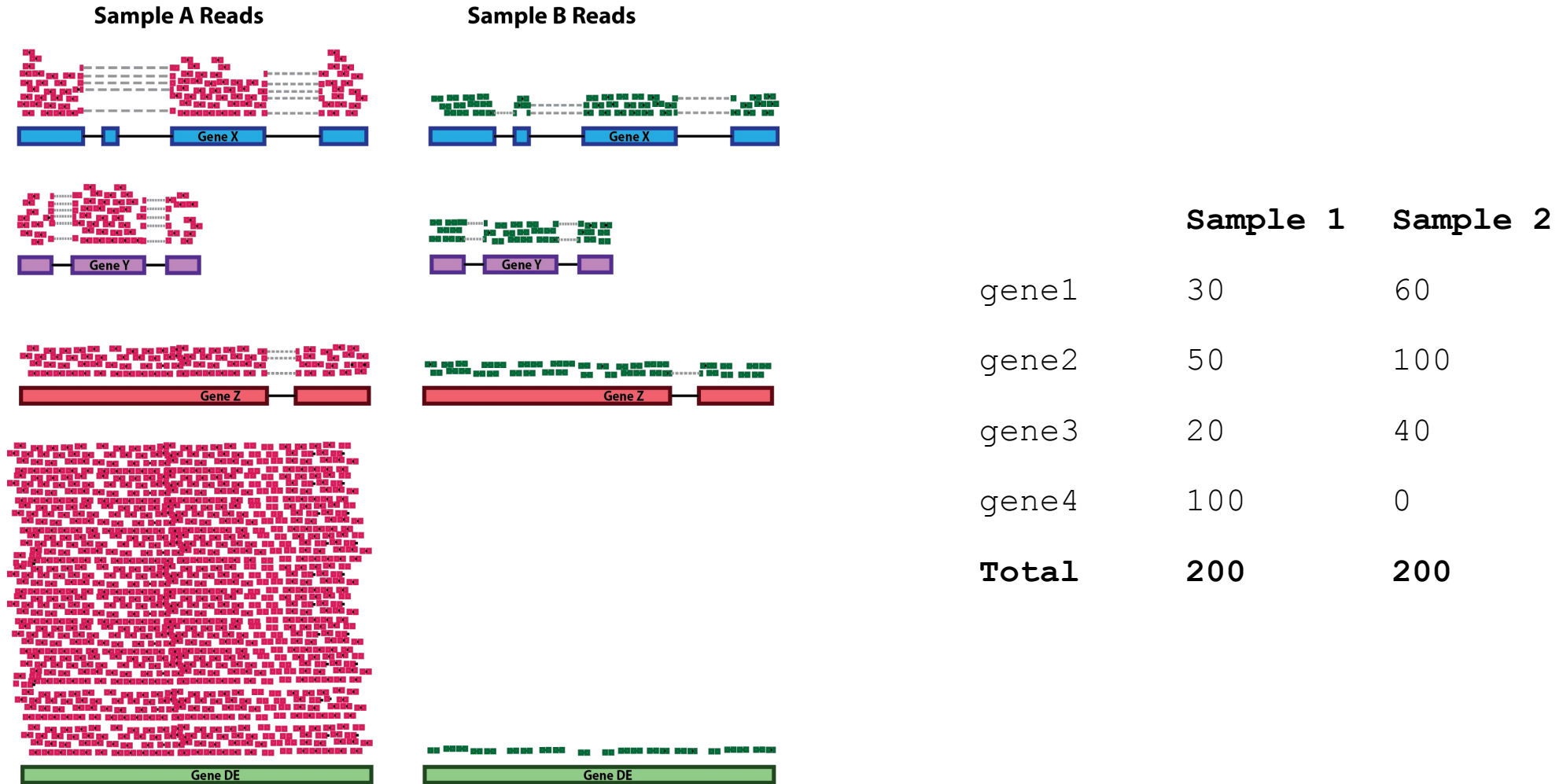


	Sample 1	Sample 2
gene1	30	60
gene2	50	100
gene3	20	40
gene4	100	200
<b>Total</b>	<b>200</b>	<b>400</b>

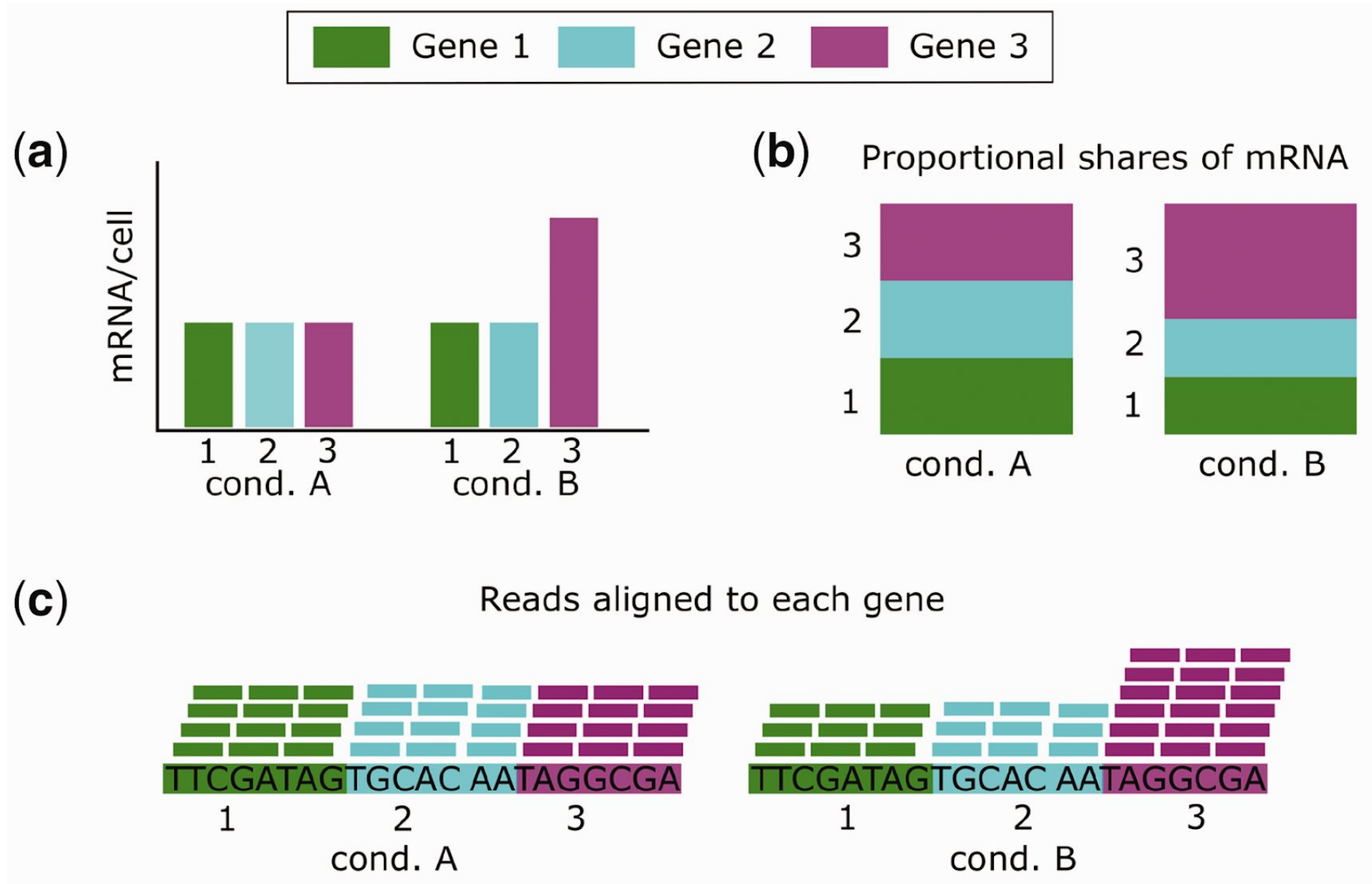
[https://hbctraining.github.io/DGE\\_workshop/lessons/02\\_DGE\\_count\\_normalization.html](https://hbctraining.github.io/DGE_workshop/lessons/02_DGE_count_normalization.html)

# Goal of the RNA-Seq normalizations

## 2. Correct for the differences of RNA compositions:

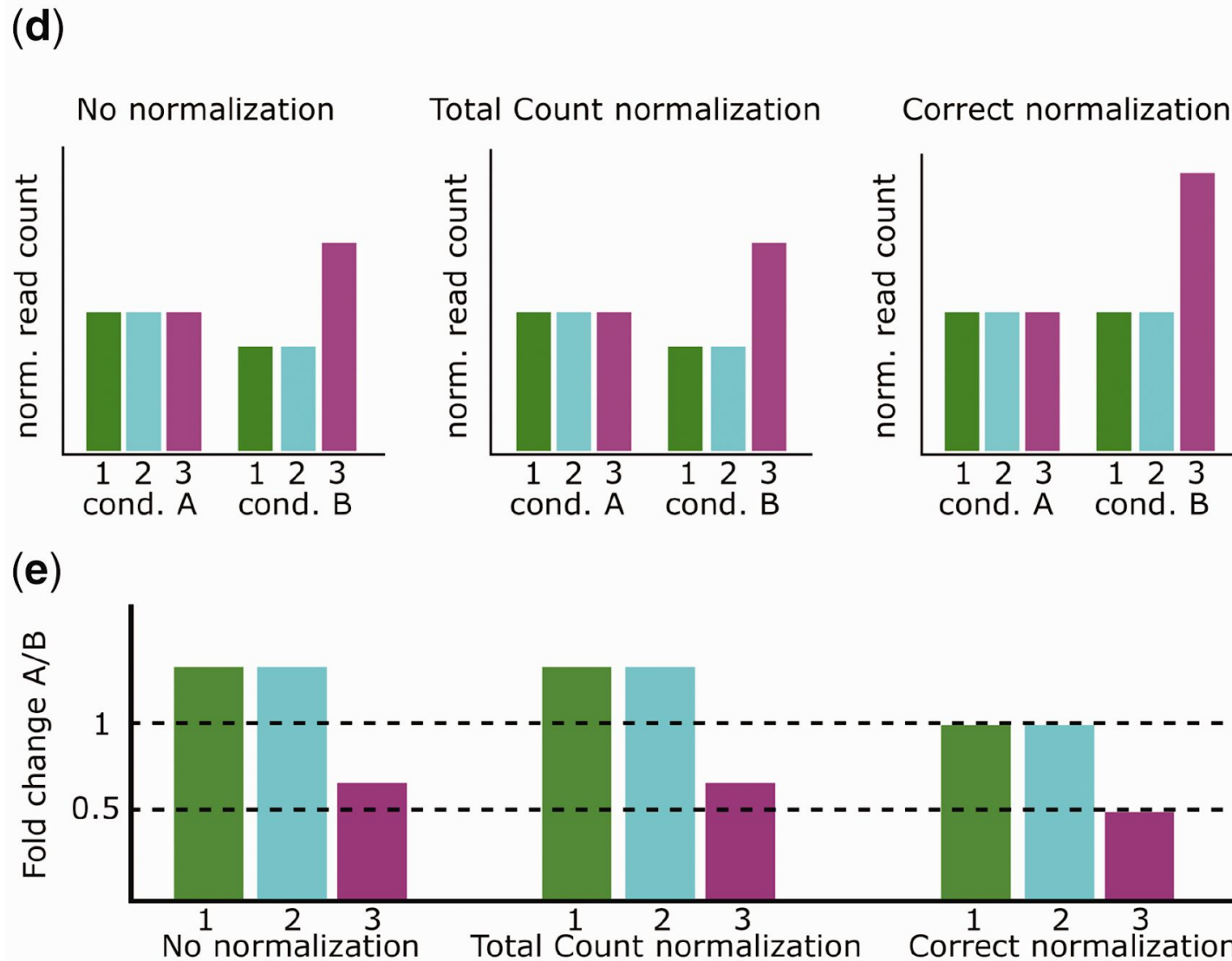


# What is a differentially expressed gene? [10]



C. Evans et al. Selecting between-sample RNA-Seq normalization methods from the perspective of their assumptions. Briefings in Bioinformatics, 2017.

# What is a differentially expressed gene? [10]



C. Evans et al. Selecting between-sample RNA-Seq normalization methods from the perspective of their assumptions. Briefings in Bioinformatics, 2017.



# DESeq2 normalization: computation of $s_i$

---

DESeq2 computes a **size factor** per sample:

**Step 1** : Creating a pseudo-reference sample (row-wise *geometric mean*)

	<b>T0-1</b>	<b>T0-5</b>	...	<b>T8-3</b>
<b>gene1</b>	151	131	...	18
<b>gene2</b>	142	134	...	151
<b>gene3</b>	157	147	...	8
<b>gene4</b>	275	249	...	62
<b>gene5</b>	4	5	...	3
<b>gene6</b>	2	0	...	3
<b>gene7</b>	4	7	...	0
<b>gene8</b>	10	16	...	23
<b>gene9</b>	12	20	...	9
<b>gene10</b>	269	262	...	48
...	...	...	...	...
<b>geneN</b>	18	31	...	2

# DESeq2 normalization: computation of $s_i$

DESeq2 computes a **size factor** per sample:

**Step 1** : Creating a pseudo-reference sample (row-wise *geometric mean*)

	T0-1		T0-5	...	T8-3	pseudo-ref
gene1	( 151	x	131	x	18 )	$1/n$ 31
gene2	142		134	...	151	
gene3	157		147	...	8	
gene4	275		249	...	62	
gene5	4		5	...	3	
gene6	2		0	...	3	
gene7	4		7	...	0	
gene8	10		16	...	23	
gene9	12		20	...	9	
gene10	269		262	...	48	
...	...		...	...	...	
geneN	18		31	...	2	

# DESeq2 normalization: computation of $s_i$

DESeq2 computes a **size factor** per sample:

**Step 1** : Creating a pseudo-reference sample (row-wise *geometric mean*)

	<b>T0-1</b>	<b>T0-5</b>	...	<b>T8-3</b>	<b>pseudo-ref</b>
<b>gene1</b>	151	131	...	18	<b>31</b>
<b>gene2</b>	142	134	...	151	<b>650</b>
<b>gene3</b>	157	147	...	8	<b>7</b>
<b>gene4</b>	275	249	...	62	<b>70</b>
<b>gene5</b>	4	5	...	3	<b>2</b>
<b>gene6</b>	2	0	...	3	<b>1</b>
<b>gene7</b>	4	7	...	0	<b>5</b>
<b>gene8</b>	10	16	...	23	<b>28</b>
<b>gene9</b>	12	20	...	9	<b>74</b>
<b>gene10</b>	269	262	...	48	<b>112</b>
...	...	...	...	...	...
<b>geneN</b>	18	31	...	2	<b>4</b>

# DESeq2 normalization: computation of $s_i$

DESeq2 computes a **size factor** per sample:

**Step 2** : Comparing each sample to pseudo-reference (ratio)

	<b>T0-1</b>	<b>T0-5</b>	...	<b>T8-3</b>	<b>pseudo-ref</b>	<b>T0-1 / ref</b>
<b>gene1</b>	151	131	...	18	<b>31</b>	<b>4.87</b>
<b>gene2</b>	142	134	...	151	<b>650</b>	<b>0.22</b>
<b>gene3</b>	157	147	...	8	<b>7</b>	<b>22.43</b>
<b>gene4</b>	275	249	...	62	<b>70</b>	<b>3.93</b>
<b>gene5</b>	4	5	...	3	<b>2</b>	<b>2.00</b>
<b>gene6</b>	2	0	...	3	<b>1</b>	<b>2.00</b>
<b>gene7</b>	4	7	...	0	<b>5</b>	<b>0.80</b>
<b>gene8</b>	10	16	...	23	<b>28</b>	<b>0.36</b>
<b>gene9</b>	12	20	...	9	<b>74</b>	<b>0.16</b>
<b>gene10</b>	269	262	...	48	<b>112</b>	<b>2.40</b>
...	...	...	...	...	...	...
<b>geneN</b>	18	31	...	2	<b>4</b>	<b>4.87</b>

# DESeq2 normalization: computation of $s_1$

DESeq2 computes a **size factor** per sample:

**Step 3** : Final size factor (median)

	T0-1	T0-5	...	T8-3	pseudo-ref	T0-1 / ref	
gene1	151	131	...	18	31	4.87	} $s_1 = \text{median}$
gene2	142	134	...	151	650	0.22	
gene3	157	147	...	8	7	22.43	
gene4	275	249	...	62	70	3.93	
gene5	4	5	...	3	2	2.00	
gene6	2	0	...	3	1	2.00	
gene7	4	7	...	0	5	0.80	
gene8	10	16	...	23	28	0.36	
gene9	12	20	...	9	74	0.16	
gene10	269	262	...	48	112	2.40	
...	...	...	...	...	...	...	
geneN	18	31	...	2	4	4.87	

# DESeq2 normalization: computation of $s_1$

Normalized count :  $x'_{ij} = \frac{x_{ij}}{s_j}$

Step 1 : geometric mean of each gene

Step 2 : ratio between sample and reference

	T0-1	T0-5	...	T8-3	$(\prod_{k=1}^n x_{ik})^{\frac{1}{n}}$	$\frac{x_{ij}}{(\prod_{k=1}^n x_{ik})^{\frac{1}{n}}}$
gene1	151	131	...	18	31	4.87
gene2	142	134	...	151	650	0.22
gene3	157	147	...	8	7	22.43
gene4	275	249	...	62	70	3.93
gene5	4	5	...	3	2	2.00
gene6	2	0	...	3	1	2.00
gene7	4	7	...	0	5	0.80
gene8	10	16	...	23	28	0.36
gene9	12	20	...	9	74	0.16
gene10	269	262	...	48	112	2.40
...	...	...	...	...	...	...
geneN	18	31	...	2	4	4.87

Step 3 : median

$s_1 = \text{median}$

# DESeq2 normalization [3]

---

Size factor  $s_j$  per sample:

$$s_j = \text{median}_i \frac{x_{ij}}{\left(\prod_{k=1}^n x_{ik}\right)^{\frac{1}{n}}}$$

- $x_{ij}$ : number of reads for gene  $i$  in sample  $j$
- $n$ : number of samples studied
- $s_j$ : normalization factor for sample  $j$

Normalized counts:

$$x'_{ij} = \frac{x_{ij}}{s_j}$$

## Assumptions:

1. The majority of the genes is not differentially expressed
2. As many down- as up-regulated genes

# edgeR normalization [4]

---

edgeR computes a normalization factor  $f_j$  per sample and normalizes the total numbers of reads  $N_j$ :

$$N'_j = f_j \times N_j$$

- $x_{ij}$ : number of reads for gene  $i$  in sample  $j$
- $N_j$ : total number of reads in sample  $j$  (lib size)
- $n$ : number of samples studied
- $s_j$  or  $f_j$ : normalization factor for sample  $j$
- $L_i$ : length of gene  $i$

We can calculate DESeq2-like size factors  $s_j$  in order to normalize the counts:

$$s_j = \frac{N'_j}{\frac{1}{n} \sum_k N'_k} \quad \text{and so} \quad x'_{ij} = \frac{x_{ij}}{s_j}$$

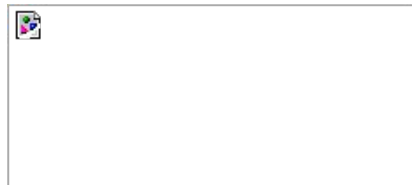
**Assumptions:** same than DESeq2.



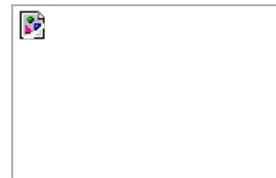
# Other normalization methods

---

**Total number of reads:**



or



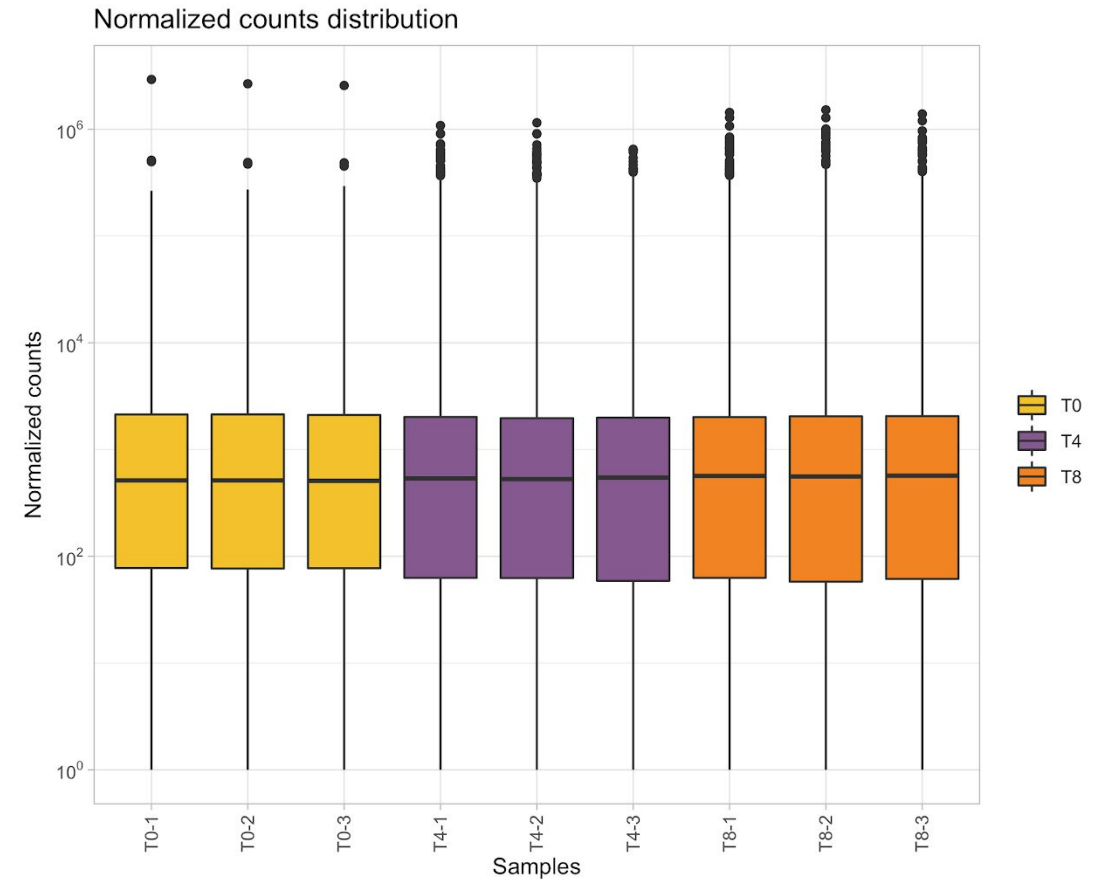
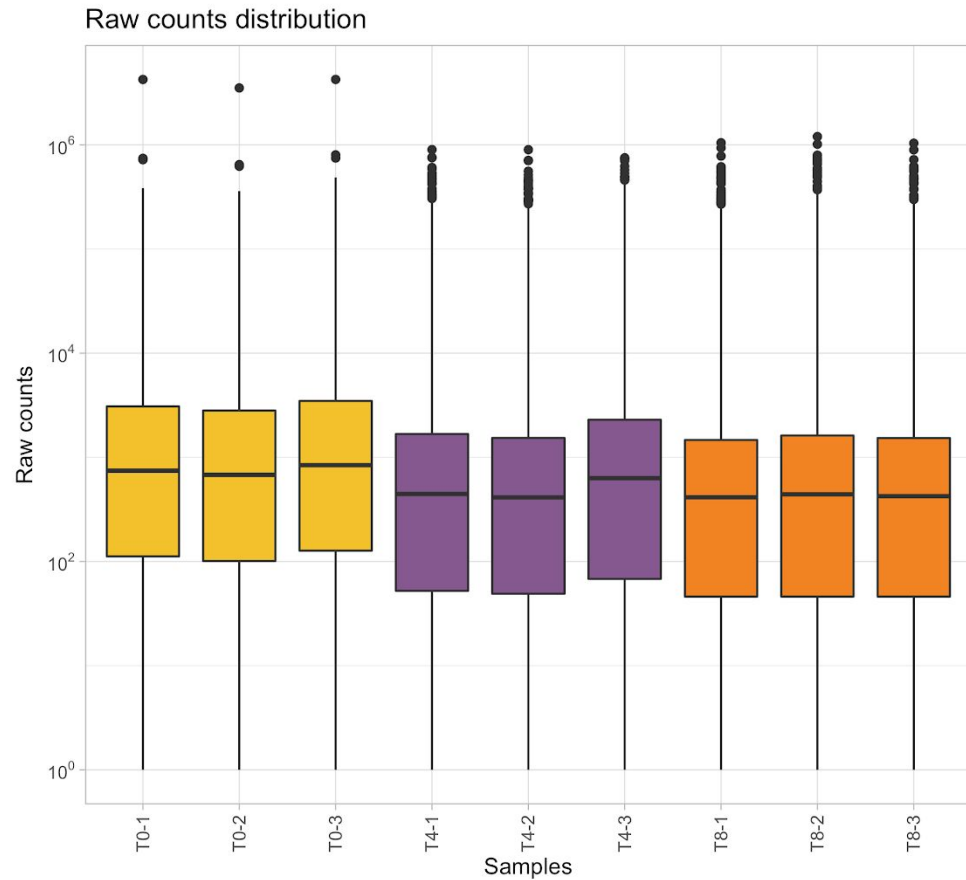
Robustness issue if a gene catches a very high number of reads.

**RPKM (Reads Per Kilobase per Million mapped reads):**

$$x'_{ij} = \frac{x_{ij}}{N_j \times L_i} \times 10^6 \times 10^3$$

- Same issue than the total number of reads method
- Introduce other biases [5]
- No need to correct for the gene length since the gene is "fixed"

# Effect of the normalization (DESeq2 or edgeR)



# Outline

---

1. Introduction
2. Designing the experiment
3. Description/exploration
4. Normalization
- 5. Modeling**
6. SARTools

# Classic linear model

---

## Goal:

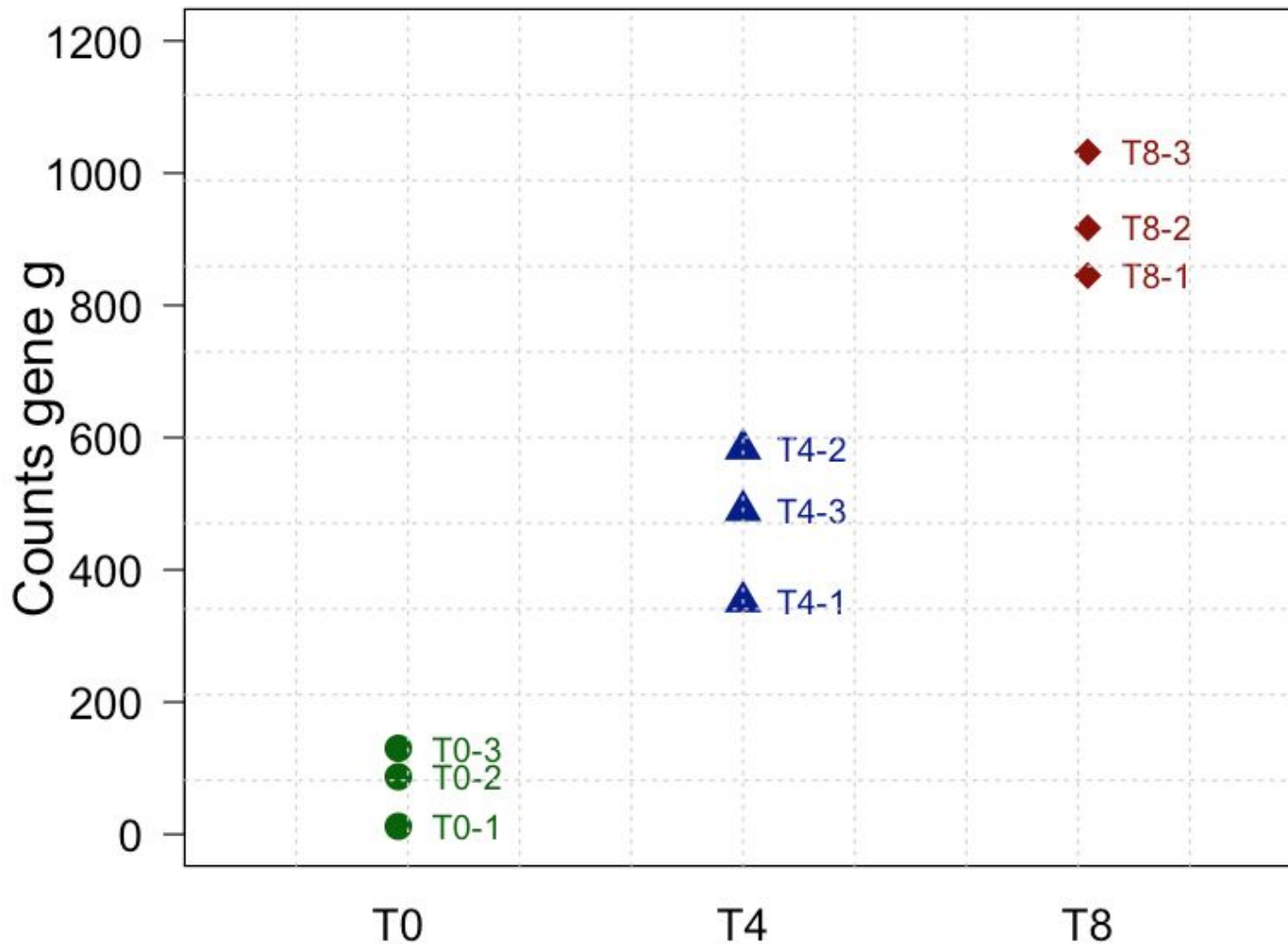
Explain a dependent variable  $Y$  thanks to a set of explicative variables  $X = (X_1, \dots, X_n)$  using the model:

$$Y \sim X\beta + \varepsilon$$

## Output of the model:

Estimations of  $\beta_1, \dots, \beta_n$ : effect of each explicative variable on  $Y$ .

# Linear model: RNA-Seq example



**Goal:** explain counts of gene  $g$  thanks to the biological conditions.

# Linear model: RNA-Seq example

---

**Goal:** explain counts of gene  $g$  thanks to the bio. conditions (T0, T4 and T8).

$$\log_2 \begin{pmatrix} 12 \\ 87 \\ 130 \\ 352 \\ 583 \\ 490 \\ 845 \\ 917 \\ 1032 \end{pmatrix} \sim \begin{pmatrix} 1 & 0 & 0 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 0 \\ 1 & 0 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} \beta_{0g} \\ \beta_{1g} \\ \beta_{2g} \end{pmatrix} + \begin{pmatrix} \epsilon_{g1} \\ \epsilon_{g2} \\ \epsilon_{g3} \\ \epsilon_{g4} \\ \epsilon_{g5} \\ \epsilon_{g6} \\ \epsilon_{g7} \\ \epsilon_{g8} \\ \epsilon_{g9} \end{pmatrix}$$

Here:  $\hat{\beta}_{0g} = 5.95$ ,  $\hat{\beta}_{1g} = 2.91$  and  $\hat{\beta}_{2g} = 3.57$

One model per gene  $\rightarrow$  thousands of models!

# Statistical testing

---

	Green1	Green2	Green3	Gray1	Gray2	Gray3
Gene <i>g</i>	151	131	183	135	184	122

## Biological question:

Is gene *g* differentially expressed between **green** and **gray** mice?

# Statistical testing

---

	Green1	Green2	Green3	Gray1	Gray2	Gray3
Gene <i>g</i>	151	131	183	135	184	122

## Biological question:

Is gene *g* differentially expressed between **green** and **gray** mice?

## Statistical notation

Let  $\mu_1$  the average expression of gene *g* for **gray** mice and  $\mu_2$  the expression of **green** mice. We wish to test the hypotheses:

$$H_0: \mu_1 = \mu_2 \quad \text{vs.} \quad H_1: \mu_1 \neq \mu_2$$

**How to decide ?**



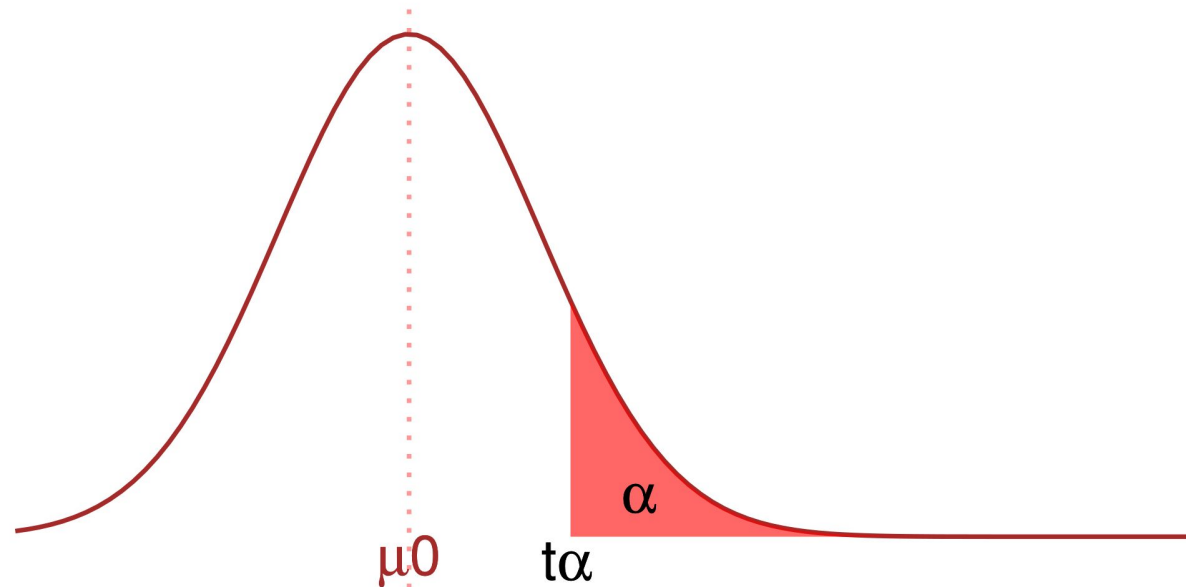
# Type I error rate: $\alpha$

---

## Framework and goal:

We wish to show that the expression of gene  $g$  of gray mice is different from the expression of green mice.

Which **risk  $\alpha$**  of being wrong do we allow when saying :  
“**gene  $g$  is differentially expressed?**”



The risk  $\alpha$  is chosen **before the analysis**

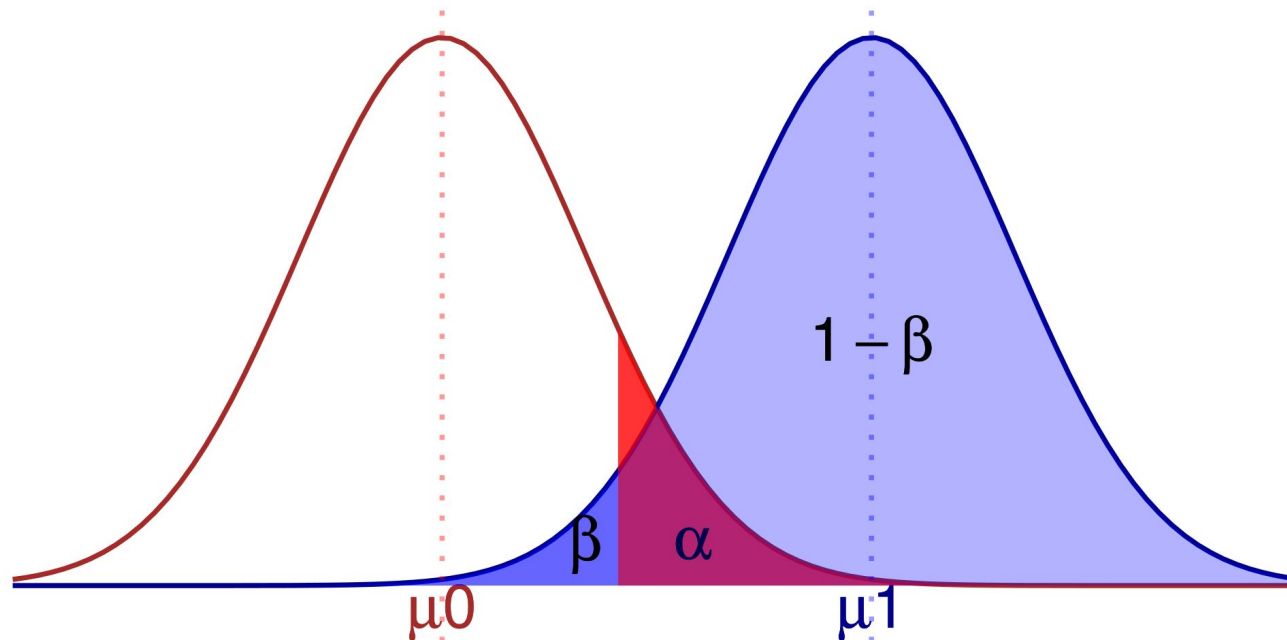
# Type II error rate: $\beta$

---

We assume that gene  $g$  is truly differentially expressed between gray and green mice.

- Which risk  $\beta$  of not discovering gene  $g$  do we allow?
- Which power  $1 - \beta$  do we want?

We can theoretically control the risk  $\beta$  according to the risk  $\alpha$  and the number of replicates.



# Type I and type II errors

## Hotdog classification

Type I error

True negative



False positive



False negative



True positive



Type II error

# Formalization

---

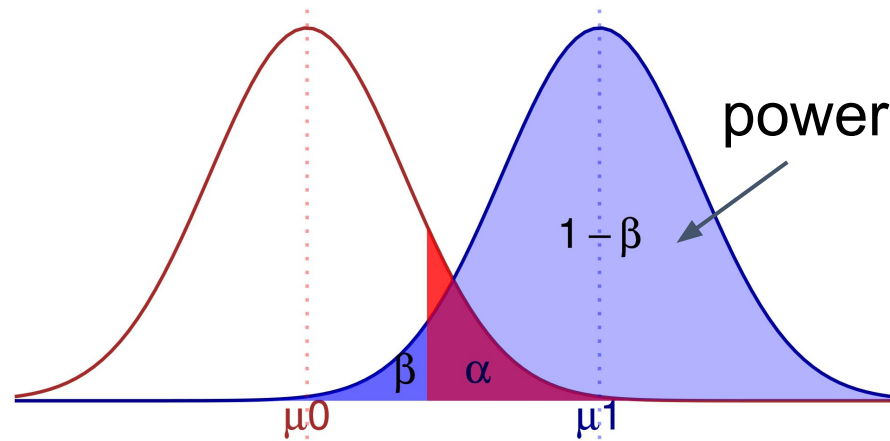
Let  $\mu_1$  the average expression of gene  $g$  for gray mice and  $\mu_2$  the expression of green mice. We wish to test the hypotheses:

$$H_0: \mu_1 = \mu_2 \quad \text{vs.} \quad H_1: \mu_1 \neq \mu_2$$

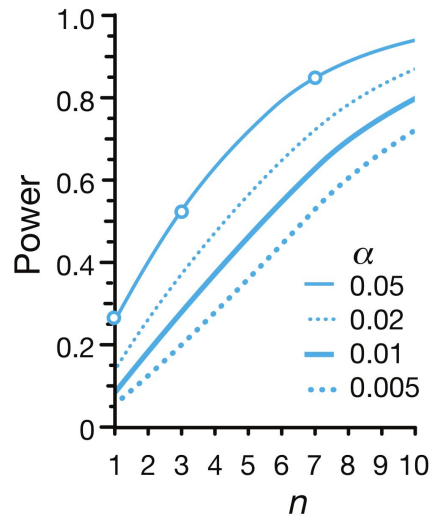
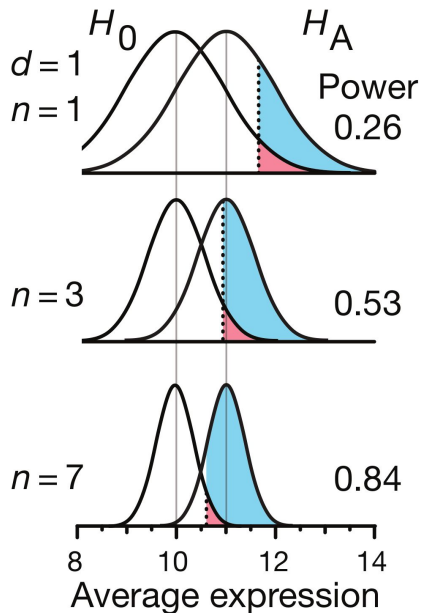
The risks can be summarized in:

		Decision	
		Do not reject $H_0$	Reject $H_0$
Unknown truth	$H_0$ true	$1 - \alpha$ TP	$\alpha$ FN
	$H_0$ false	$\beta$ FP	$1 - \beta$ TN

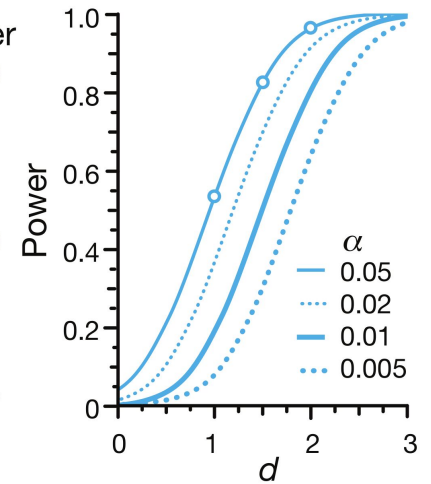
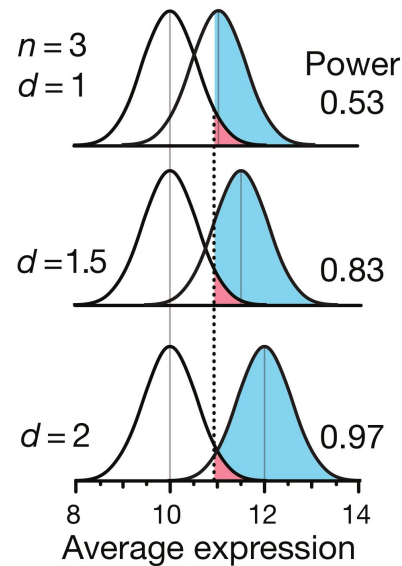
# Statistical Power



power increases with sample size



and with effect size !



$$d = (\mu_1 - \mu_0) / (\sigma)$$

# *p*-value and conclusion of the test

---

## Definition:

*p*-value = Proba(reject  $H_0$  |  $H_0$  true)  
= Proba(doing a mistake when rejecting  $H_0$ )  
= Proba(observed difference is due to hazard)

## Conclusion:

if *p*-value  $\leq \alpha$  then we reject  $H_0$

With a risk  $\alpha$ , we can conclude that there is a significant difference in gene *g* expression between **green** and **gray** mice

# Equal Fold-Changes – different $p$ -values

---

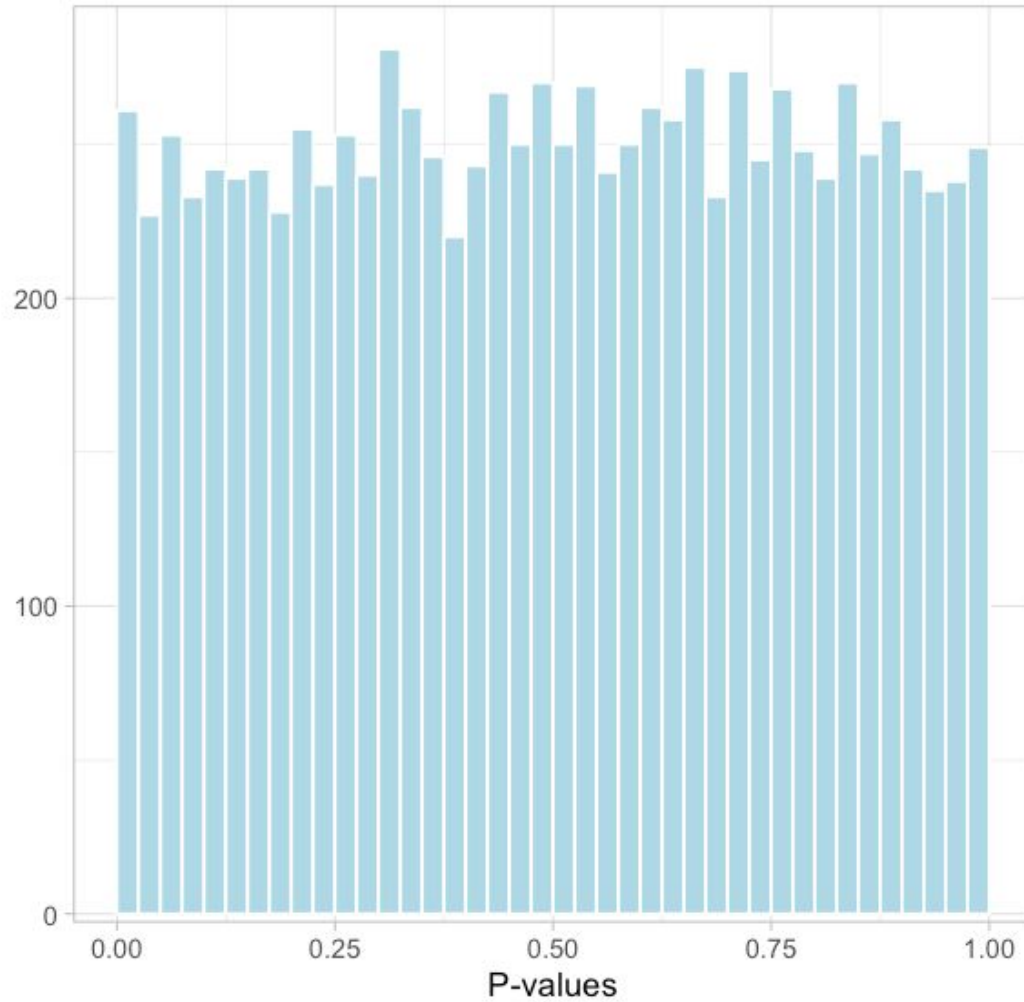
**Reminder:** Fold-Change definition:

$$\text{FC} = \frac{\text{expression condition "green"}}{\text{expression condition "gray"}} = \frac{\mu_2}{\mu_1}$$

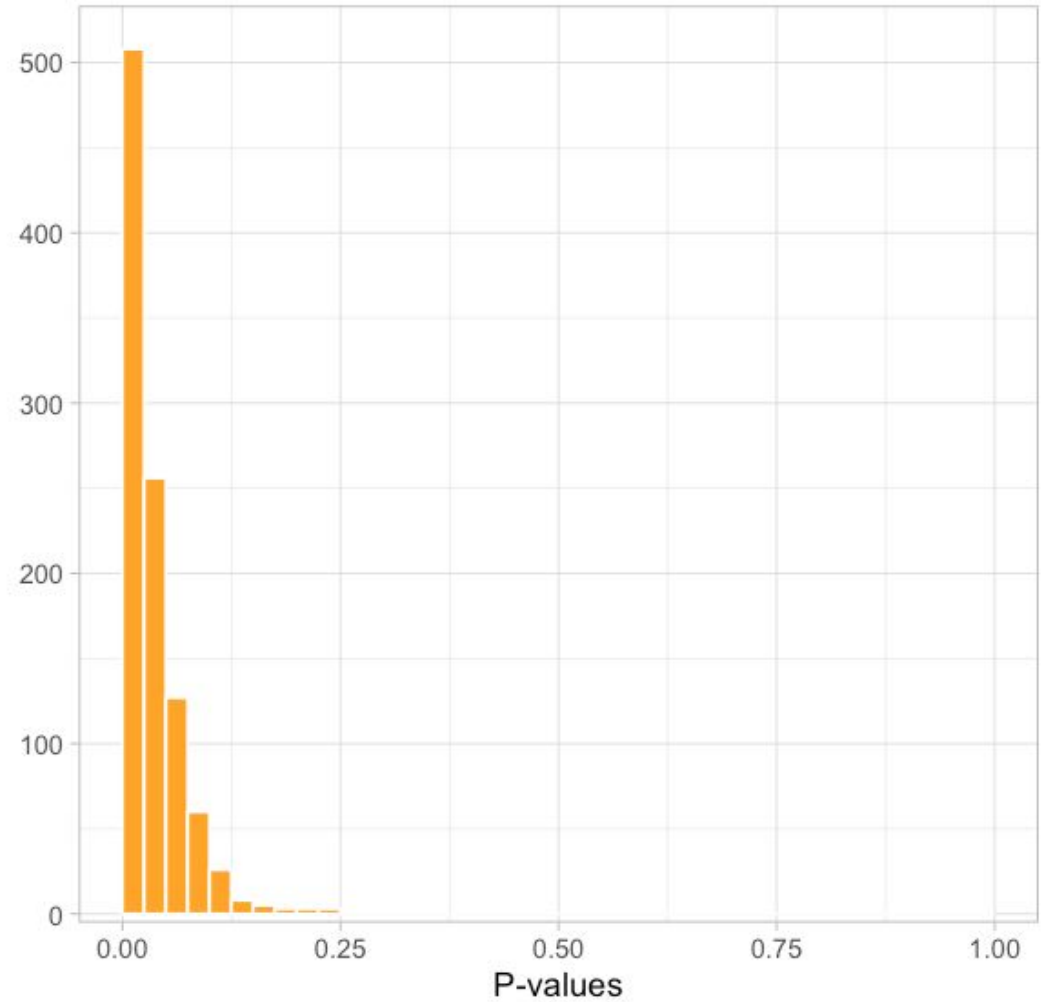
<b>Gene</b>	<b>m1</b>	<b>m2</b>	<b>m3</b>	<b>m4</b>	<b>m5</b>	<b>m6</b>	<b>FC</b>	<b><math>p</math>-value</b>
gene1	5	7	6	2	2	2	3	0.06
gene2	800	1000	900	350	250	200	3	0.03
gene3	700	900	1100	350	200	250	3	0.10
gene4	900	500	1300	200	550	50	3	0.06
...	...	...	...	...	...	...	...	...

# Distribution of raw $p$ -values

Distribution of raw  $p$ -values under  $H_0$

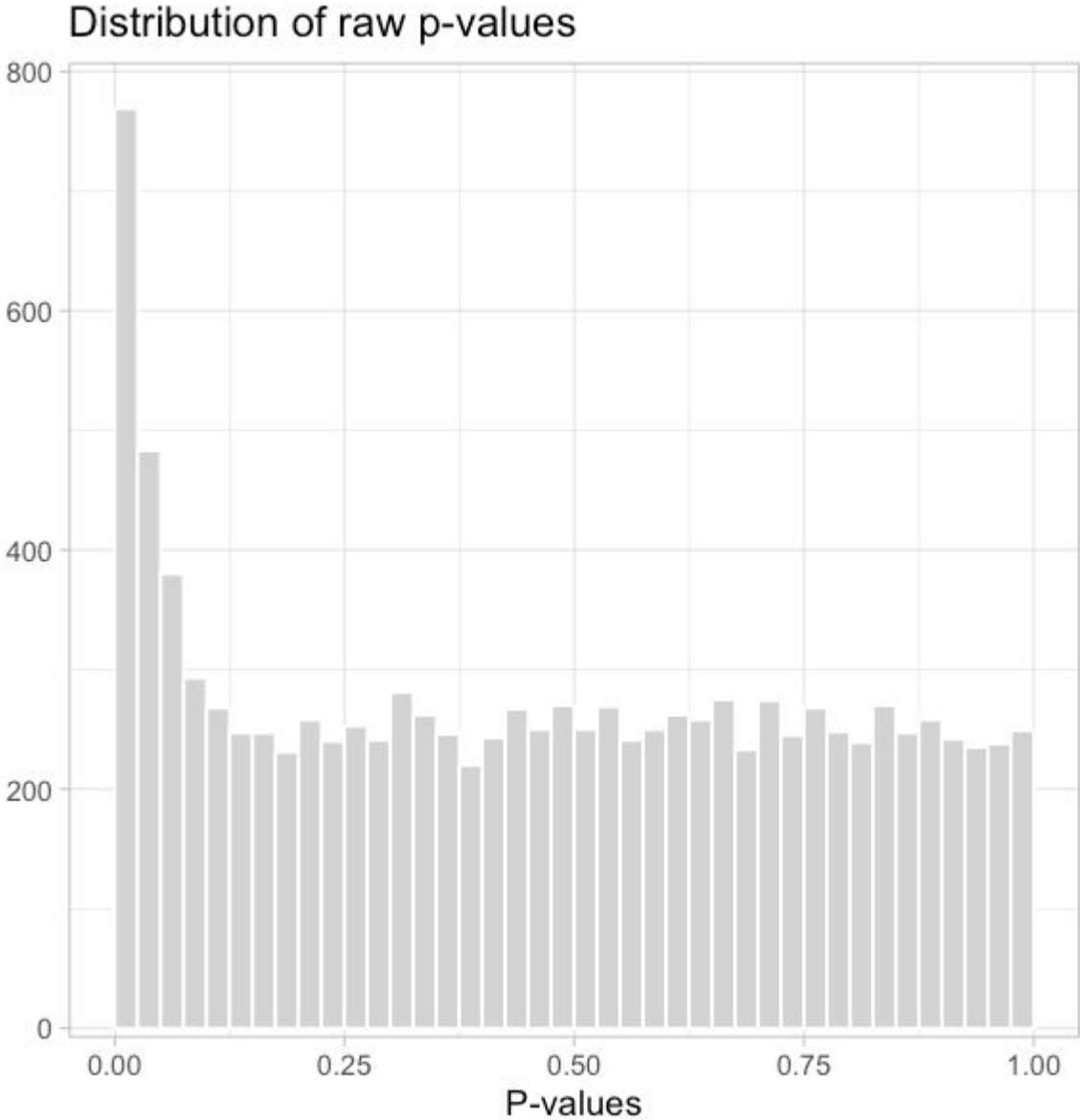


Distribution of raw  $p$ -values under  $H_1$





# Distribution of raw $p$ -values



# Omics data: multiple testing issue

---

## Context:

We perform a large number  $N$  of statistical tests for which we reject or not  $H_0$ .

## Possible conclusions:

		Decisions	
		Non rejects of $H_0$	Rejects of $H_0$
Unknown truths	$H_0$ true	TN	FP
	$H_0$ false	FN	TP

Among all the genes told differentially expressed, the False Discovery Rate (FDR) is:

$$\frac{FP}{FP + TP}$$

# Example of the multiple testing issue

---

We perform  $N = 10000$  statistical tests and we get the following conclusions:

	Non rejects of $H_0$	Rejects of $H_0$	Total
$H_0$ true	8550	450	9000
$H_0$ false	200	800	1000
Total	8750	1250	10000

$$\frac{\text{FP}}{\text{FP} + \text{TP}} = \frac{450}{450 + 800} = 36\% \text{ of falsely discovered genes!}$$

# Control of the FDR

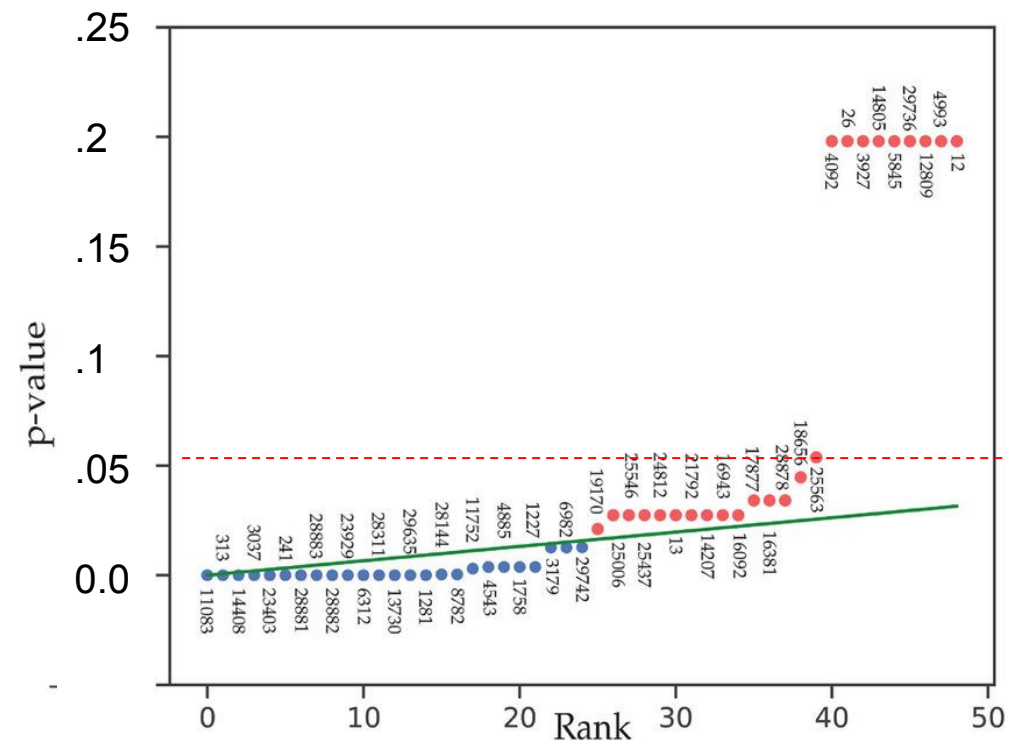
**Goal:** control the FDR among the list of differentially expressed genes.

**(Very strong) assumption:** all the  $N$  statistical tests are independent.

**Procedure:** The Benjamini & Hochberg [6] algorithm transforms the  $N$  raw  $p$ -values in  $N$  adjusted  $p$ -values.

**Conclusion:**

if adjusted  $p$ -value  $\leq \alpha$  then we reject  $H_0$



# Importance of the # of biological replicates

---

**RNA-Seq specificity:** often 2 or 3 replicates because of the high cost of the experiment ... But it's not ideal !

## With more biological replicates...

- Better estimation of:
  - the variability present in the populations studied
  - the difference between the biological conditions
- Better control of the FDR: bad control with only 2 replicates [7]
- Higher statistical power: we detect more easily genes which are truly differentially expressed

**At the very least : 3 replicates !**

# DESeq2 [3] and edgeR [4,8]

---

## Three main steps:

1. Normalization
2. Dispersion (i.e. variability) estimation: crucial step
3. Statistical tests and adjustment for multiple testing

## Advantages:

- User friendly and very well documented
- Good performances
- Authors are reactive on web forums and mailing lists

## Similarities:

- Negative Binomial distribution
- Generalized Linear Model (GLM)

## Differences:

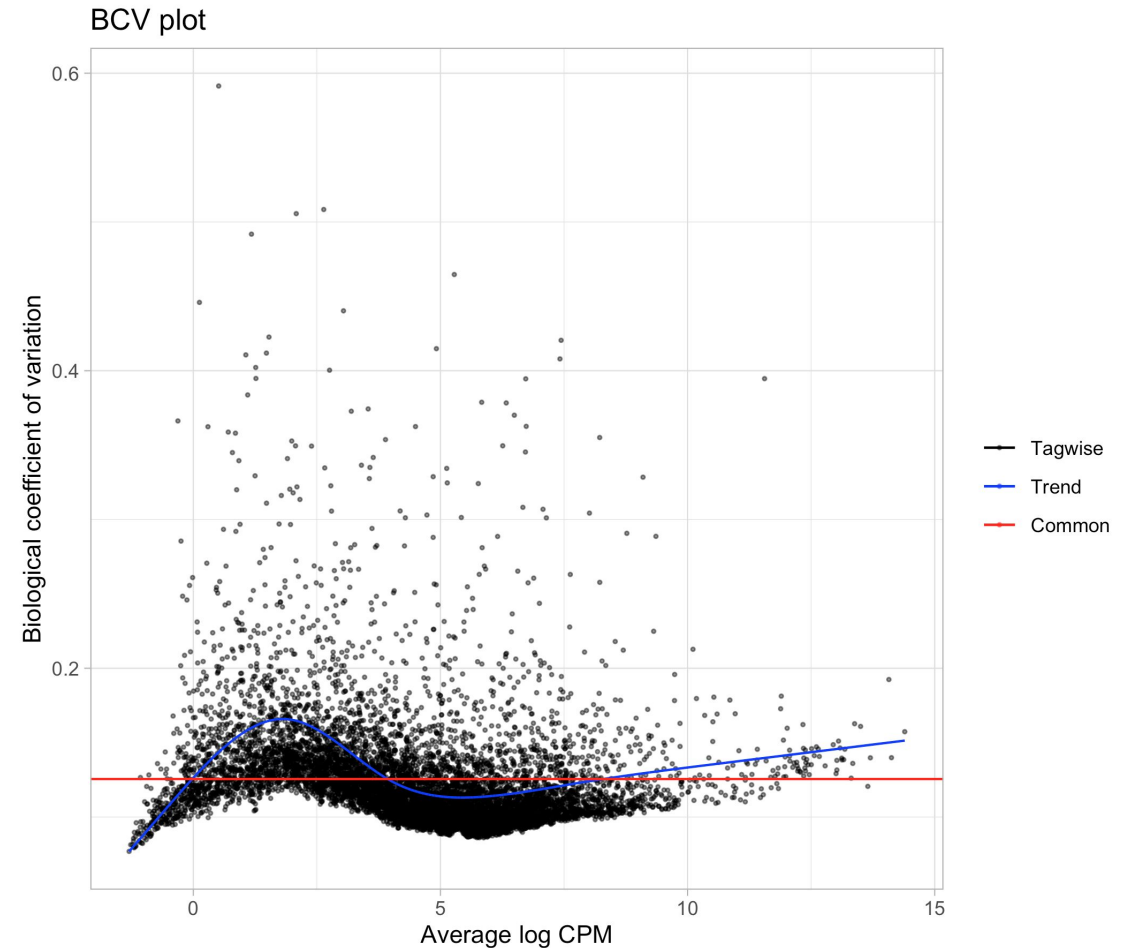
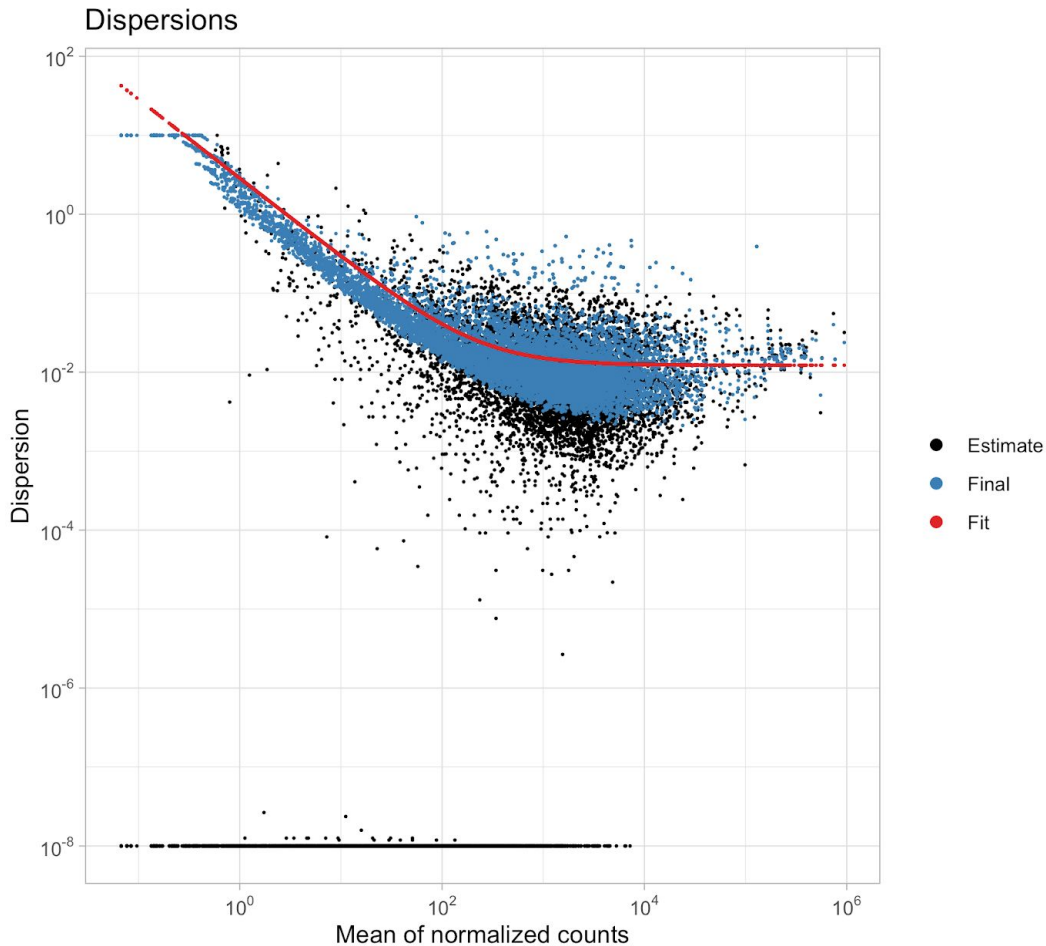
- Dispersion estimation
- Way of dealing with outlier counts
- Low counts filtering

Many other tools exist: NBPSeg, TSPM, baySeq, EBSeq, NOISeq, SAMseq, ShrinkSeq, voom(+limma)

# Dispersion estimation $\phi_i$ : DESeq2 vs edgeR

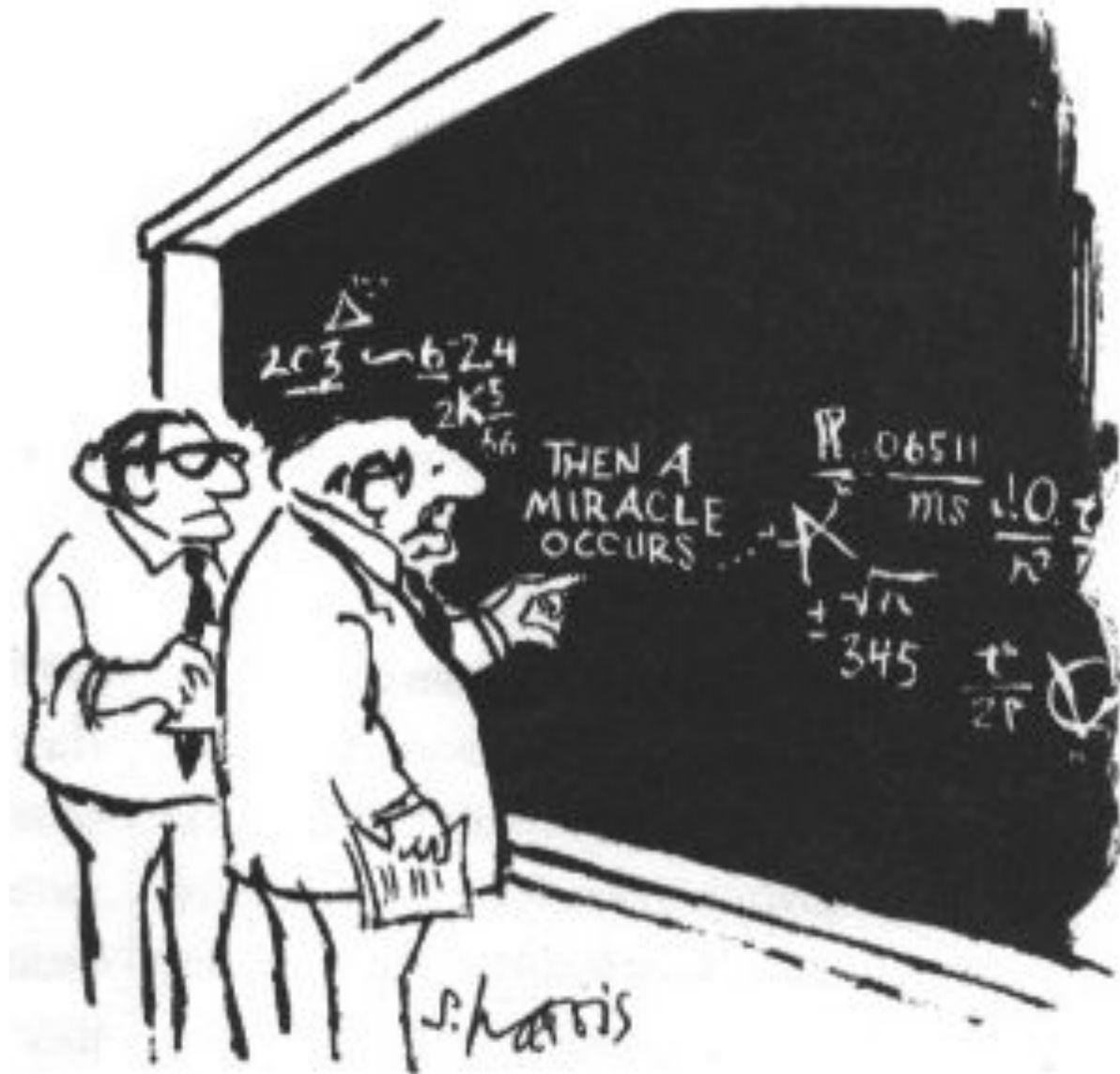
## Reminder:

$$x_{ij} \sim \text{NB}(\mu_{ij}, \sigma_{ij}^2 = \mu_{ij} + \phi_i \mu_{ij}^2)$$



# Statistical theory and parameters tuning

---



"I think you should be more explicit here in step two."



# Statistical testing

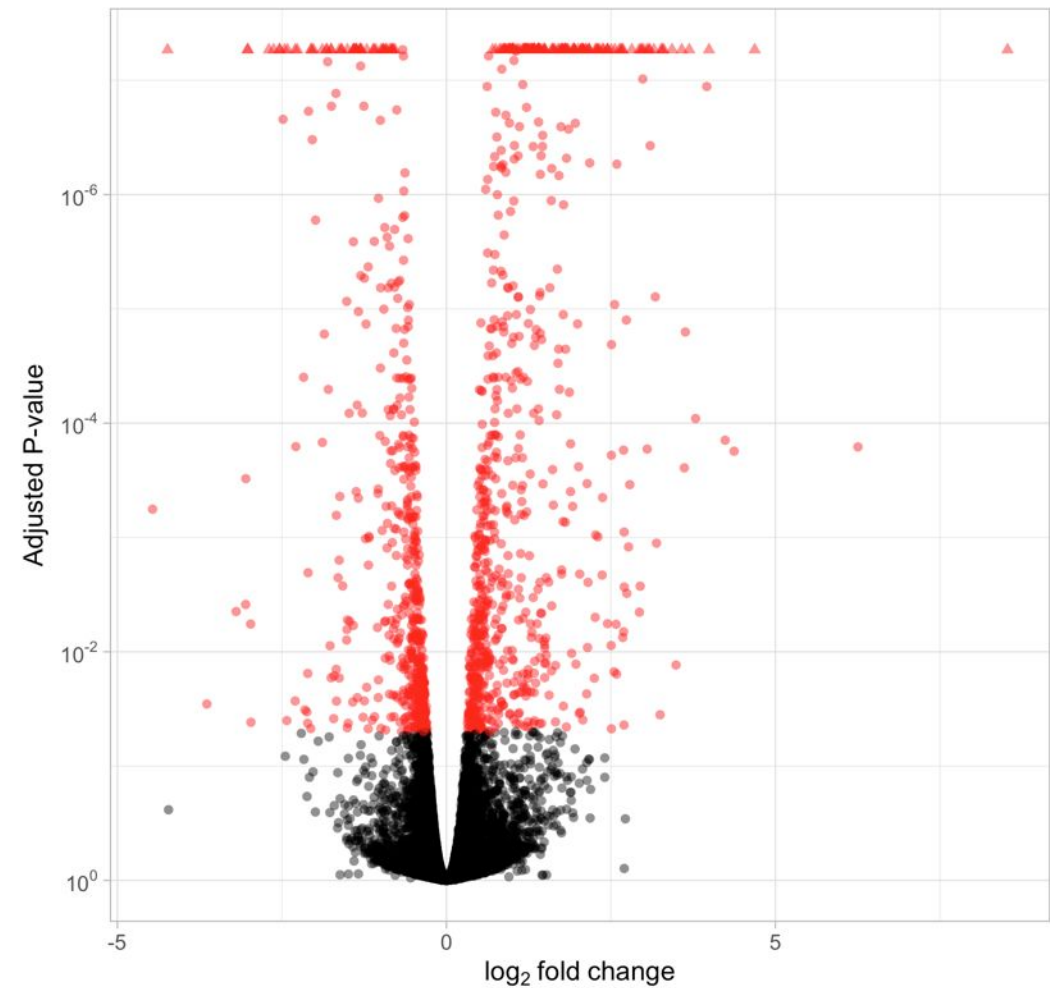
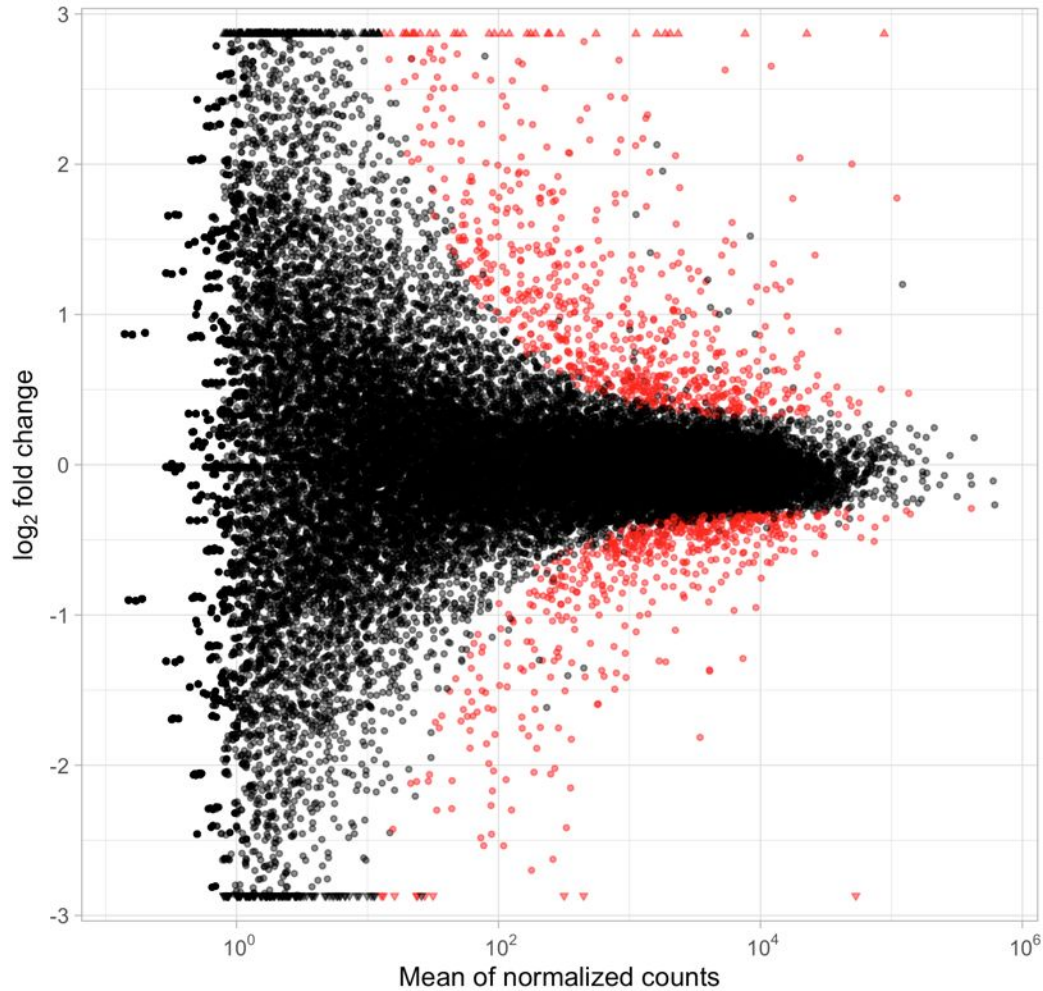
---

**For each gene  $g$ , DESeq2 and edgeR give:**

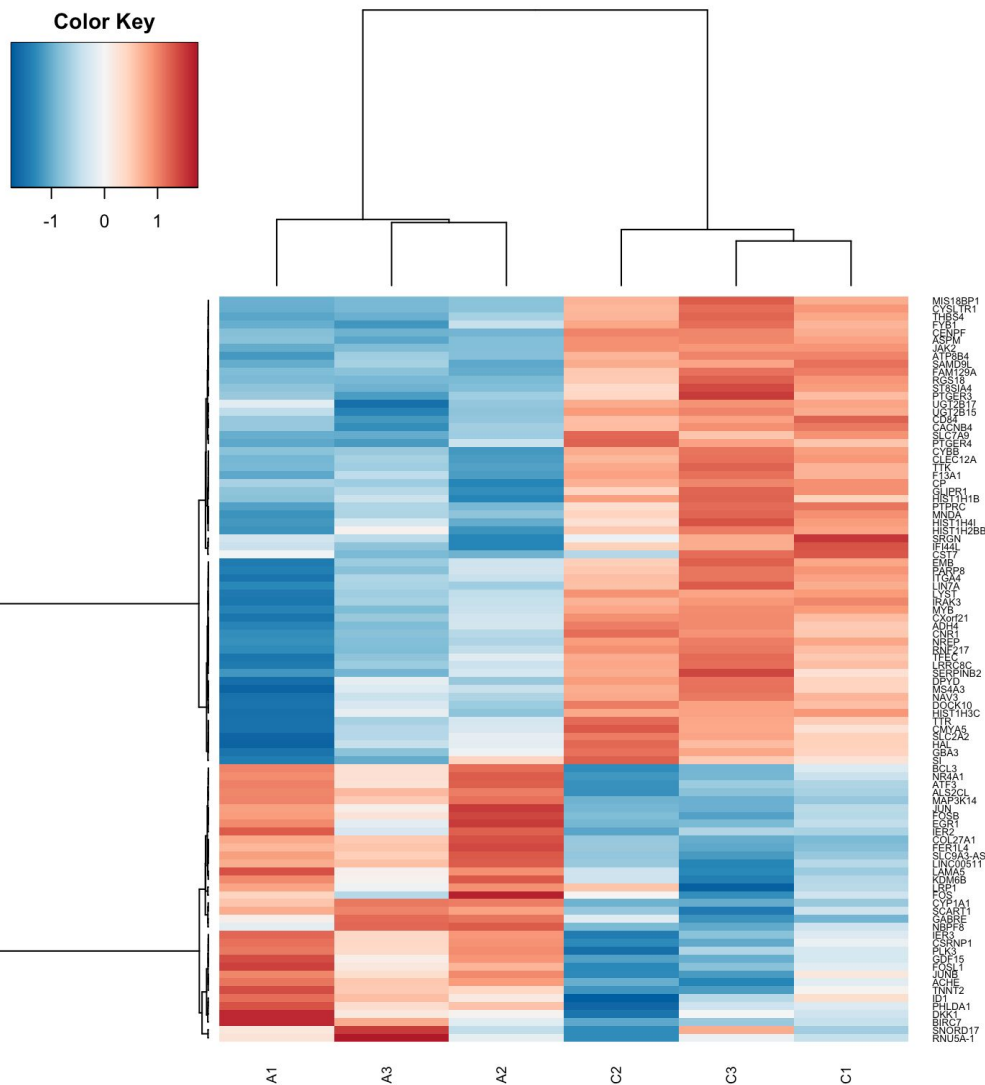
- an estimation of  $\beta_g = \log_2(\text{FC}_g)$
- the precision of this estimation (standard error)
- so the  $p$ -value associated with gene  $g$

The set of the  $N$   $p$ -values is adjusted in order to conclude.

# Description of the results: MA-plot and volcano-plot



# Description of the results: heatmap



## Much more complex than it appears:

- Use expression data or  $\log_2(\text{FC})$ ?
- Which genes to display?
- Expression data transformation:
  - Homoscedasticity?
  - Row centering and scaling?
- Row/column clustering method?
- Average data by condition?
- Batch/replicate effect removal?

# Data normalization & modelling : Take-home message

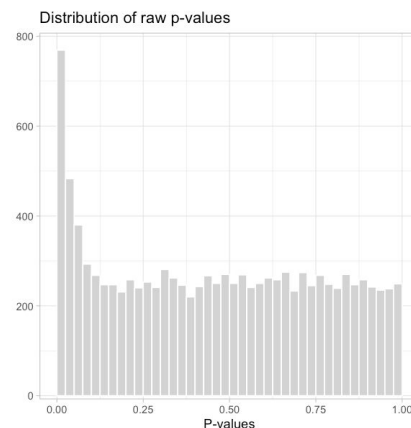
---

**Data normalization** is crucial to make sure you are really testing your biological question by removing systematic bias. Specific RNASeq methods must take into account library size & composition.

**Multiple testing** must be corrected using FDR as many tests are done simultaneously

**Replicate your measures** according to the expected variability in the data and the differences you want to highlight

**Visualize your results** and use diagnostic plots to check that the model / test you chose was adapted to your data.



# Outline

---

1. Introduction
2. Designing the experiment
3. Description/exploration
4. Normalization
5. Modeling
- 6. SARTools**

SARTools = Statistical Analysis of RNA-Seq Tools [9]

1. Perform a systematic quality control of the data
2. Avoid misusing the DESeq2 or edgeR packages
3. Keep track of all the parameters used: reproducible research
4. Provide a HTML report containing all the results of the analysis

`github.com/PF2-pasteur-fr/SARTools/`

# Input files

---

**Target:** tab-delimited text file describing the experimental design:

label	files	condition
WT1	WT1.counts.txt	WT
WT2	WT2.counts.txt	WT
KO1	KO1.counts.txt	KO
KO2	KO2.counts.txt	KO

**Counts:** one tab-delimited text file per sample (from HTSeq-count or featureCounts):

gene1	23
gene2	355
gene3	0
...	...
gene4	3643

# Usage: with



```
#####  
###           parameters: to be modified by the user           ###  
#####  
rm(list=ls())           # remove all the objects from the R session  
  
workDir <- "C:/path/to/your/working/directory/"           # working directory for the R session  
  
projectName <- "projectName"           # name of the project  
author <- "Your name"           # author of the statistical analysis/report  
  
targetFile <- "target.txt"           # path to the design/target file  
rawDir <- "raw"           # path to the directory containing raw counts files  
featuresToRemove <- c("alignment_not_unique",           # names of the features to be removed  
                      "ambiguous", "no_feature",           # (specific HTSeq-count information and rRNA for example)  
                      "not_aligned", "too_low_aQual")  
  
varInt <- "group"           # factor of interest  
condRef <- "WT"           # reference biological condition  
batch <- NULL           # blocking factor: NULL (default) or "batch" for example  
  
fitType <- "parametric"           # mean-variance relationship: "parametric" (default) or "local"  
cooksCutoff <- TRUE           # TRUE/FALSE to perform the outliers detection (default is TRUE)  
independentFiltering <- TRUE           # TRUE/FALSE to perform independent filtering (default is TRUE)  
alpha <- 0.05           # threshold of statistical significance  
pAdjustMethod <- "BH"           # p-value adjustment method: "BH" (default) or "BY"  
  
typeTrans <- "VST"           # transformation for PCA/clustering: "VST" or "rlog"  
locfunc <- "median"           # "median" (default) or "shorth" to estimate the size factors  
  
colors <- c("dodgerblue", "firebrick1",           # vector of colors of each biological condition on the plots  
           "MediumVioletRed", "SpringGreen")
```



# Usage: with Galaxy

The screenshot displays the Galaxy / ABiMS interface for configuring the SARTools DESeq2 tool (version 0.99.2). The interface is divided into three main sections:

- Left Sidebar (Tools):** Contains a search bar and a list of tool categories including Get Data, MICRHODE WORKFLOW, ABiMS WORKFLOWS, W4M WORKFLOWS, COMMON TOOLS, and Send Data.
- Central Configuration Area:** Contains the following fields and options:
  - Name of the project used for the report:** 2015-T048
  - Name of the report author:** Hugo Varet
  - Design / target file:** 62: targetT048.txt
  - Zip file containing raw counts files:** 182: t048.zip
  - Names of the features to be removed:** alignment\_not\_unique,ambiguous,no\_feature,not\_aligned,too\_low\_aQual
  - Factor of interest:** time
  - Reference biological condition:** T0
  - Advanced Parameters:** Hide
- Right Sidebar (History):** Shows a list of datasets with their names, sizes, and actions (view, edit, delete). The datasets listed are:
  - DESeq2 (73.4 MB)
  - 182: t048.zip
  - 62: targetT048.txt
  - 2: targetAnonymise.txt
  - 1: rawAnonymises.zip

# Output: HTML report

## 1 Introduction

2 Description of raw data

3 Variability within the experiment:  
data exploration

4 Normalization

5 Differential analysis

6 R session information and  
parameters

Bibliography

## Statistical report of project testdeseq2: pairwise comparison(s) of conditions with DESeq2

*Hugo Varet*

**2017-12-11**

The SARTools R package which generated this report has been developed at PF2 - Institut Pasteur by M.-A. Dillies and H. Varet ([hugo.varet@pasteur.fr](mailto:hugo.varet@pasteur.fr)). Thanks to cite H. Varet, L. Brillet-Guéguen, J.-Y. Coppee and M.-A. Dillies, *SARTools: A DESeq2- and EdgeR-Based R Pipeline for Comprehensive Differential Analysis of RNA-Seq Data*, PLoS One, 2016, doi: <http://dx.doi.org/10.1371/journal.pone.0157022> when using this tool for any analysis published.

## 1 Introduction

The analyses reported in this document are part of the testdeseq2 project. The aim is to find features that are differentially expressed between T0, T4 and T8. The statistical analysis process includes data normalization, graphical exploration of raw and normalized data, test for differential expression for each feature between the conditions, raw p-value adjustment and export of lists of features having a significant differential expression between the conditions.

The analysis is performed using the R software [1], Bioconductor [2] packages including DESeq2 [3,4] and the SARTools package developed at PF2 - Institut Pasteur. Normalization and differential analysis are carried out according to the DESeq2 model and package. This report comes with additional tab-delimited text files that contain lists of differentially expressed features.

For more details about the DESeq2 methodology, please refer to its related publications [3,4].

## 2 Description of raw data

The count data files and associated biological conditions are listed in the following table.

label	files	groupbatch
T0-1	sampleT0-1-htseq.outT0	1
T0-5	sampleT0-5-htseq.outT0	2
T0-6	sampleT0-6-htseq.outT0	3
T4-1	sampleT4-1-htseq.outT4	1
T4-2	sampleT4-2-htseq.outT4	2
T4-3	sampleT4-3-htseq.outT4	3
T8-1	sampleT8-1-htseq.outT8	1
T8-2	sampleT8-2-htseq.outT8	2
T8-3	sampleT8-3-htseq.outT8	3

Table 1: Data files and associated biological conditions.

1 Introduction
2 Description of raw data
3 Variability within the experiment: data exploration
4 Normalization
5 Differential analysis
<b>6 R session information and parameters</b>
Bibliography

## 6 R session information and parameters

The versions of the R software and Bioconductor packages used for this analysis are listed below. It is important to save them if one wants to re-perform the analysis in the same conditions.

- R version 3.4.1 (2017-06-30), x86\_64-pc-linux-gnu
- Locale: LC\_CTYPE=fr\_FR.UTF-8, LC\_NUMERIC=C, LC\_TIME=fr\_FR.UTF-8, LC\_COLLATE=fr\_FR.UTF-8, LC\_MONETARY=fr\_FR.UTF-8, LC\_MESSAGES=fr\_FR.UTF-8, LC\_PAPER=fr\_FR.UTF-8, LC\_NAME=C, LC\_ADDRESS=C, LC\_TELEPHONE=C, LC\_MEASUREMENT=fr\_FR.UTF-8, LC\_IDENTIFICATION=C
- Running under: Ubuntu 16.04.3 LTS
- Matrix products: default
- BLAS: /usr/lib/libblas/libblas.so.3.6.0
- LAPACK: /usr/lib/lapack/liblapack.so.3.6.0
- Base packages: base, datasets, graphics, grDevices, methods, parallel, stats, stats4, utils
- Other packages: Biobase 2.38.0, BiocGenerics 0.24.0, DelayedArray 0.4.1, DESeq2 1.18.1, edgeR 3.20.1, GenomInfoDb 1.14.0, GenomicRanges 1.30.0, IRanges 2.12.0, limma 3.34.1, matrixStats 0.52.2, S4Vectors 0.16.0, SARTools 1.5.2, SummarizedExperiment 1.8.0, xtable 1.8-2
- Loaded via a namespace (and not attached): acepack 1.4.1, annotate 1.56.1, AnnotationDbi 1.40.0, backports 1.1.1, base64enc 0.1-3, BiocParallel 1.12.0, bit 1.1-12, bit64 0.9-7, bitops 1.0-6, blob 1.1.0, checkmate 1.8.5, cluster 2.0.6, colorspace 1.3-2, compiler 3.4.1, data.table 1.10.4-3, DBI 0.7, digest 0.6.12, evaluate 0.10.1, foreign 0.8-69, Formula 1.2-2, genefilter 1.60.0, geneplotter 1.56.0, GenomInfoDbData 0.99.1, ggplot2 2.2.1, grid 3.4.1, gridExtra 2.3, gtable 0.2.0, Hmisc 4.0-3, htmlTable 1.9, htmltools 0.3.6, htmlwidgets 0.9, knitr 1.17, lattice 0.20-35, latticeExtra 0.6-28, lazyeval 0.2.1, locfit 1.5-9.1, magrittr 1.5, Matrix 1.2-10, memoise 1.1.0, munsell 0.4.3, nnet 7.3-12, plyr 1.8.4, RColorBrewer 1.1-2, Rcpp 0.12.13, RCurl 1.95-4.8, rlang 0.1.4, rmarkdown 1.8, rpart 4.1-11, rprojroot 1.2, RSQLite 2.0, scales 0.5.0, splines 3.4.1, stringi 1.1.6, stringr 1.2.0, survival 2.41-3, tibble 1.3.4, tools 3.4.1, XML 3.98-1.9, XVector 0.18.0, yaml 2.1.14, zllbioc 1.24.0

Parameter values used for this analysis are:

- workDir: .
- projectName: testdeseq2
- author: Hugo Varet
- targetFile: target.txt
- rawDir: raw
- featuresToRemove: alignment\_not\_unique, ambiguous, no\_feature, not\_aligned, too\_low\_aQual
- varInt: group
- condRef: T0
- batch: NULL
- fitType: parametric
- cooksCutoff: TRUE
- independentFiltering: TRUE
- alpha: 0.05
- pAdjustMethod: BH
- typeTrans: VST
- locfunc: median
- colors: dodgerblue, firebrick1, MediumVioletRed, SpringGreen

# Output: lists of differentially expressed genes

---

## Three tab-delimited text files per comparison:

- \*.complete.txt: all the genes
- \*.up.txt: up-regulated genes ordered by adj.  $p$ -value
- \*.down.txt: down-regulated genes ordered by adj.  $p$ -value

**Columns:** gene id,  $\log_2$ (Fold-Change), adjusted  $p$ -value, ...

## SARTools vignette for the differential analysis of 2 or more conditions with DESeq2 or edgeR

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SARTools version: `r packageVersion("SARTools")`

Authors: M.-A. Dillies and H. Varet ([hugo.varet@pasteur.fr](mailto:hugo.varet@pasteur.fr)) - Transcriptome and Epigenome Platform, Institut Pasteur, Paris

Website: <https://github.com/PF2-pasteur-fr/SARTools>

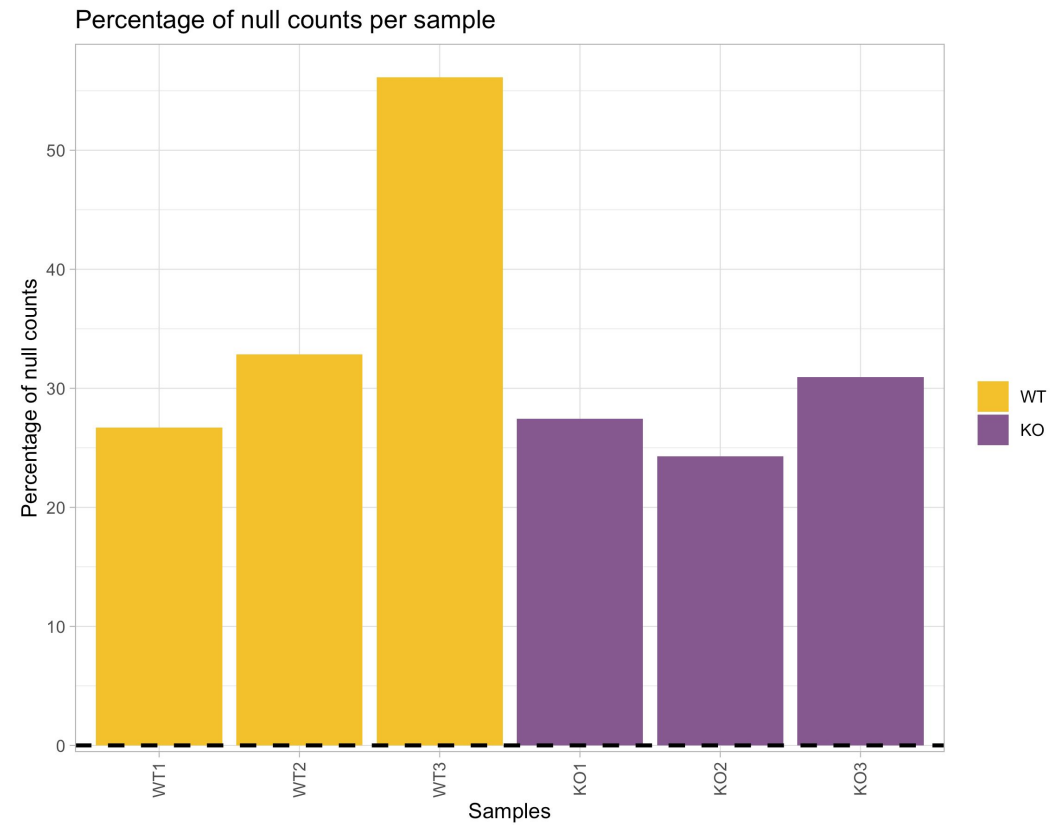
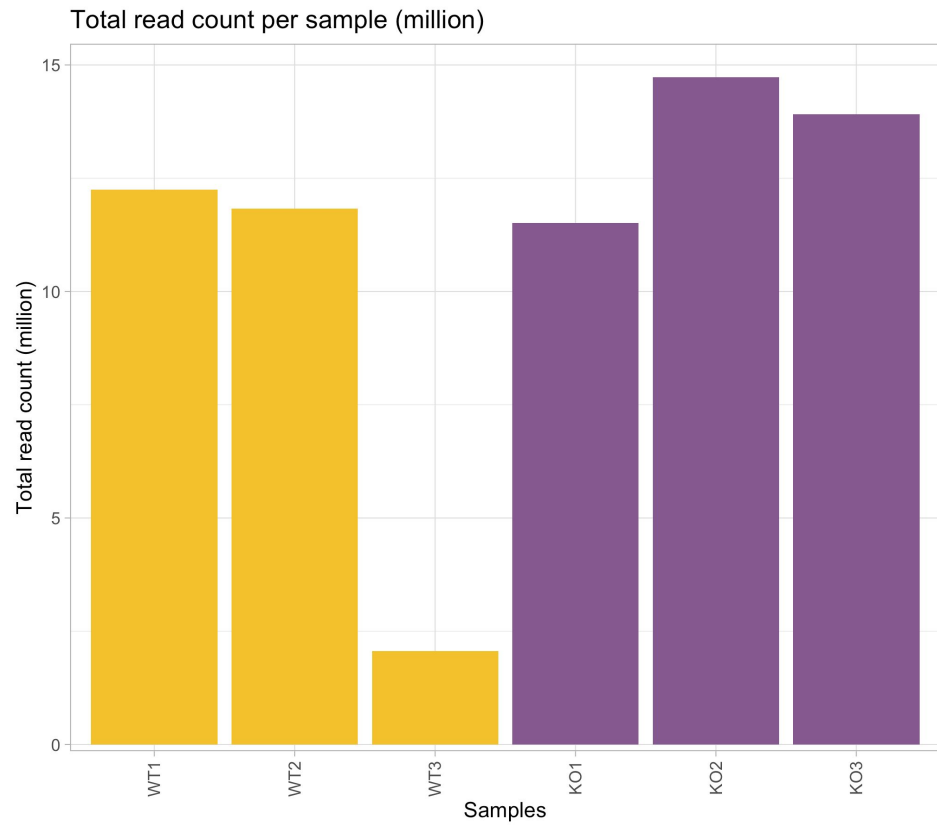
### 1 Introduction

---

This document aims to illustrate the use of the SARTools R package in order to compare two or more biological conditions in a RNA-Seq framework. SARTools provides tools to generate descriptive and diagnostic graphs, to run the

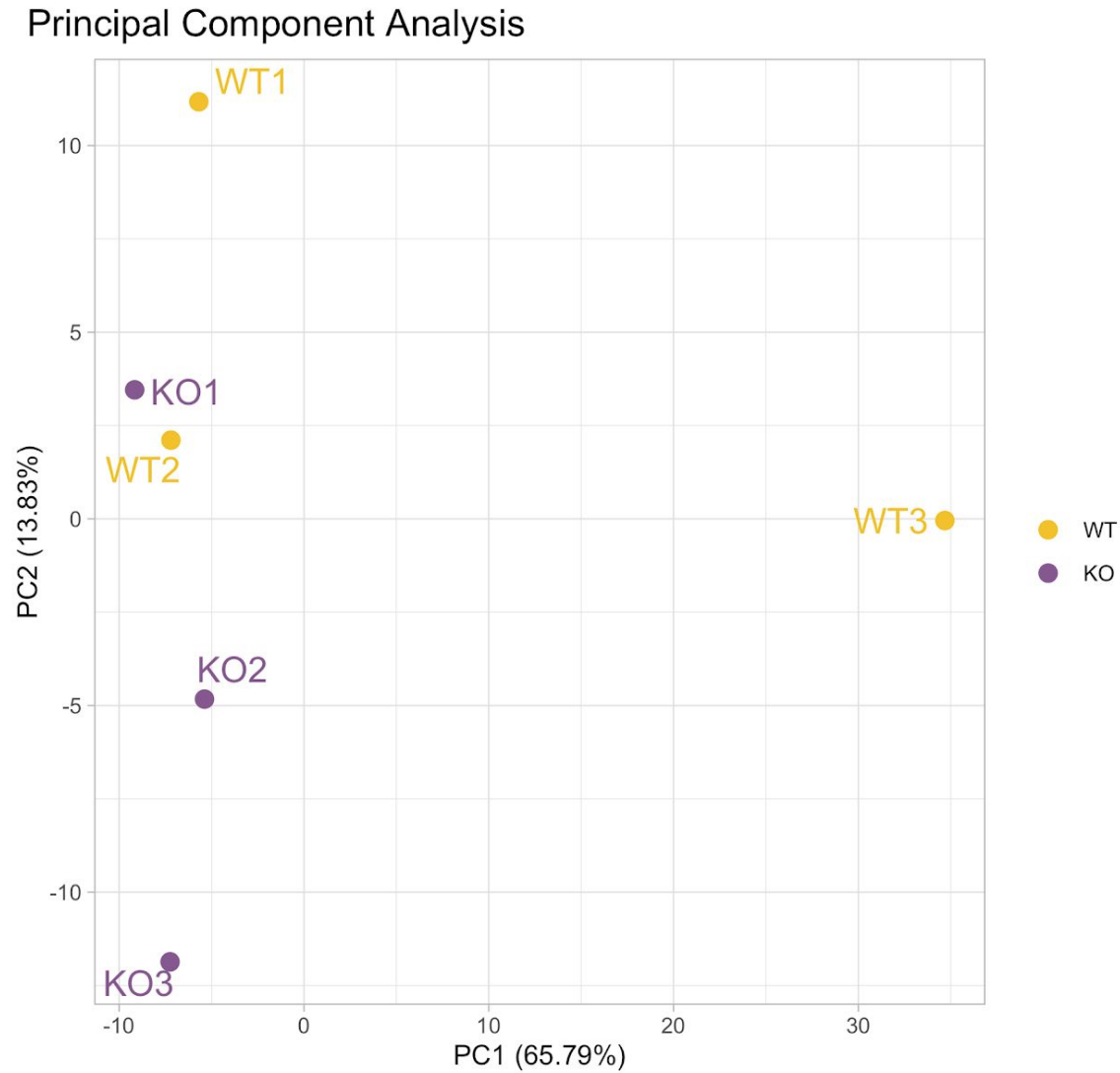
- Installation
- Input files
- Definition of the parameters
- Potential issues: technical problems, inversion of samples, batch effects, outliers...

# Potential issue: detecting outliers



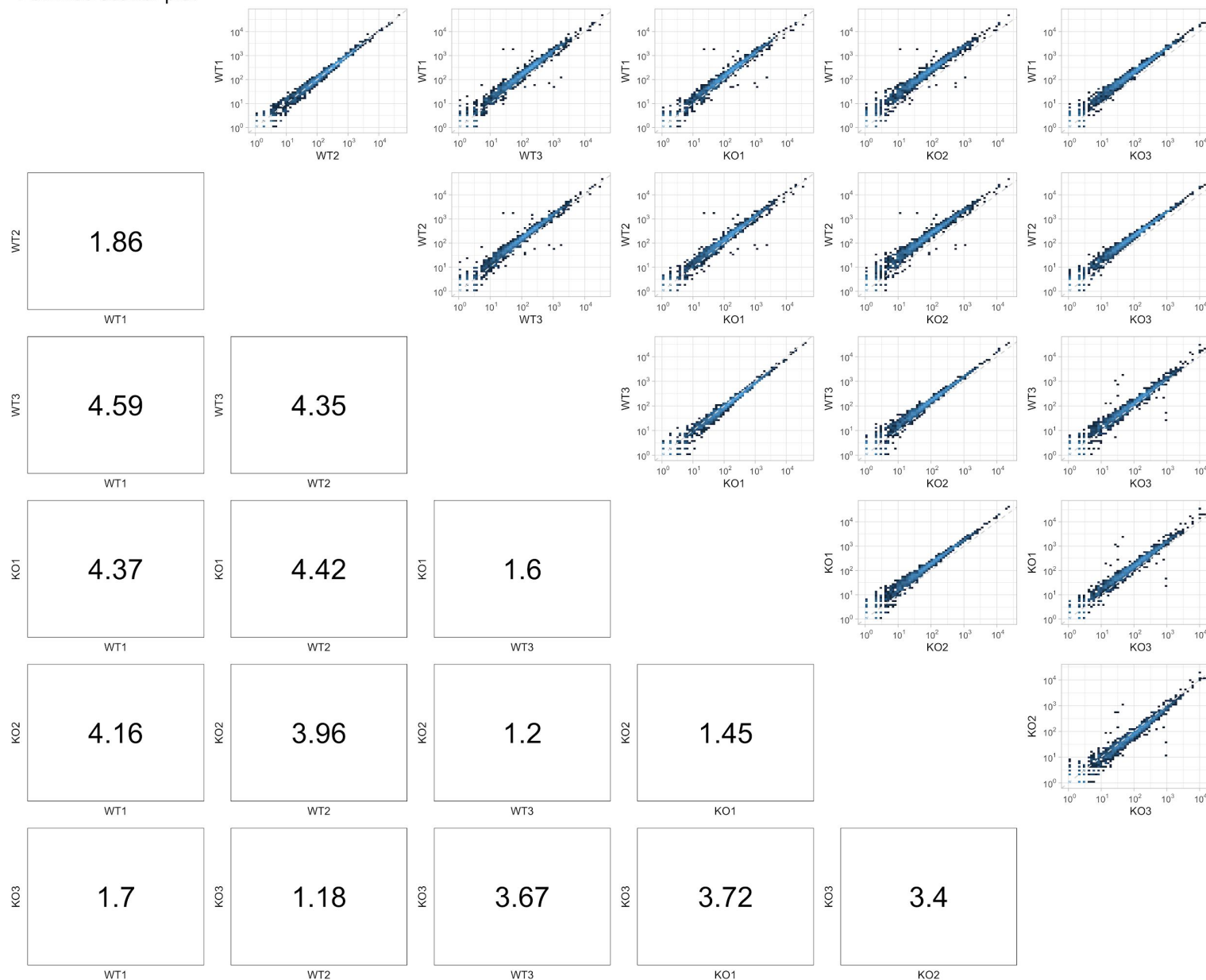
# Potential issue: detecting outliers

---



# Potential issue: inversion of samples

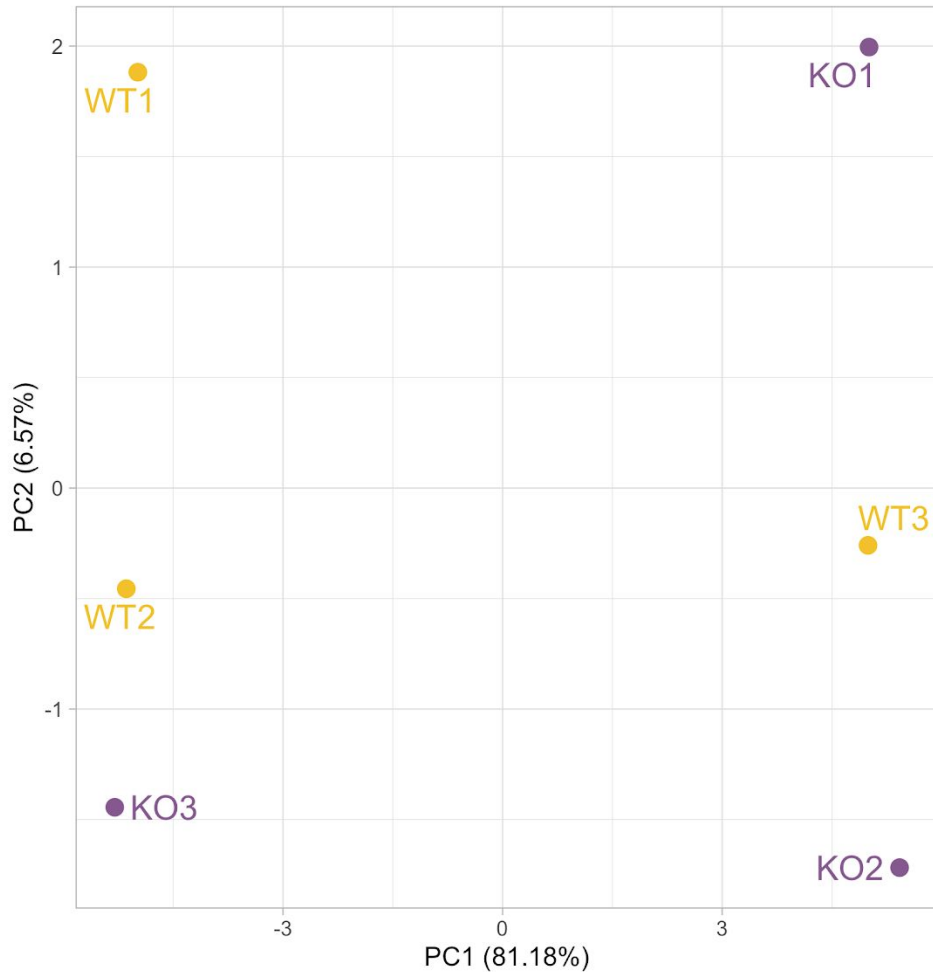
Pairwise scatter plot



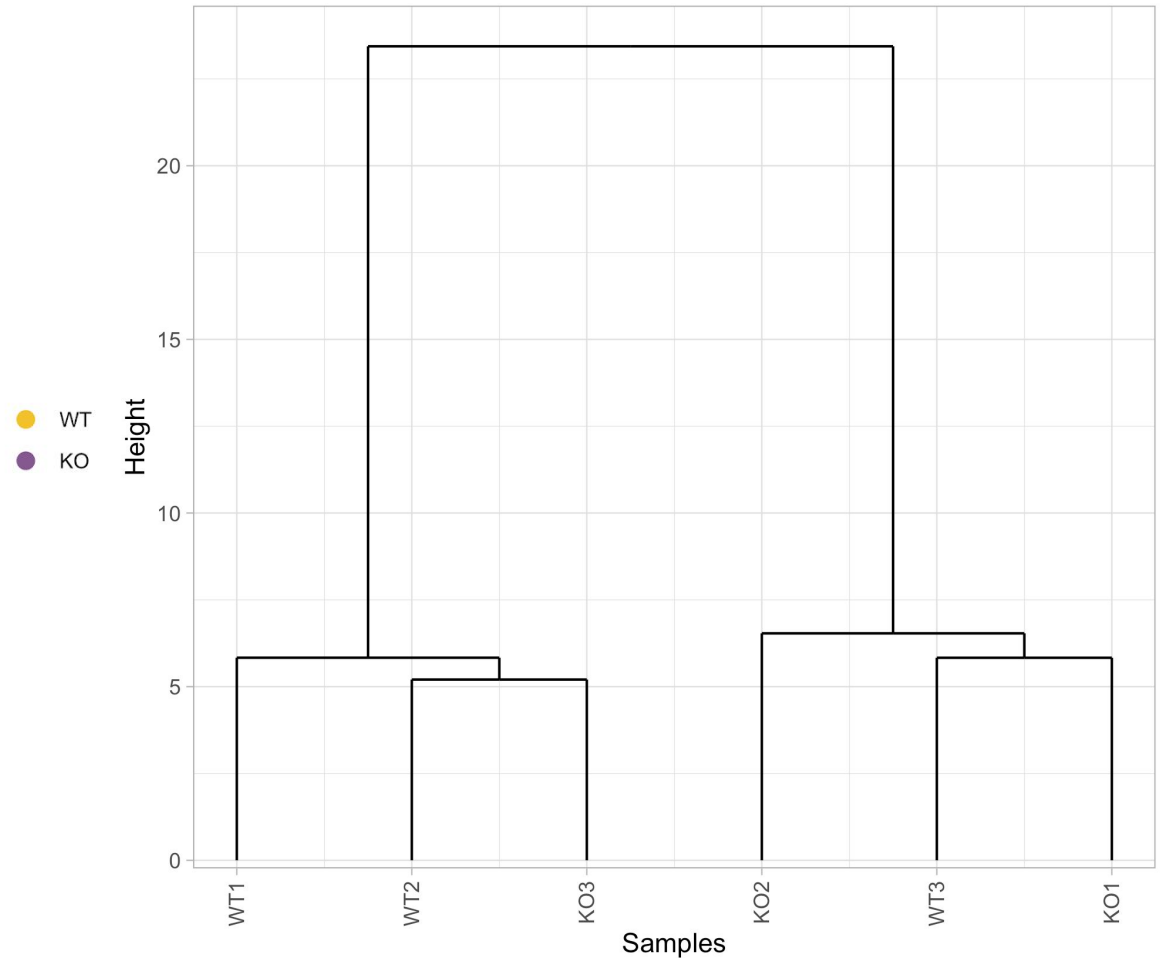


# Potential issue: inversion of samples

Principal Component Analysis



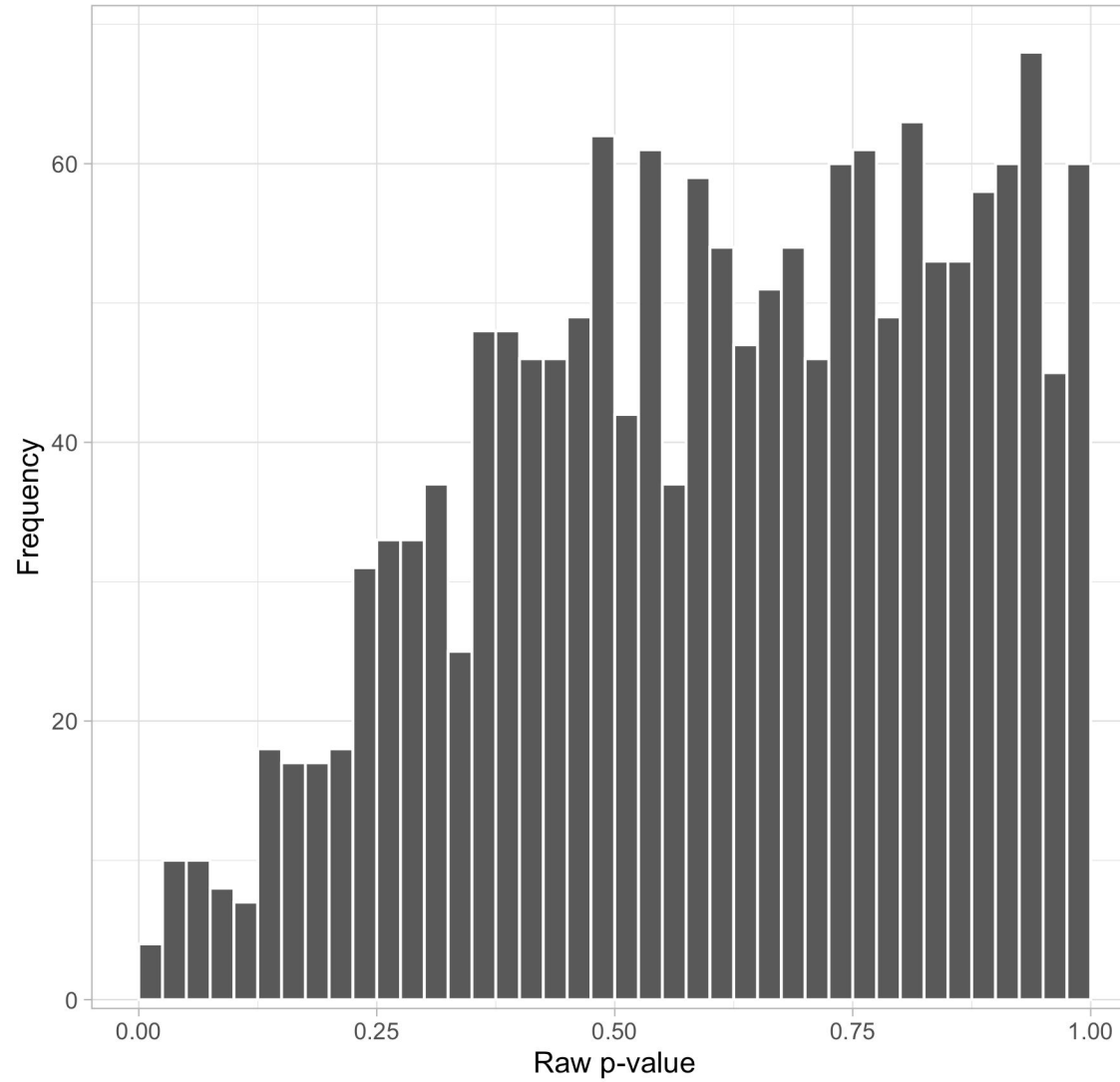
Cluster dendrogram  
Euclidean distance, Ward criterion



# Potential issue: inversion of samples

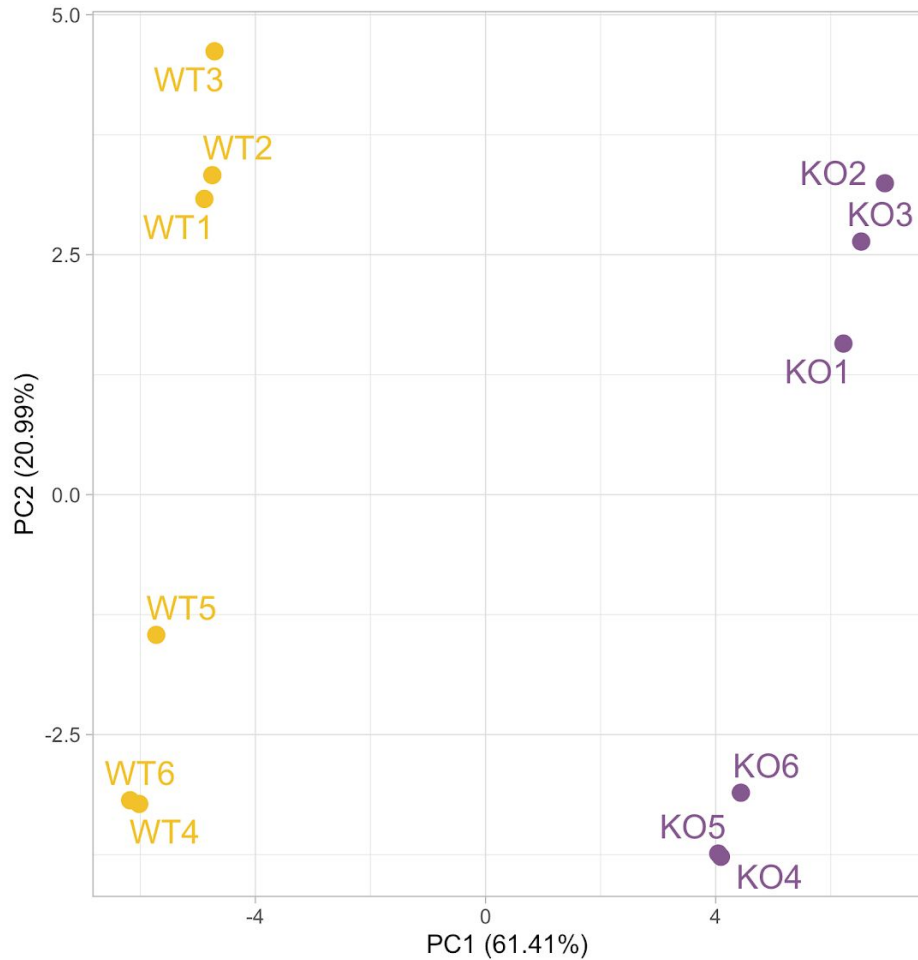
---

Distribution of raw p-values - KO vs WT

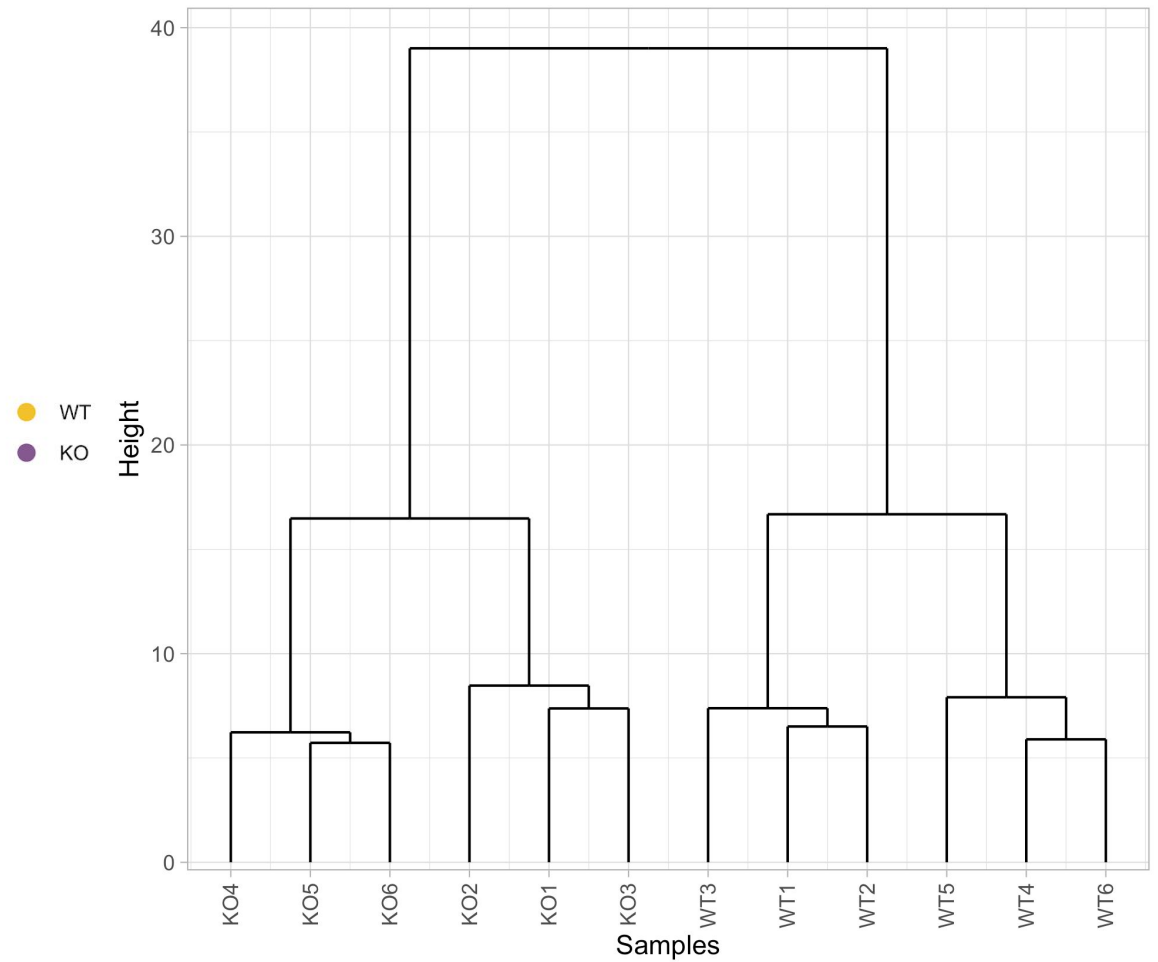


# Potential issue: batch effect

Principal Component Analysis

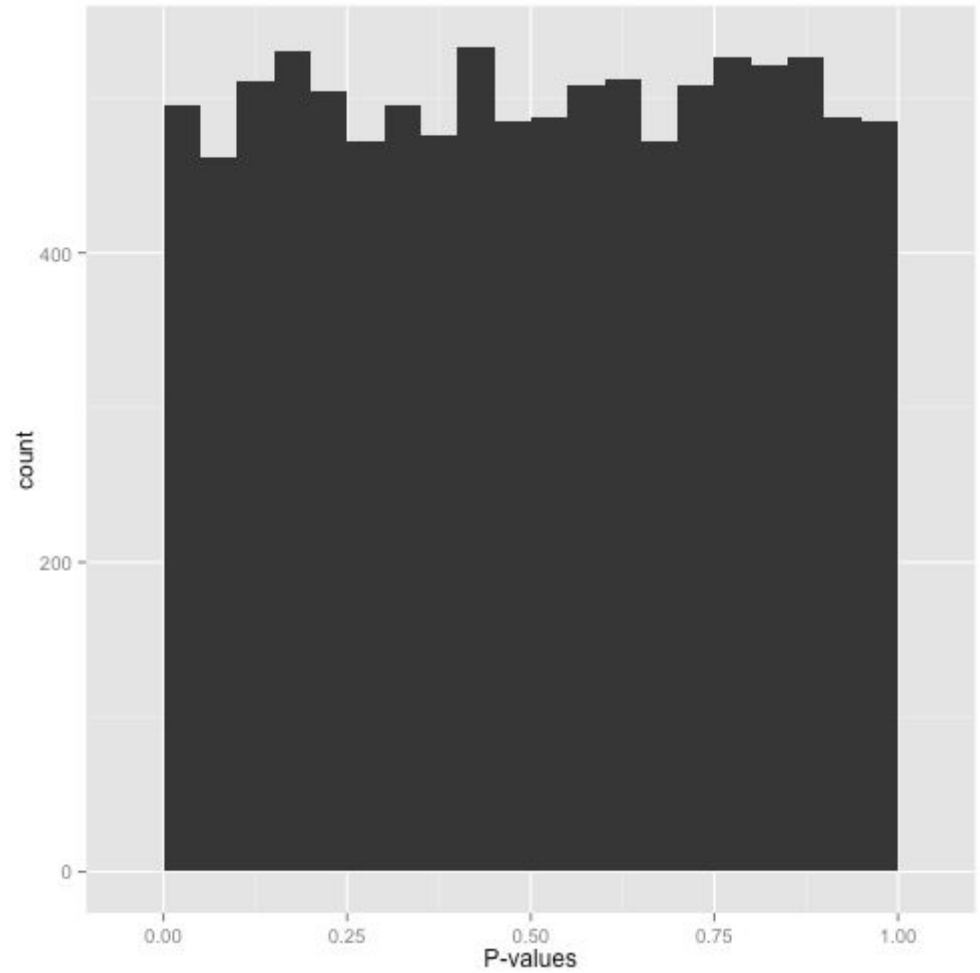
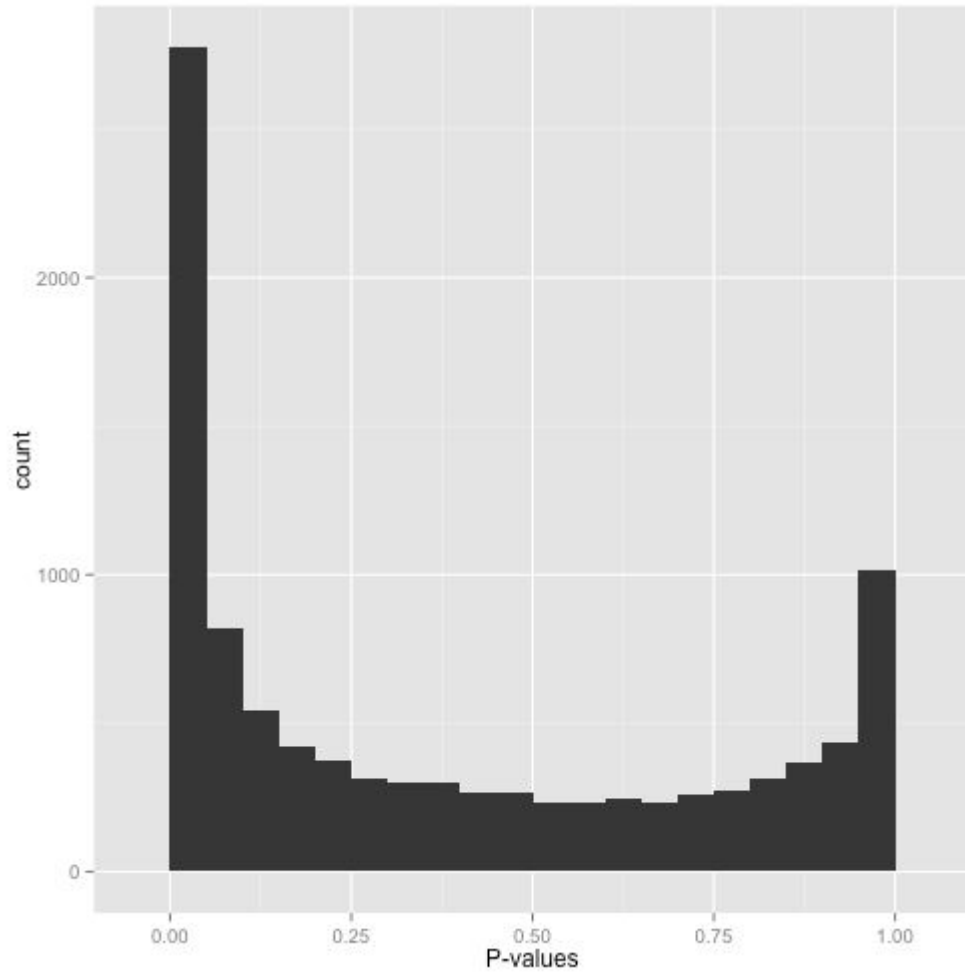


Cluster dendrogram  
Euclidean distance, Ward criterion



# Other cases :

---



# DESeq2 and edgeR common parameters

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- Project and author names
- Target and count files paths
- Rows of the count files to remove
- Factor of interest and the reference biological condition
- Adjustment variable (batch effect, pairing) in the target file
- Multiple testing adj. method and significance threshold  $\alpha$
- Colors for the graphics

# DESeq2-specific parameters

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- **fitType:** type of link to model the intensity-dispersion relationship, `parametric` (by default) or `local`
- **cooksCutoff:** `TRUE` (by default) to detect genes having outlier counts
- **independentFiltering:** `TRUE` (by default) to filter out lowly expressed genes and gain power on the others
- **typeTrans:** `VST` (by default) or `rlog` to make the data homoscedastic to perform exploratory data analysis (PCA, clustering, heatmaps)
- **lfcshrink:** `median` (by default) or `shrink`. `shrink` allows to improve the normalization for some cases

# edgeR-specific parameters

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- **cpmCutoff:** low counts filtering threshold (in counts per million of reads)
- **gene.selection:** genes selection method for the MDS-plot (`pairwise` by default)
- **normalizationMethod:** `TMM` by default, `RLE` (DESeq2), or `upperquartile`

# Conclusion

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## SARTools...

- facilitates the utilization of DESeq2 and edgeR
- performs quality control and helps to detect potential problems
- fits the **reproducible research** criteria

Take time to interpret each figure/table in the HTML report!



# Interpreting lists of DE genes: gene-set level analysis

---

## What is a gene-set?

→ Any group of genes having a biological meaning

Note: some genes can belong to several sets and others to none

## Two main approaches:

- **Competitive** null hypothesis: genes in the set are “as DE as” genes not in the set
- **Self-contained** null hypothesis: genes in the set are not DE

## Several methods:

- Over-Representation Analysis (competitive): are genes in the set more DE than genes not in the set? → Fisher’s hypergeometric test
- Linear models using limma R package’s functions:
  - **competitive**: `camera()` and `romer()`
  - **self-contained**: `roast()` and `fry()`

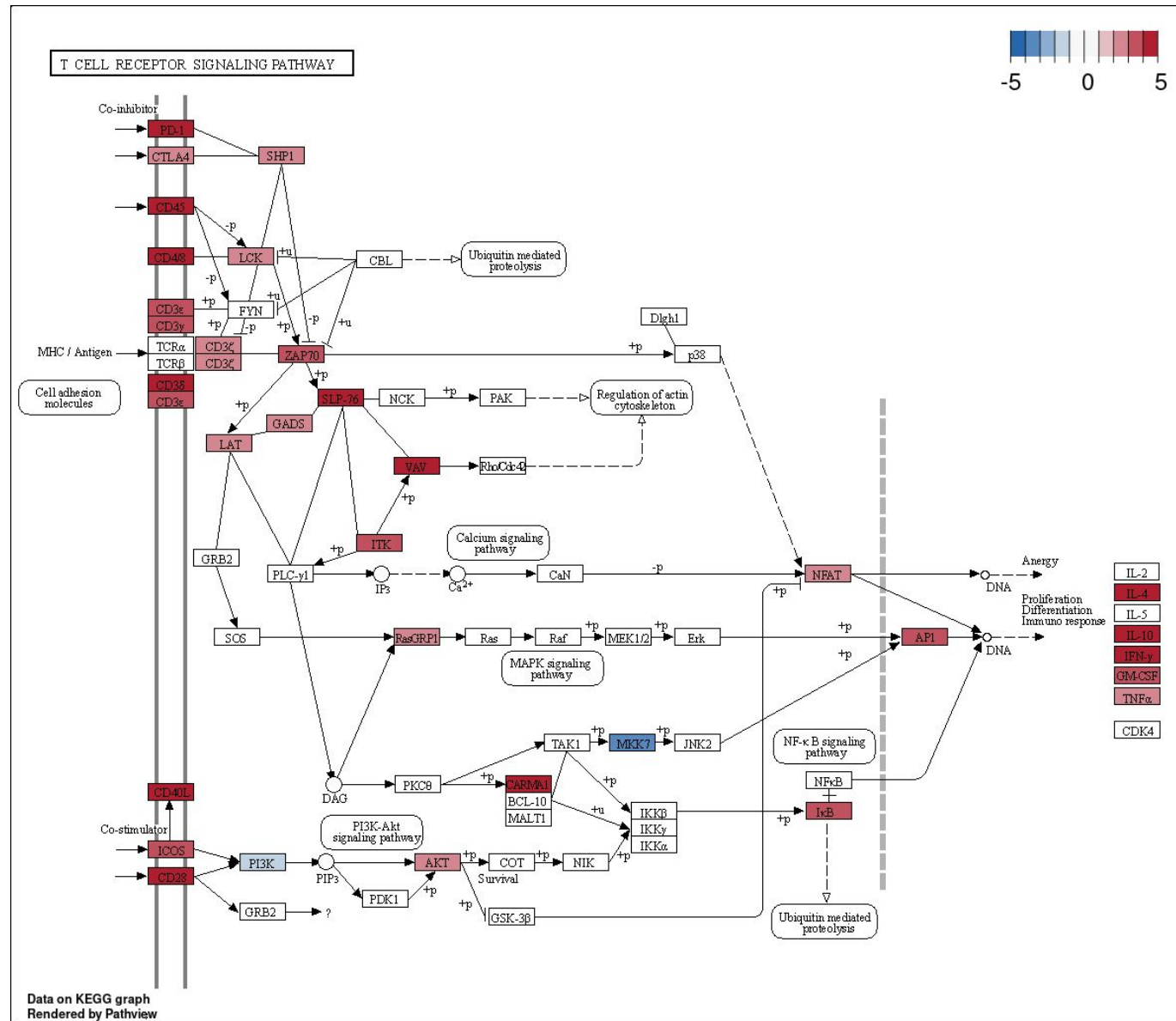
# Interpreting lists of DE genes: gene-set level analysis

---

Several issues/options to deal with:

- Make gene IDs compatible with the gene-sets by converting diff. analysis **Ensembl** IDs (for instance) into **ENTREZ** IDs: no perfect matching and be careful with the annotation version(s) used
- Which gene-sets to test?
  - depends on the **biological question**
  - will impact the p-value adjustment for multiple testing
  - restrict the **background** to genes belonging to at least one set?
- Separate down- and up-regulated genes?
- Import gene-sets into R and make them ready for the analysis: from MSigDB or R packages... but there may be some differences

# Interpreting lists of DE genes: gene-set level analysis



# General conclusion

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- RNA-Seq project = discussions between biologists, bioinformaticians and biostatisticians... as soon as the project starts!
- Statistical needs during all the project, not only for the differential analysis
  - Normalization step is critical: the assumptions have to be checked
  - No magic recipe: need to choose the statistical model according to your biological question
  - Statistical analysis must not be a black box!
- Data visualization is a crucial tool along all the steps of the analysis



**Complex experimental design → difficult interpretation of the results**

# The end

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Thank you for your attention!

# Bibliography

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