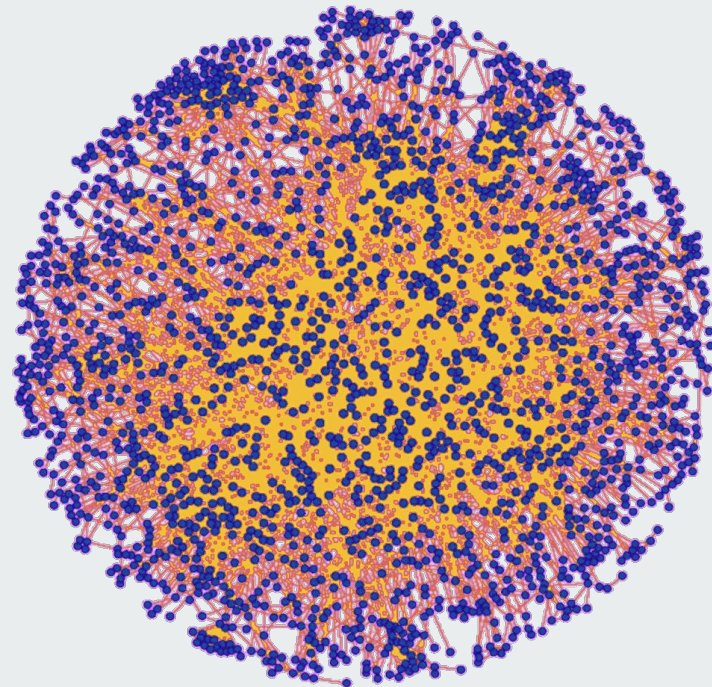


Network theory

Galadriel Brière, Morgane Térézol, Bastien Chassagnol

Inspired by the slides of Anaïs Baudot



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<https://orcid.org/0000-0003-0885-7933> (Anaïs Baudot)

<https://orcid.org/0000-0003-1808-3759> (Galadriel Brière)

<https://orcid.org/0000-0002-8955-2391> (Bastien Chassagnol)

<https://orcid.org/0009-0005-0362-1835> (Benjamin Loire)

ÉCOLE THÉMATIQUE

ETBII

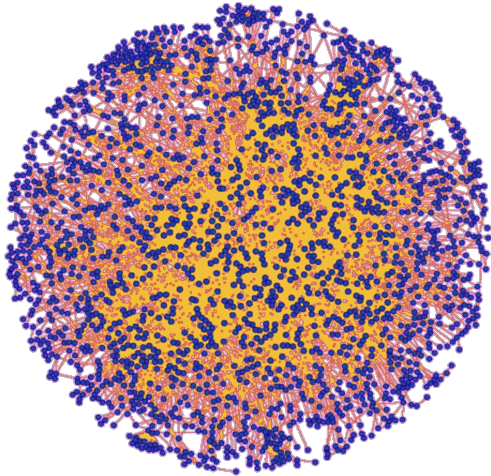
BIOINFORMATIQUE INTÉGRATIVE IFB



INSTITUT FRANÇAIS DE BIOINFORMATIQUE



Outline



Source: <https://www3.nd.edu/~tmilenko/research.html>.

General Introduction, Key Concepts

Network Biology, Network Science, Complex Systems, ...

Network Construction/Inference

Data sources, Distances/Similarities, Correlation, ...

Network Analysis

Measures

Degree, Centrality, Distances, ...

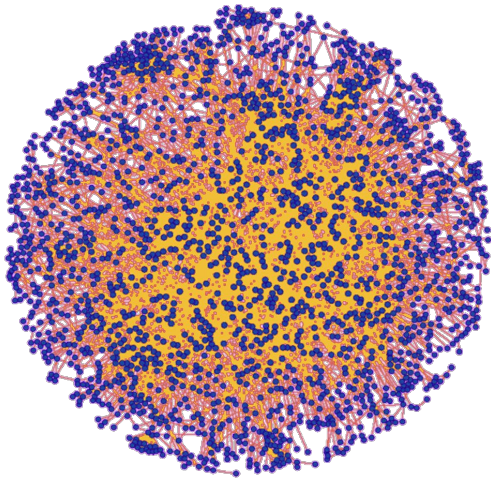
Algorithms

Diffusion, Clustering, Embedding, ...

Networks and Integration

Multiplex Networks, Multilayer Networks, Knowledge Graphs, ...

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Key Concept 1: **Systems Biology**

➤ Computational and mathematical analysis and modeling of **complex biological systems**.

- **Complex Systems**

Systems composed of **many components**
These components may **interact with each others**
Properties emerge from these interactions

The whole is greater than the sum of its parts

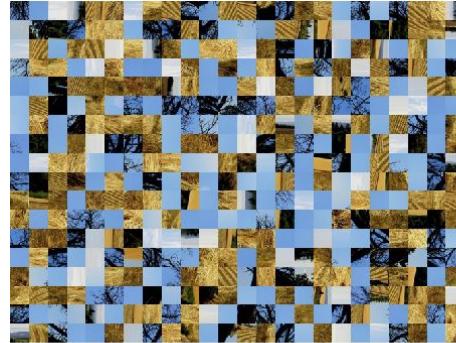
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(a)



(b)

Source: CatalyzeX. "DNN-Buddies: A Deep Neural Network-Based Estimation Metric for the Jigsaw Puzzle Problem: Paper and Code." CatalyzeX. Accessed September 1, 2023. <https://www.catalyzeX.com/>.

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- **Complex Systems**

Systems composed of **many components**
These components may **interact with each others**
Properties emerge from these interactions

The whole is greater than the sum of its parts

- **Ecological Systems**

Systems components: **organisms, ...**
Interactions: **prey, symbiosis, competition, ...**
Emerging properties: **resilience, stability, ...**

- **Systems Biology**

Systems components: **genes/proteins, ...**
Interactions: **PPI, co-expression, ...**
Emerging properties: **Phenotypes**

Phenotype does not emerge from isolated biological molecules but from their interactions

- **Nervous System**

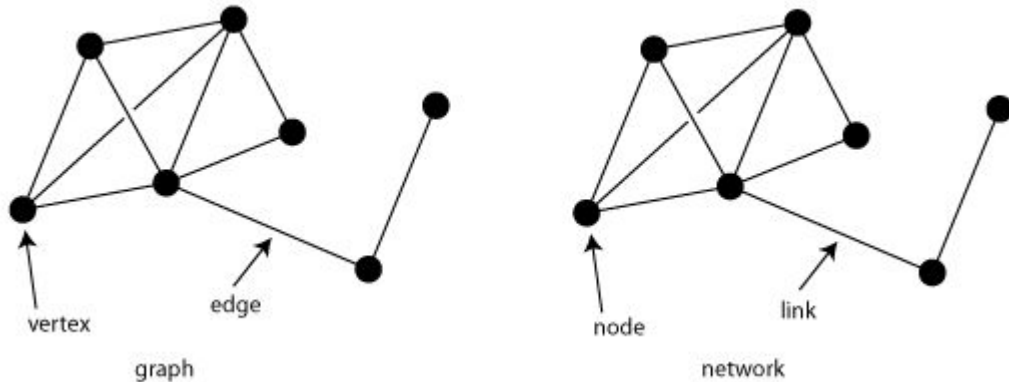
Systems components: **neurons, axons, dendrites, ...**
Interactions: **synaptic transmission, ...**
Emerging properties: **memory, cognition, ...**

- **etc...**

Key Concept 2: Graph Theory/Network Science

- **Networks** are real-world systems modeled using **graphs**.

$G = (V, E)$, where V is the set of vertices and $E \subseteq (V \times V)$
 is the set of edges

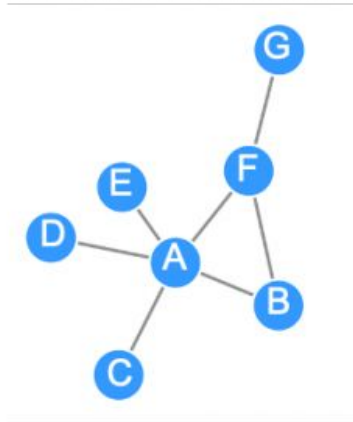


- In practice, the terms **network** and **graph** are often used interchangeably.

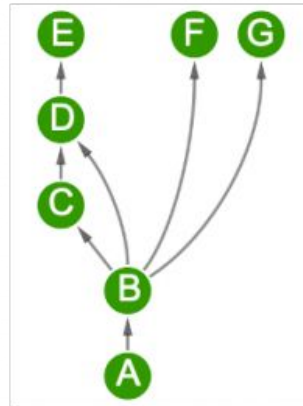
Key Concept 2: Graph Theory/Network Science

➤ Various types of networks...

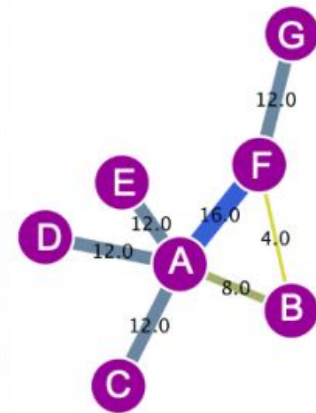
Undirected



Directed



Weighted



Source: EMBL-EBI. "Graph Theory: Graph Types and Edge Properties | Network Analysis of Protein Interaction Data." Accessed August 28, 2023.

<https://www.ebi.ac.uk/training/online/courses/network-analysis-of-protein-interaction-data-an-introduction/introduction-to-graph-theory/graph-theory-graph-types-and-edge-properties/>

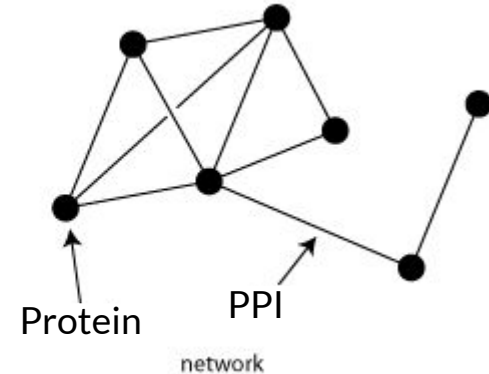
Network Science and Systems Biology

- **Systems Biology**

Systems components: **genes/proteins, ...**
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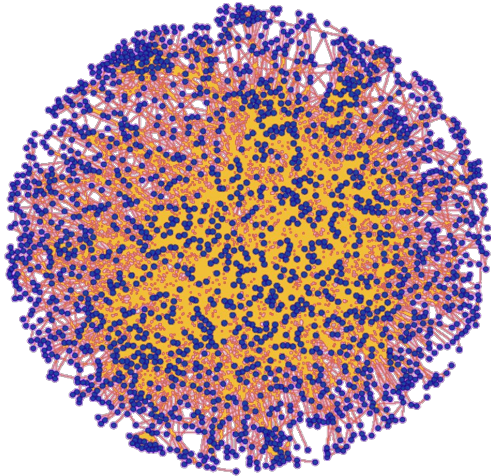
Phenotype does not emerge from isolated biological molecules but from their interactions

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Graph theory/network science: a **powerful toolbox** for representing and studying complex systems.

Outline



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General Introduction, Key Concepts

Network Biology, Network Science, Complex Systems, ...

Network Construction/Inference

Types of associations: from direct correlations, to directed causal interactions

Zoom on Bayesian Networks

Network Analysis

Measures

Degree, Centrality, Distances, ...

Algorithms

Diffusion, Clustering, Embedding, ...

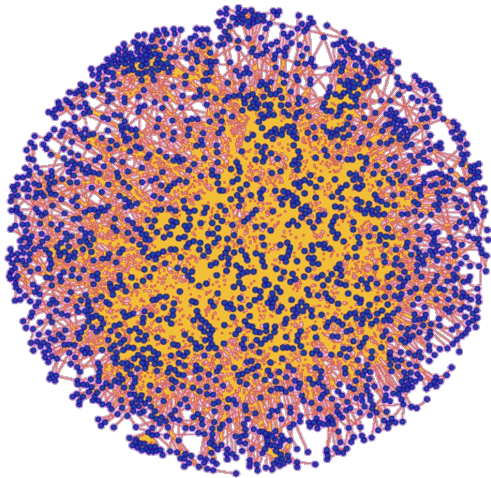
Networks and Integration

Multiplex Networks, Multilayer Networks, Knowledge Graphs, ...

Network Modelling

Boolean networks, ODE models, ...

Data sources

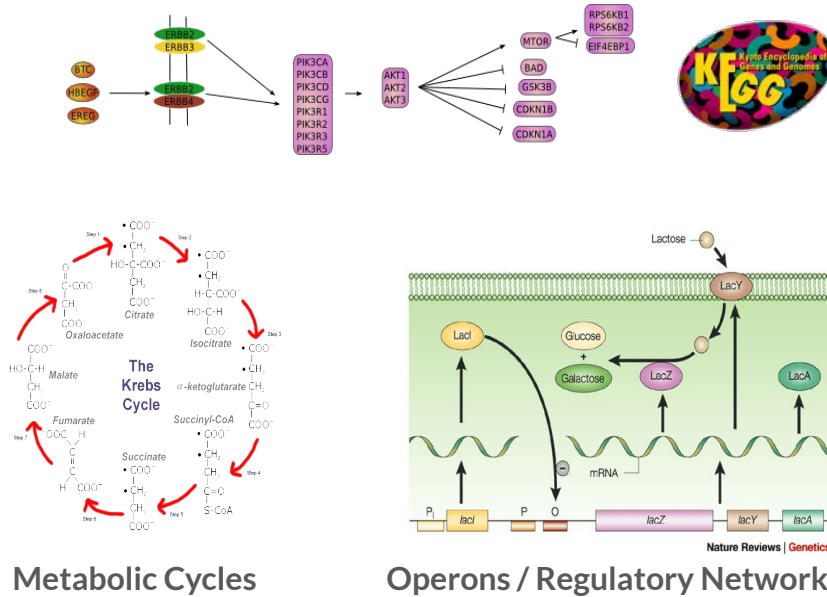


- Expert knowledge and literature
- High-throughput screening
- Inference from (omics) data

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Source 1: Expert knowledge and literature

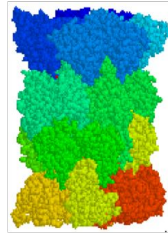
Biological Pathways



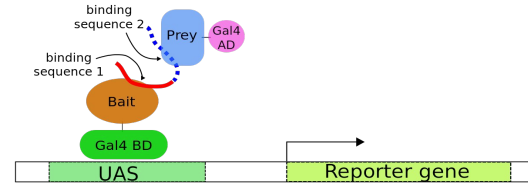
Metabolic Cycles

Operons / Regulatory Networks

Source 2: High-throughput screening



Molecular complex interactions
 -> GFP-trap



Protein-Protein interactions
 -> Yeast 2-hybrids screens

Thousands of interactions in model organisms



STRING

IntAct



etc...

Source 3: Inference from (Omics) data



- Basically, you need two things:
 - A **dataset** with the values of features for various samples
 - An **algorithm** to relate your features (e.g. gene network) or samples (e.g. patient network)

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 - Any type of similarity or distance

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 - A regression model

relationship between j and i

$$X_j = \beta_0 + \beta_1 X_i + \epsilon$$

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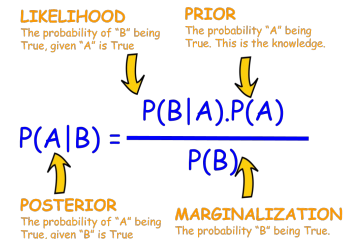
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$$P(X_j | X_i)$$



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$$P(X_j/X_i)$$
 - A regression model

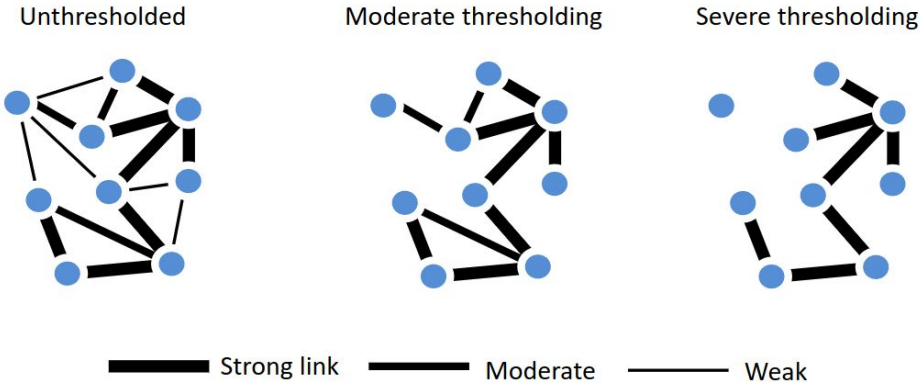
$$X_j = \beta_0 + \beta_1 X_i + \epsilon$$

relationship between j and i
 - A correlation metric (more about this soon!)
 - etc...

Source 3: Inference from (Omics) data

- Basically, you need two things:
 - A **dataset** with the values of features for various samples
 - An **algorithm** to relate your features (e.g. gene network) or samples (e.g. patient network)

- Often, the similarity/distances/correlations/... are **thresholded**:



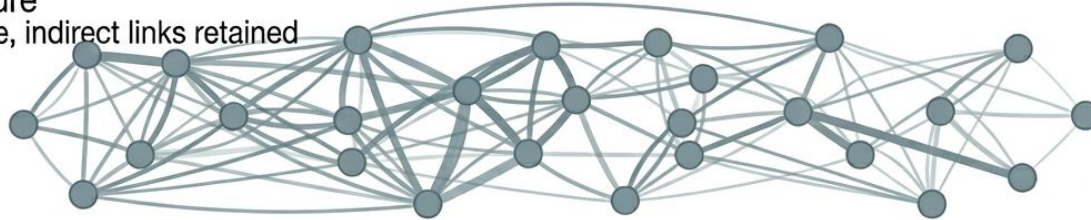
- Eliminating spurious (weak) associations
- Emphasizing topological properties
- Easing computational and storage burden of large graphs

Topologies of network representations

Depending on the algorithm, three paradigms of representing interactions can be identified, corresponding to distinct topological structures.

1. Association networks

Pairwise structure
undirected, dense, indirect links retained

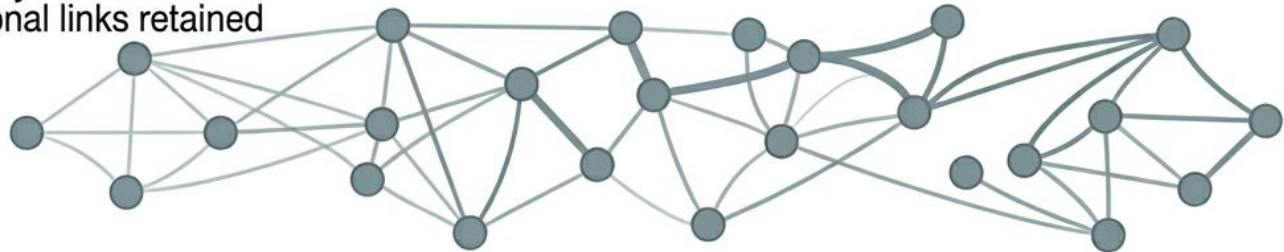


Topologies of network representations

Depending on the algorithm, three paradigms of representing interactions can be identified, corresponding to distinct topological structures.

1. Association networks
2. Dependency networks

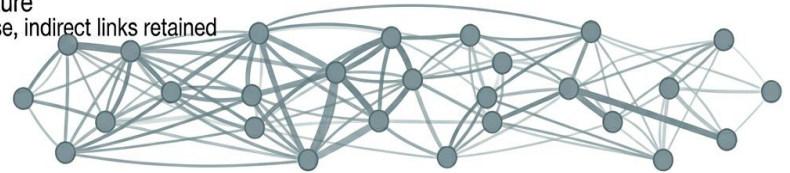
Partial dependency structure
 undirected, conditional links retained



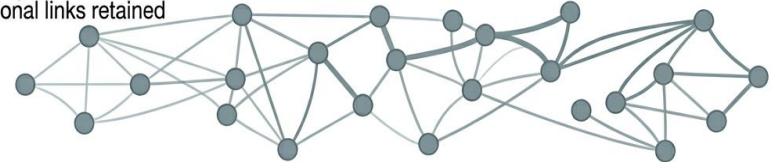
Topologies of network representations

1. Association networks
2. Dependency networks
3. Regulatory networks

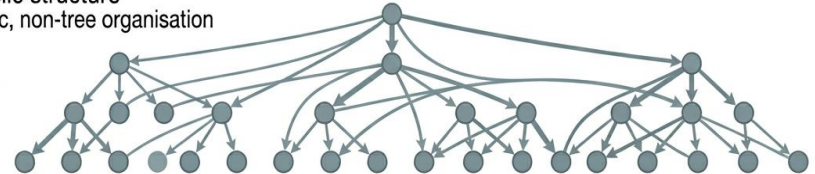
Pairwise structure
undirected, dense, indirect links retained



Partial dependency structure
undirected, conditional links retained



Directed acyclic structure
directed, acyclic, non-tree organisation

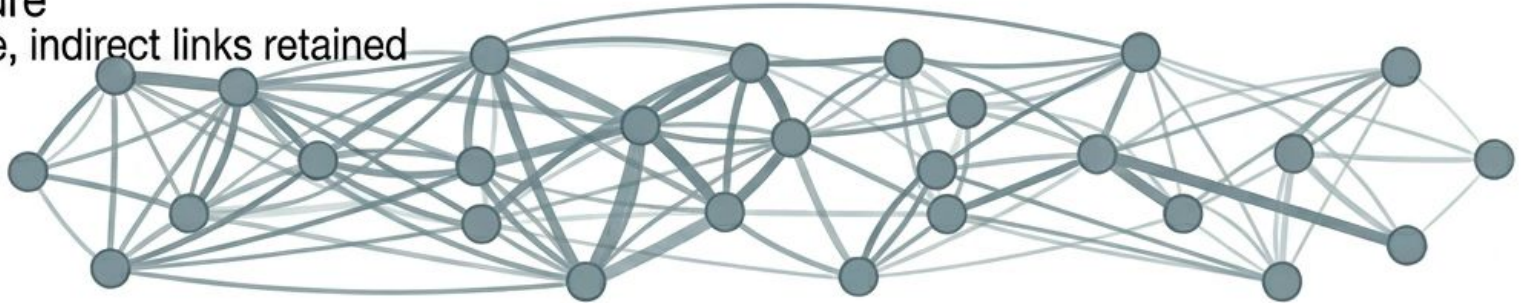


Simpler
More Complex, Biologically Realistic

1) Inference of association networks



Pairwise structure
undirected, dense, indirect links retained



Association networks



Association networks connect entities whose profiles **co-vary** across conditions or samples. They capture **similarity patterns**, not causal influence.

Depending on the level of representation:

- You can connect **features** (genes, proteins, metabolites, ...) → *Feature–Feature network* => see *WGCNA R hands-on*
- Or connect **samples** (patients, cell lines, conditions) → *Sample–Sample network* => see *SNF R hands-on*

Association networks



Which metric to quantify the degree of similarity between two features?



Association networks



Which metric to quantify the degree of similarity between two features?

- **Correlation-based** measures: Pearson, Kendall, ...
- **Mutual information-based** measures
- Depends on the type of the inputs: continuous, discrete, ordinal, ...

Correlation-based measures of association

Measure *how two variables co-vary* across samples. But edges are **undirected** (symmetry: $\text{corr}(A,B) = \text{corr}(B,A)$)

Pearson correlation

- measures *linear* dependence between two vectors
- sensitive to outliers

Spearman correlation

- correlation of *ranks*
- robust to outliers
- detects *non-linear but monotonic trends*

Linear Data

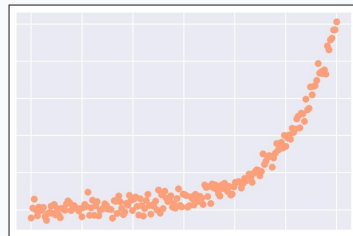


Pearson Correlation **0.96**

Spearman Correlation **0.96**

Same

Non-linear Data



Pearson Correlation **0.76 X**

Spearman Correlation **0.92 ✓**

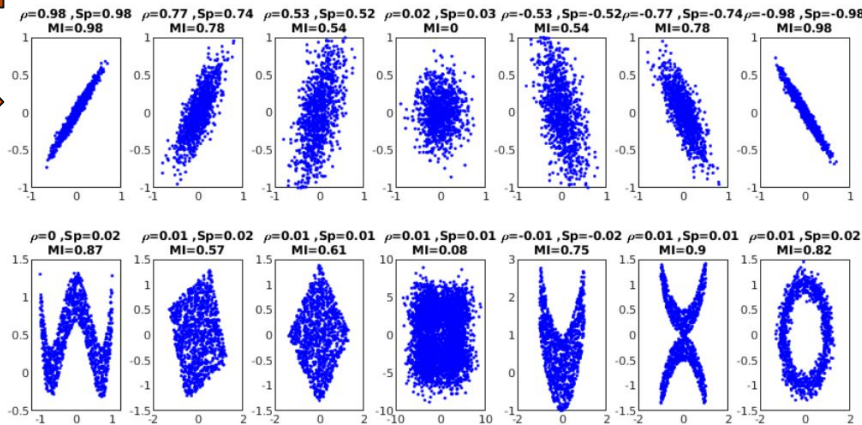
Correlation (Pearson / Spearman)

- Detects **linear** (Pearson) or **monotonic** (Spearman) co-variation.
- The edge has a **sign** (+ / -).
- But correlation also captures **indirect co-variation**

Correlation versus Mutual Information

Mutual Information (MI)

- MI is always positive → the sign is missing.
- However, it's able to detect more complex dependence relationships, including non-linear and non-monotonic patterns.

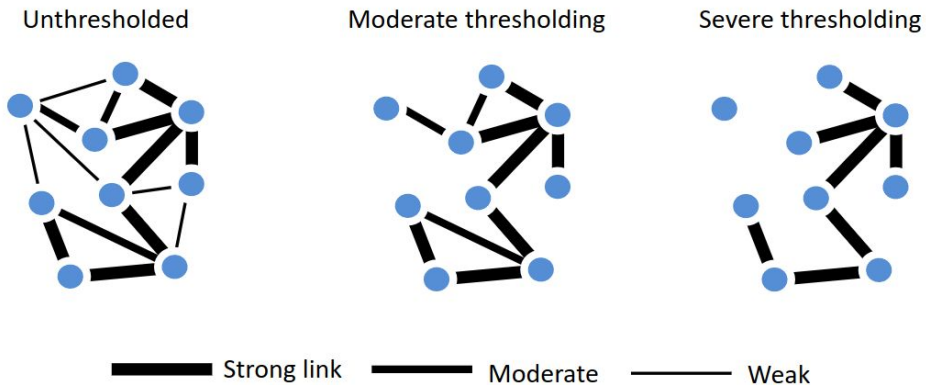


Association networks represent co-variation between genes.
 To identify **direct relationships**, we need to go beyond pairwise co-variation and **consider the gene set jointly.**
Correlation ≠ Causality

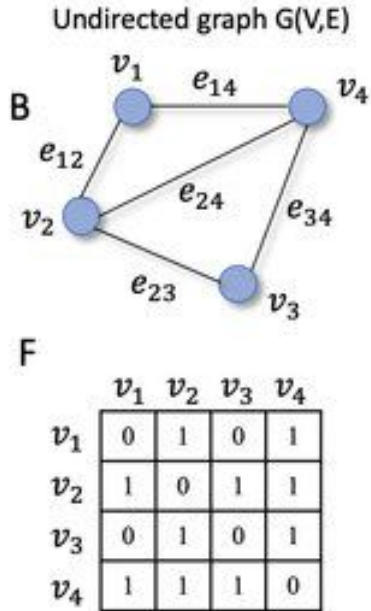
Source 3: Inference from (Omics) data

➤ Often, the similarity/distances/correlations/... are **thresholded**. Calibration enables to:

- Reduce spurious (weak) associations
- Emphasizing topological properties
- Reducing storage burden of large graphs

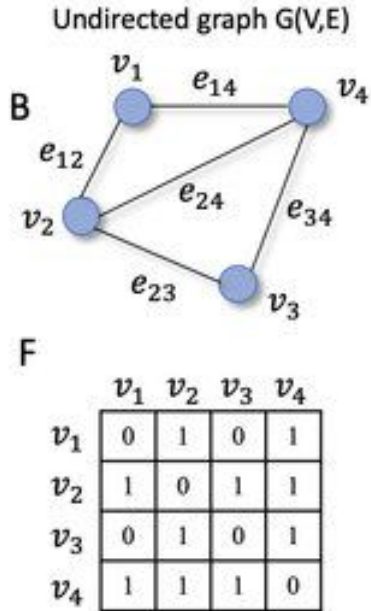


Data structure to store interactions: **Adjacency** matrix

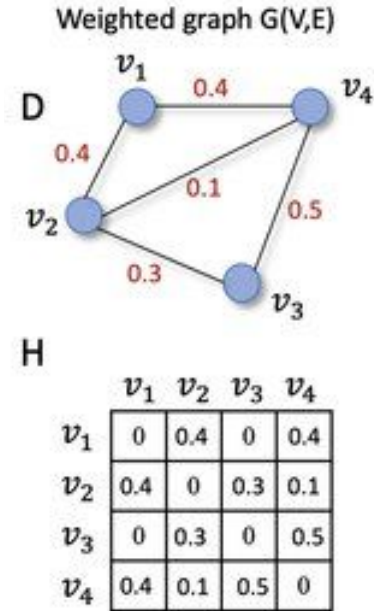


Undirected -> **Symmetric adjacency**

Data structure to store interactions: **Adjacency** matrix



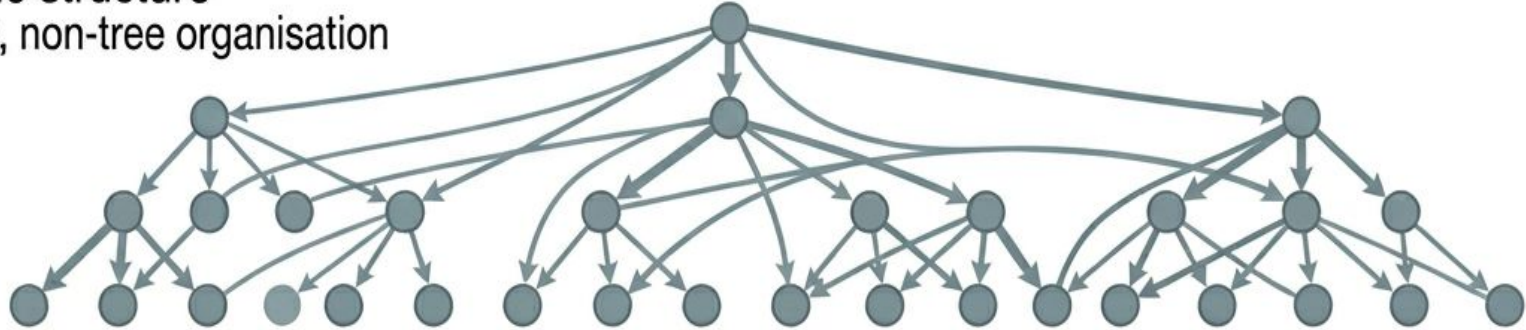
Undirected -> **Symmetric adjacency**



Symmetric matrix, but with weights representing the strength of the interaction

3) Inference of regulatory networks

Directed acyclic structure
directed, acyclic, non-tree organisation



Bayesian networks Table of Contents

1

Probability

Marginal, conditional,
and Bayes theorem

3

Bayesian networks

Factorisation,
d-separation

5

Inference of BNs

Score-based Versus
Constraint-based

Probability reminders

With A, C discrete random variables,

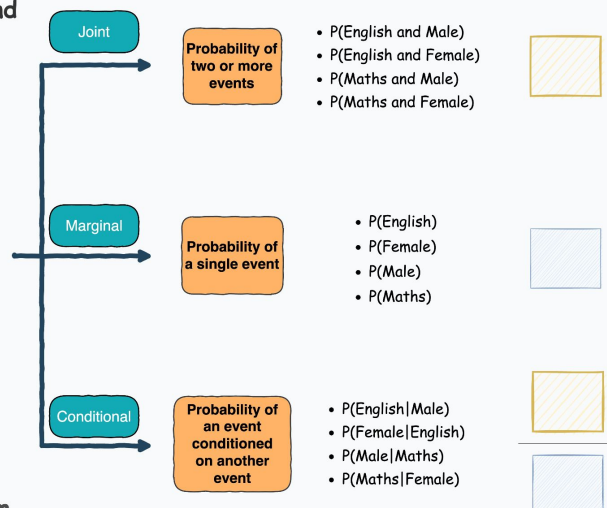
- Marginal Probability aka *sum rule* : $P(A) = \sum_C P(A, C)$
- Conditional Probability aka *product rule* :

$$\underbrace{P(A, C)}_{\text{joint probability}} = \underbrace{P(A|C)}_{\text{conditionnal probability}} P(C)$$

Conditional, Marginal and Joint Probabilities

	Male	Female	
English	0.1	0.25	P(English) 0.35
Maths	0.4	0.25	P(Maths) 0.65
	P(Male) 0.5	P(Female) 0.5	1

Probabilities



- Joint**
 - Probability of two or more events
 - P(English and Male)
 - P(English and Female)
 - P(Maths and Male)
 - P(Maths and Female)
- Marginal**
 - Probability of a single event
 - P(English)
 - P(Female)
 - P(Male)
 - P(Maths)
- Conditional**
 - Probability of an event conditioned on another event
 - P(English|Male)
 - P(Female|English)
 - P(Male|Maths)
 - P(Maths|Female)

DailyDoseofDS.com

- **Marginalisation**, and **conditioning**, are the two core operations enabling to reconstruct any set of probability distributions.
- Extension to the continuous case using **integrals** instead of **sums**.

Probability reminders

Definition (Independence)

A and C are said independent, namely $A \perp\!\!\!\perp C$ iif :

$$P(A, C) = P(A)P(C)$$

Independent events happen when the outcome of the first event does not change the outcomes of the next events.

Dependent events happen when the outcome of the first event changes the likelihood of the outcomes of the next events.



Independence advantages



- Decomposition of intractable joint multivariate distributions into simpler product of marginal terms
 - Faster inference of parameters
 - Straightforward estimation of the mean and variance estimates
- Most machine-learning algorithms assume independence between features

How to expand independence definition?

- In real-life, **full standard independence** is rarely observed -> underlying factors induce statistical dependencies (**flow of information** partially conveyed)
- **Conditional independence** solves this issue, by providing independence conditions after accounting for the effect of the remaining factors

► Definition (Conditional independence)

Let A , B and C be random variables. Then, A and B are said conditionally independent given C , namely $A \perp\!\!\!\perp B | C$ iif :

$$P(A, B | C) = P(A | C)P(B | C)$$

Property

$$A \perp\!\!\!\perp B | C \iff P(A | B, C) = P(A | C)$$

$$A \perp\!\!\!\perp B | C \iff P(A, B, C)P(C) = P(A, C)P(B, C)$$

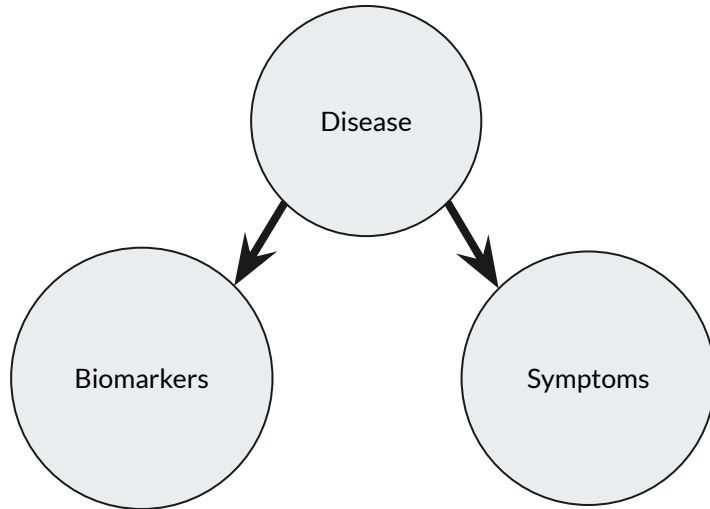
Conditional Independence

How to expand independence definition?

► Definition (Conditional independence)

Let A , B and C be random variables. Then, A and B are said conditionally independent given C , namely $A \perp\!\!\!\perp B \mid C$ iff :

$$P(A, B \mid C) = P(A \mid C)P(B \mid C)$$



In exploratory research, we often try to pair biomarkers with the clinical symptoms

-> But the variations of biomarkers are rarely the core factors that trigger the clinical symptoms

Conditional Independence

Represent Conditional independencies

Definition of independence models

- An **independence model** I over a set V :
 - a set of triples $\langle X, Y \mid Z \rangle$, called **independence relations**
 - X, Y and Z are disjoint subsets of V .
- The independence model I is said **probabilistic**, if it can be represented by a probabilistic distribution, compliant with basic probability rules

$$\langle X, Y \mid Z \rangle \in I \iff X \perp\!\!\!\perp Y \mid Z \text{ w.r.t. } p.$$

Is there any insightful representation that would capture the set of independent clauses?



Represent Conditional independencies

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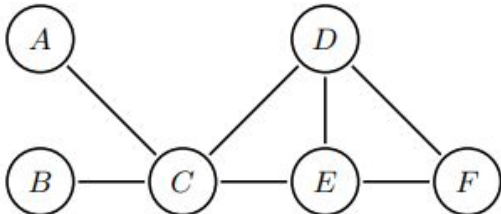
Is there any insightful representation that would capture the set of independent clauses?

Yes, **probabilistic graphical networks**

The two most popular PGMs frameworks

Markov Networks

- Undirected graphs
- Also named Markov **Random fields** -> **GGMs** are a special case of it
- Criteria of independence is based on the ***u*-separation**

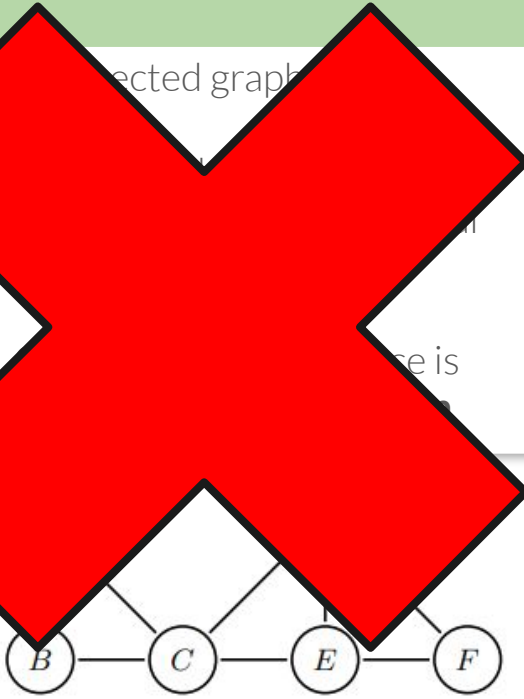


The two most popular PGMs frameworks

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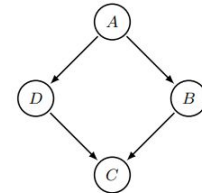
• Undirected graph

• The joint probability distribution is

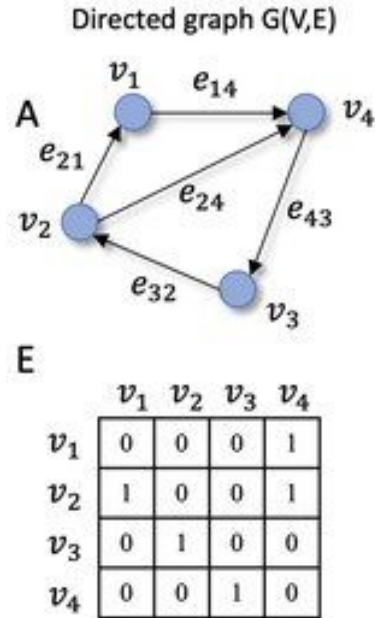


Bayesian Networks

- DAGs (no cycle, but directed)
- Factorises as a probability distribution
- Criteria of independence is based on the **d-separation**



Data structure to store interactions: **Adjacency** matrix



Directed -> **Asymmetric adjacency**

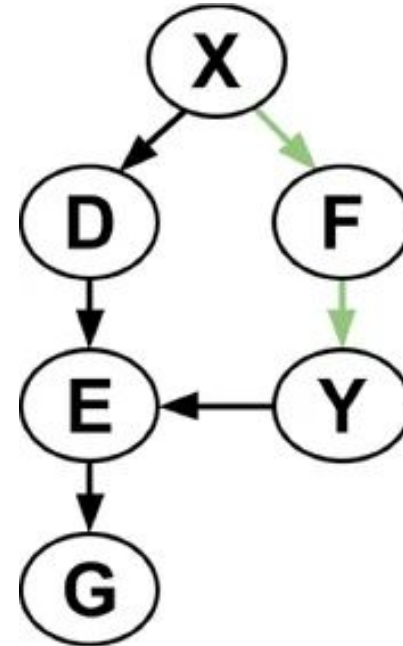
d-separation: Intuitive Interpretation as flow

D-separation for noobs

Consider a path between X and Y + disjoint subset Z:

1. Without conditioning node (Z=empty)
 - a. any intermediate node between X and Y is **open**
 - b. except if the node is a **collider**, or any of its **descendants** -> **in this case, it's closed**

To be independent, all paths between X and Y must be closed (no flux of information).



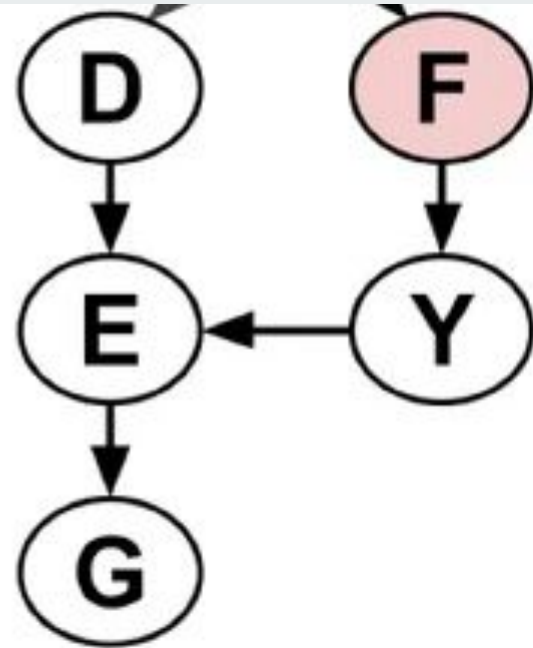
$X \not\perp Y$

D-separation for noobs

Consider a path between X and Y + disjoint subset Z:

1. Without conditioning node:
 - a. any intermediate node between X and Y is **open**
 - b. except if the node is a **collider**, or any of its **descendants** -> **in this case, it's closed**

Z d-separates X and Y if all the paths between X and Y are closed (no flux of information).



Are D and Y independent?

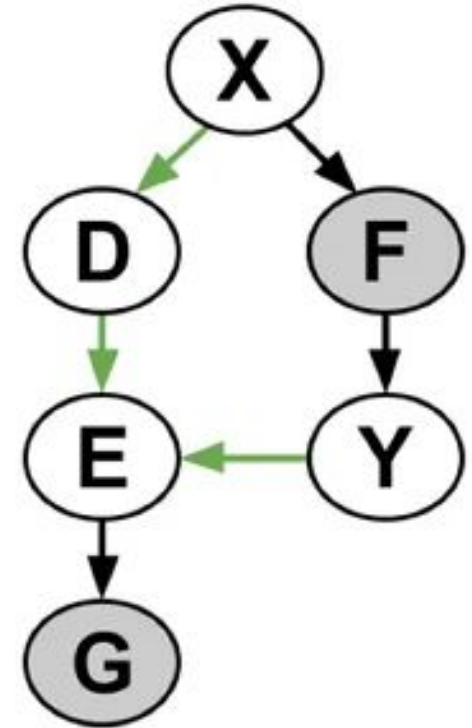
d-separation: Intuitive Interpretation as flow

D-separation for noobs

Consider a path between X and Y + disjoint subset Z:

1. **Conditioning** reverses the flow:
 - a. Open -> close
 - b. Close -> Open

Z d-separates X and Y if all the paths between X and Y are closed (no flux of information).



$$X \perp\!\!\!\perp Y \mid F, G$$

d-separation: Intuitive Interpretation as flow



1. **First misconception:** only interested in direct pairwise interactions -> BNs are interested in modelling higher-order interactions
2. **Second misconception:** The direction of the arrows is irrelevant, except for V-structures
3. **Third misconception:** account for the topological context.
 - a. V-structure are counter-intuitive
 - b. Conditioning on a set of nodes may open paths that used to be closed, and reciprocally

3-node special BNs, and rehearsal



Measure the effect of variation of the **independent variable** X on the **response variable** Y (defined by expert knowledge) that is mediated by a **covariate** Z , with no direct effect of X upon Y .



How many distinct configurations in total can you identify, being DAGs, and with node Z as the intermediate node?

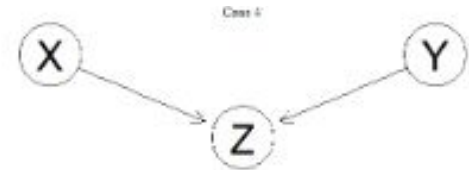
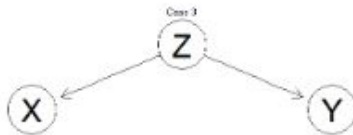
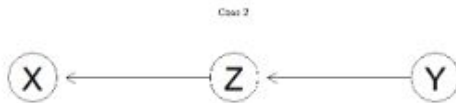
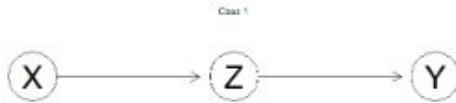
3-node special BNs, and rehearsal



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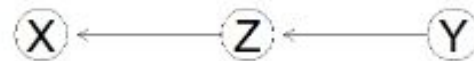
4 distinct configurations can be identified, changing the orientation of edges.



3-node special BNs, and rehearsal

Markov chains

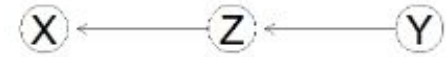
- Subsets of Bayesian networks.
- They model stochastic process, in which the next state depends only on the current state.
- Considering **dynamics**, you may interpret a given node as an observation at time t , and its parent an observation at time $t - 1$, after unrolling the BN.



3-node special BNs: Markov Chains

Exercise: prove the two CIs

- Apply d -separation criterion.
- Apply Bayes theorem, and law of total probabilities



$$X \not\perp\!\!\!\perp Y \mid \emptyset \quad \text{?}$$



D-separation for noobs

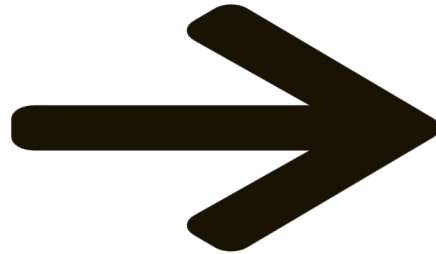
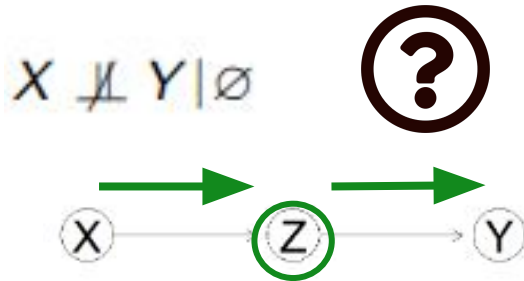
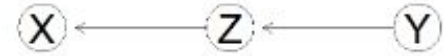
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3-node special BNs: Markov Chains

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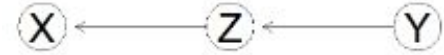
$$\begin{aligned}
 p(y \mid x) &= \frac{p(x,y)}{p(x)} \\
 &= \frac{\sum_z p(x,y,z)}{p(x)} \\
 &= \frac{p(x)}{p(x)} \sum_z p(z \mid x) p(y \mid z) \\
 &\neq p(y)
 \end{aligned}$$

3-node special BNs: Markov Chains

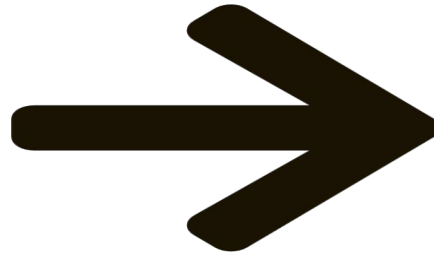
Exercise: prove the two CIs



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$$X \perp\!\!\!\perp Y | Z$$

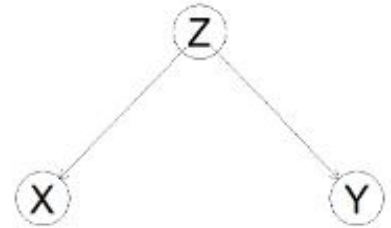


$$\begin{aligned}
 p(x, y | z) &= \frac{p(x, y, z)}{p(z)} \\
 &= \frac{p(z)p(y|z)p(x|z)}{p(z)} \\
 &= p(y | z)p(x | z)
 \end{aligned}$$

3-node special BNs: Markov Chains

Confounder

- Z is a **latent cause**, that must be controlled
- If not observed, that may wrongly leads statisticians into setting up a spurious correlation between X and Y.



Exercise: prove the two CIs

- Apply *d*-separation criterion.
- Apply Bayes theorem, and law of total probabilities



$$X \not\perp\!\!\!\perp Y \mid \emptyset$$



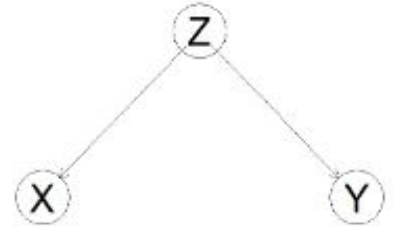
$$X \perp\!\!\!\perp Y \mid Z$$



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$$X \not\perp\!\!\!\perp Y | \emptyset$$



$$\begin{aligned}
 p(x, y) &= \sum_z p(x, y, z) \\
 &= \sum_z p(x | z) p(y | z) \\
 &\neq p(x) p(y)
 \end{aligned}$$

$$X \perp\!\!\!\perp Y | Z$$



$$\begin{aligned}
 p(x, y | z) &= \frac{p(x, y, z)}{p(z)} \\
 &= \frac{p(z) p(y | z) p(x | z)}{p(z)} \\
 &= p(y | z) p(x | z)
 \end{aligned}$$

V-structure (aka the least intuitive)

- Z is a **collider** -> **different strategy**
 - You should not control for it, as it may induce spurious correlation
 - Related to selection bias, and Simpson's paradox
- Used for **XOR** encoding, such as genes activation, or toggle switch.



Exercise: prove the two CIs

- Apply *d*-separation criterion.
- Apply Bayes theorem, and law of total probabilities



$$X \perp\!\!\!\perp Y \mid \emptyset$$



$$X \not\perp\!\!\!\perp Y \mid Z$$



3-node special BNs: Markov Chains



Exercise: prove the two CIs

- Apply d -separation criterion.
- Apply Bayes theorem, and law of total probabilities



V-structure (aka the least intuitive)

$$X \perp\!\!\!\perp Y \mid \emptyset$$



$$\begin{aligned}
 p(x, y) &= \sum_z p(x, y, z) \\
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 &\neq p(x \mid z)p(y \mid z)
 \end{aligned}$$

Datasaurus toy model

Visual depiction of V-structure



Always visualise the distribution of your datasets:

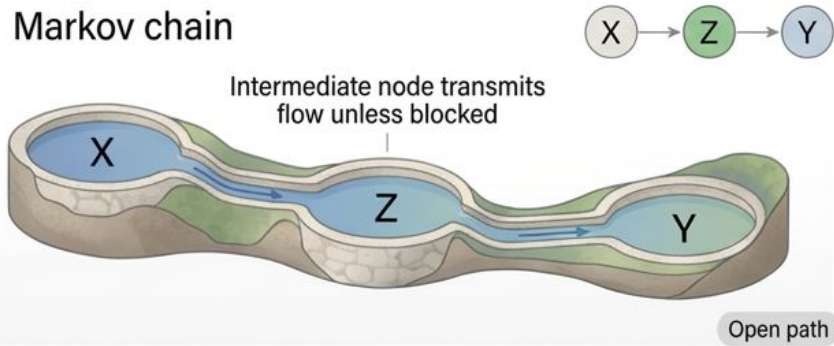
- Datasaurus: similar descriptive statistics
- But complete distinct distributions (visually easy to discriminate)

V-structures can unravel hidden dependencies.

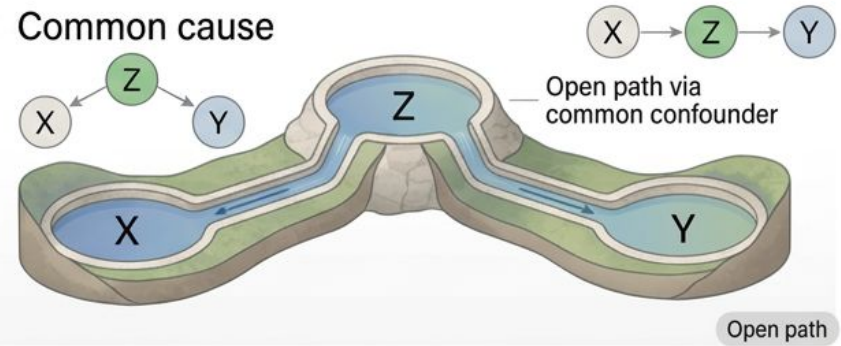
Add a **latent categorical** variable Z for each cloud of points
will reveal an underlying connection between X and Y .

A metaphor of conditional dependencies

a Markov chain

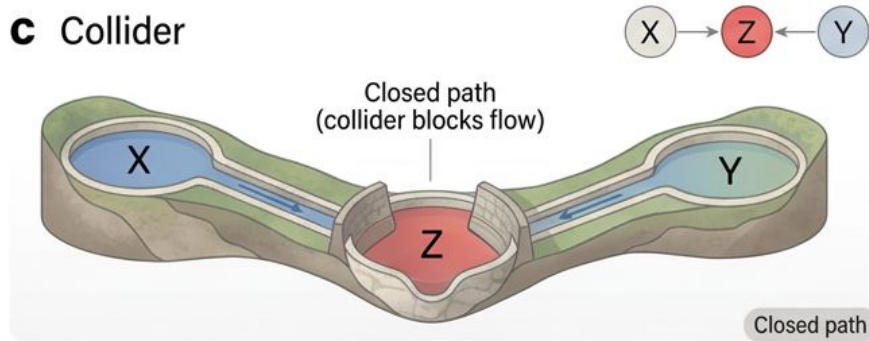


b Common cause

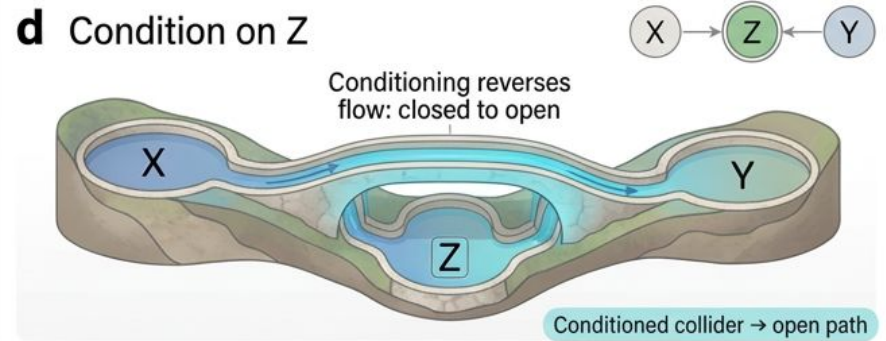


A metaphor of conditional dependencies

c Collider



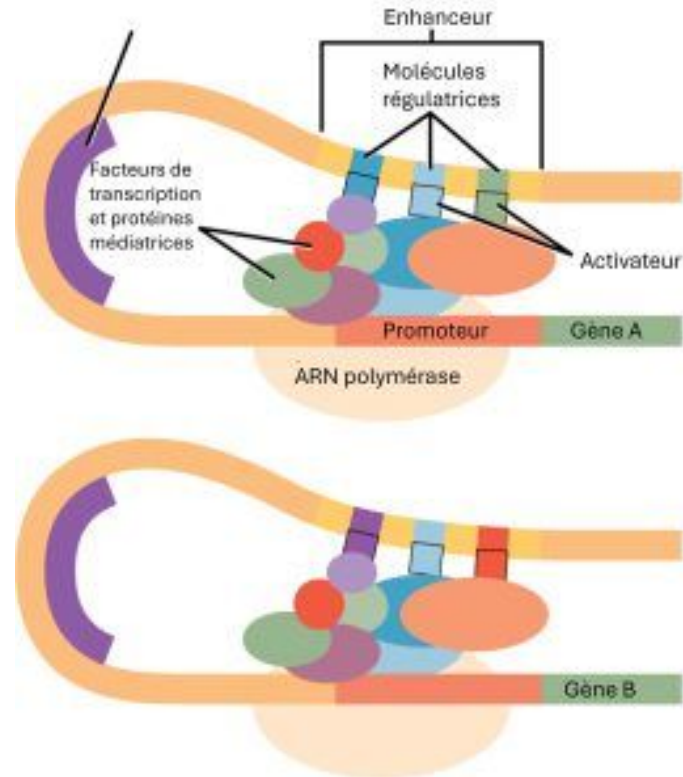
d Condition on Z



Z d-separates X and Y when all paths between them are closed (no information flow).
Conditioning can reverse path states: open paths may close, and colliders may open.

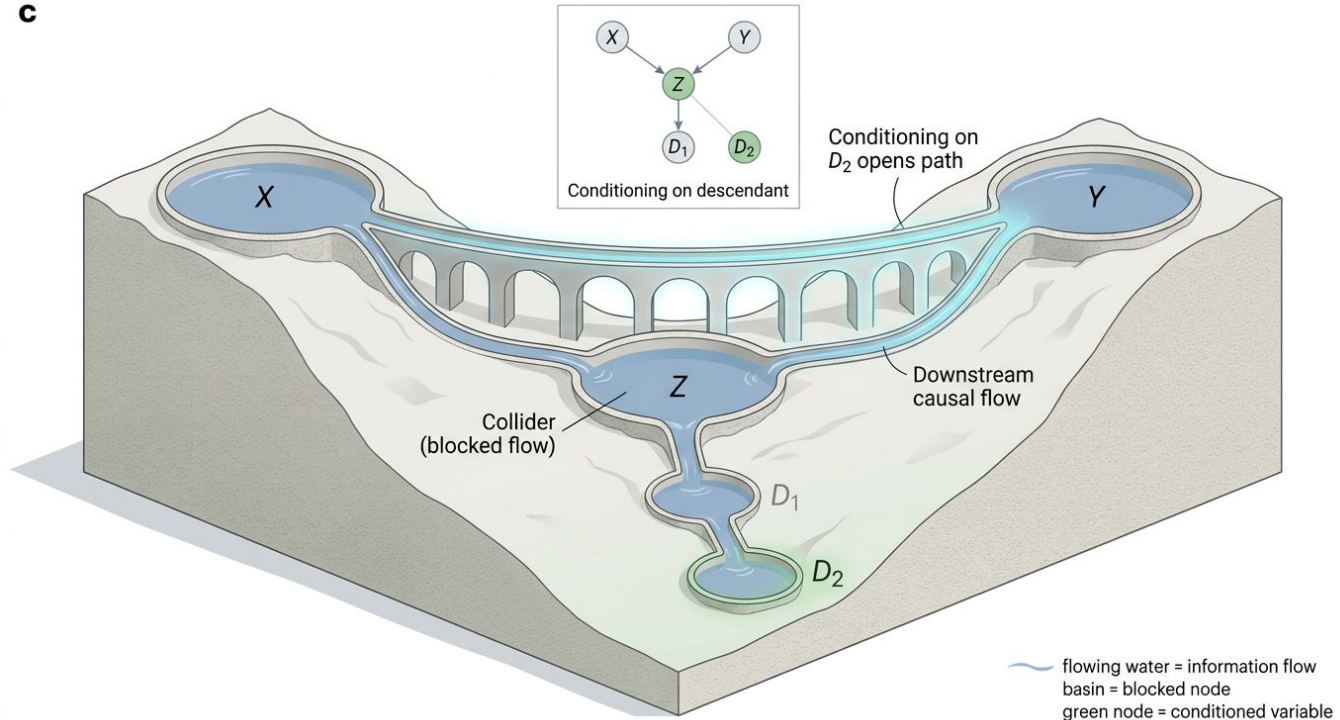
■ blue flowing water = information flow
■ blocked basin / dam = closed path
■ highlighted channel / gate / aqueduct = conditioning
■ DAG node Z (green: path open / red: path closed)

V-structure as complexes of transcription factors



Descendants can help in unravelling complex mechanistic interactions

c



Markov Blanket, and Boundary

▶ Definition (Markov blanket and boundary)

A Markov blanket of X in V is a subset $M \subseteq (V \setminus X)$ such that $X \perp\!\!\!\perp V \setminus (X \cup M) \mid M$. A Markov boundary MB is the optimal Markov blanket (no subset can be found into it).

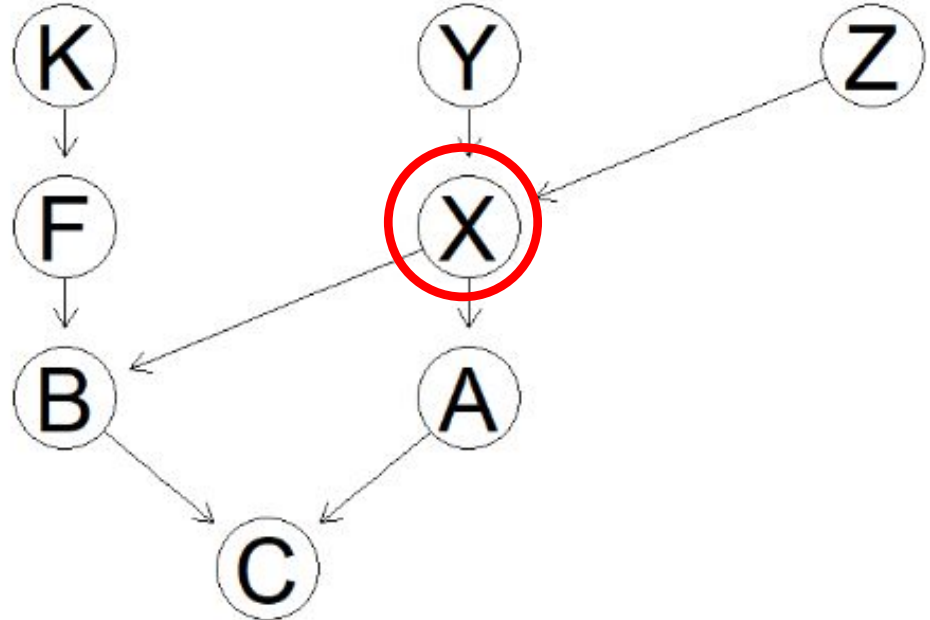
With:

- V_x the **neighbours** of X (namely, its direct parents, and children)
- SP_x the **spouses** of X (nodes sharing the same children)

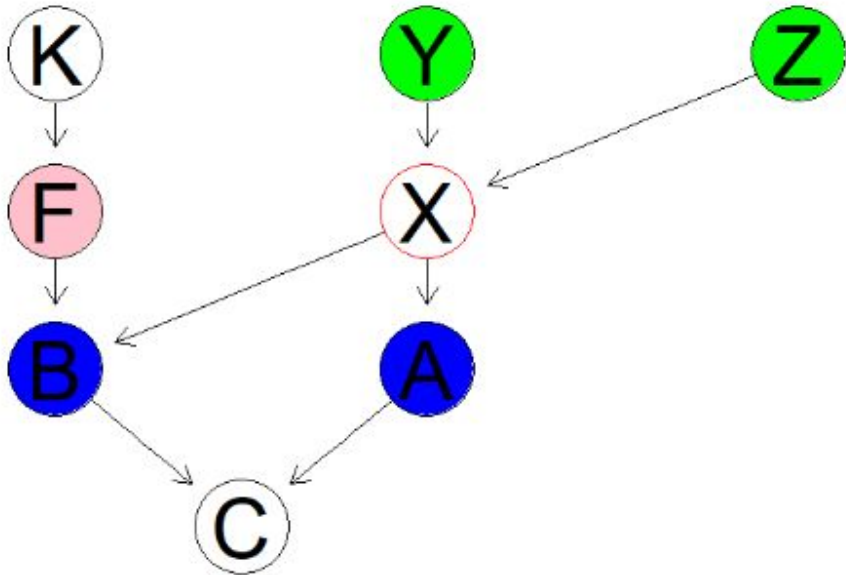
Markov Boundary: a biological application



Find the **Markov boundary** of node **X**.



Markov Boundary: a biological application

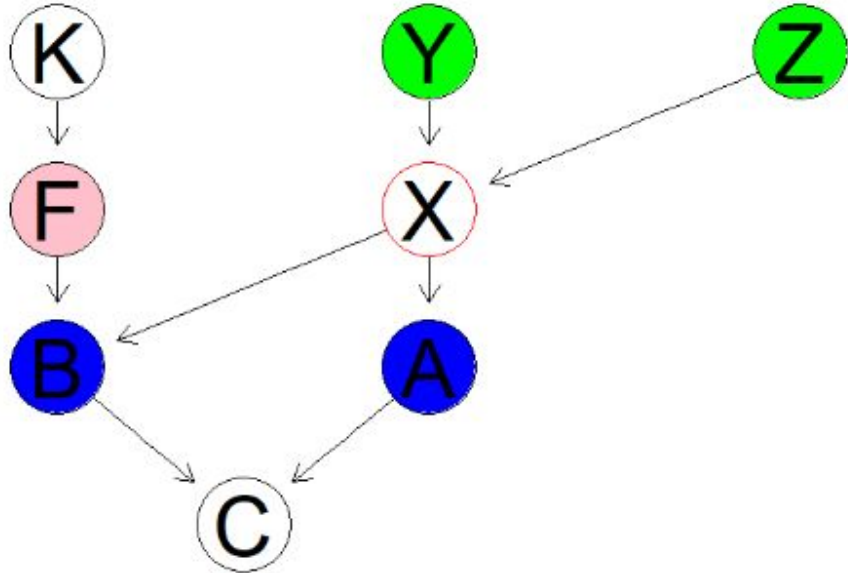


Solutions:

- a **Markov blanket** of node X

Find back the legend: what are the **spouses, children, and parents** of node X?

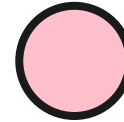
Markov Boundary: a biological application



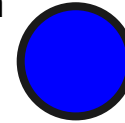
Solutions:

- Which are the kinship relationships of X?

- spouses



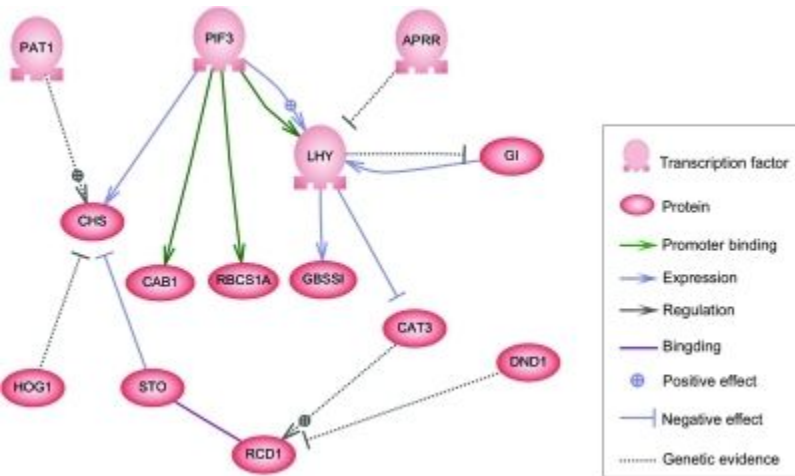
- children



- parents



Markov Boundary: a biological application



In GRNs, the **Markov boundary** is the *smallest set of other genes* you need to look at to predict its behavior.

Example: to try to predict whether a gene is “on” or “off”, instead of looking at *all* genes in the network, you only need to look at the genes covered by the **Markov boundary**, namely its:

1. **Direct regulators**, the parents, such as the **transcription factors**
2. The Direct downstream targets (children) **AND**
3. **Co-regulators** (spouses), aka the other genes that regulate the same targets as G (for example, **operons**) -> this information requires *V-structure* conditional structure

Bibliography



Books

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- Richard E. Neapolitan. *Learning Bayesian Networks* (2019). Pearson
- Koller, Daphne, and Nir Friedman. *Probabilistic Graphical Models*. MIT Press, 2009.



Packages

- [bnlearn](#) for BN inference with R
- [PyAgrum](#) for BN Inference with Python



Slides

- Alexandre Aussem on [Probabilistic Graphical Models](#) (Markov + Bayesian networks)
- Marco Scutari on [Understanding Bayesian Networks with Examples in R](#)



Biological applications

- Yupeng Li Naim, Yushi Liu (2019). *A Bayesian gene network reveals insight into the JAK-STAT pathway in systemic lupus erythematosus*. Plos One.
- Louis Verny and Hervé Isambert (2017). *Learning causal networks with latent variables from multivariate information in genomic data*. Plos Computational Biology

Acknowledgments



Alexandre Aussem

Hybrid-based BN inference



Pierre Henri Willemin

PyAgrum developer



Herve Isambert

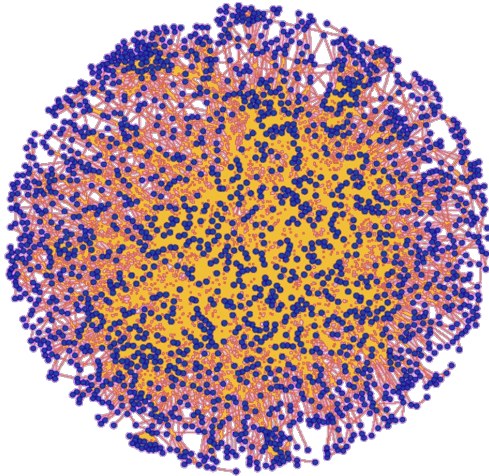
Curie's MIIC developer



Marco Scutari

Core bnlearn developer

Outline



Source: <https://www3.nd.edu/~tmilenko/research.html>.

General Introduction, Key Concepts

Network Biology, Network Science, Complex Systems, ...

Network Construction/Inference

Data sources, Distances/Similarities, Correlation, ...

Network Analysis

Measures

Degree, Centrality, Distances, ...

Algorithms

Diffusion, Clustering, Embedding, ...

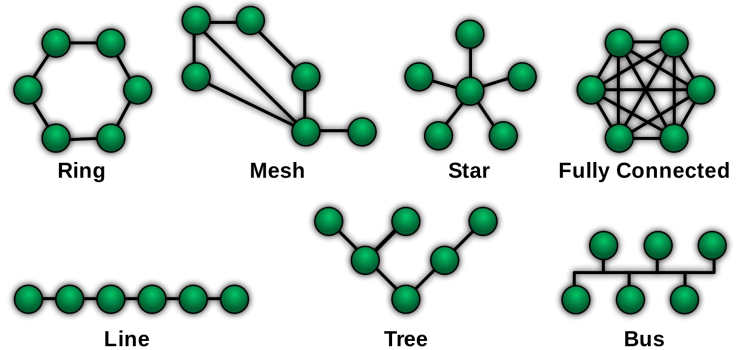
Networks and Integration

Multiplex Networks, Multilayer Networks, Knowledge Graphs, ...

Studying Network **Topology**

➤ **Topology** is the way in which the **nodes and the edges are arranged** within a network.

- Robustness of a network
- Hub nodes
- Essential nodes
- Paths/accessibility
- Communities
-



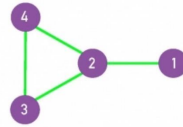
Source: "Network Topology." In Wikipedia, August 30, 2023.

https://en.wikipedia.org/w/index.php?title=Network_topology&oldid=1172927659.

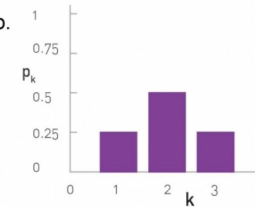
Metrics in network analysis: **Node Degree**

- The **degree of a node** in a network is the **number of edges that are incident to the node**.
- Observing the **degree distribution** of a network can reveal interesting properties:
 - Overall connectivity

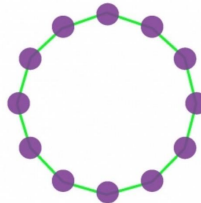
a.



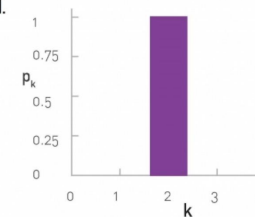
b.



c.



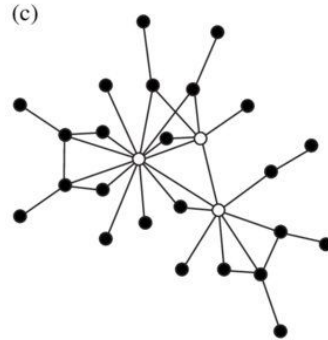
d.



Source: Courtesy of Anaïs Baudot

Metrics in network analysis: **Node Degree**

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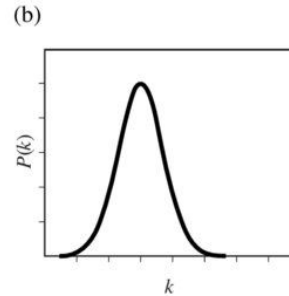
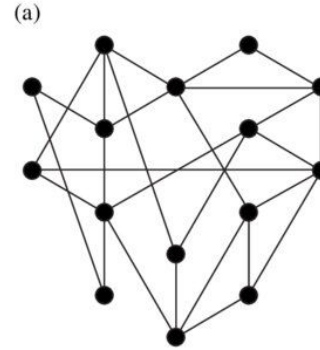
Source: Bentley, Barry. "Connectomics of Extrasynaptic Signalling: Applications to the Nervous System of *Caenorhabditis Elegans*," 2017. <https://doi.org/10.17863/CAM.16873>.

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 - **Scale-free** property

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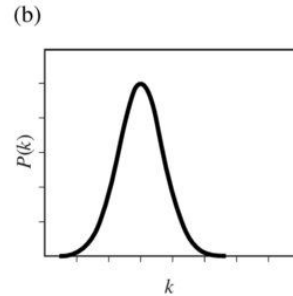
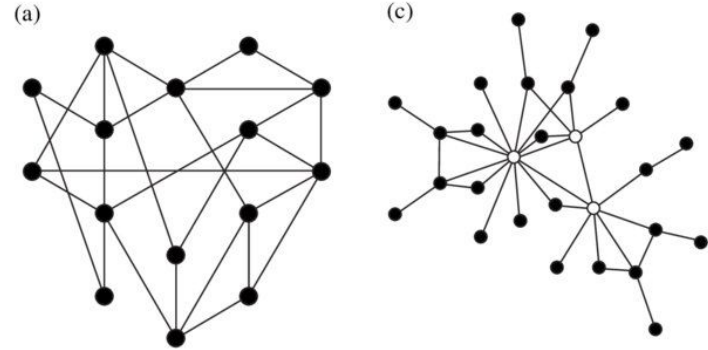
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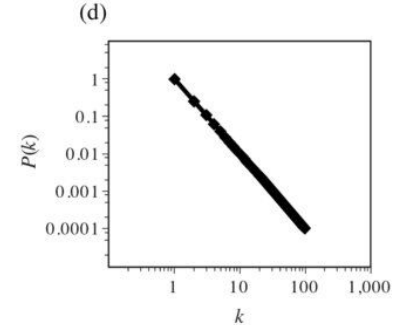
Random Network

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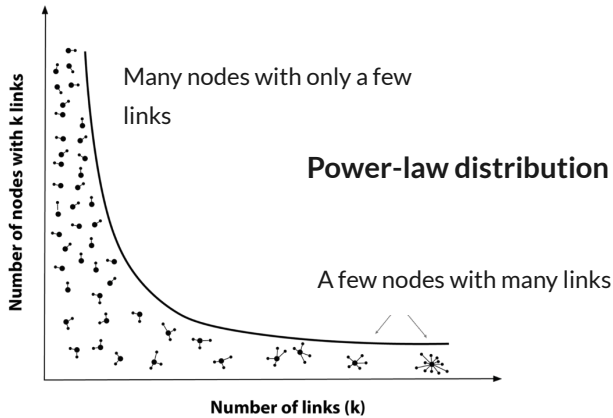
Random Network



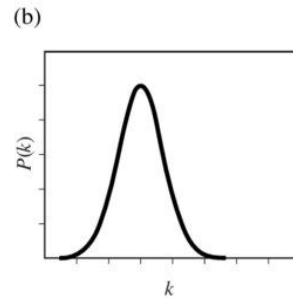
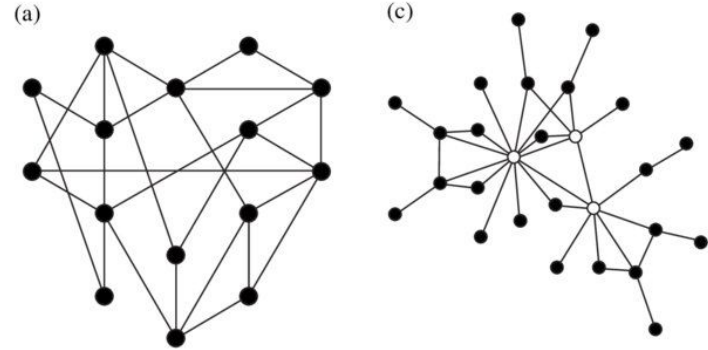
Scale-free Network
(plot in log-log scale)

Metrics in network analysis: Node Degree

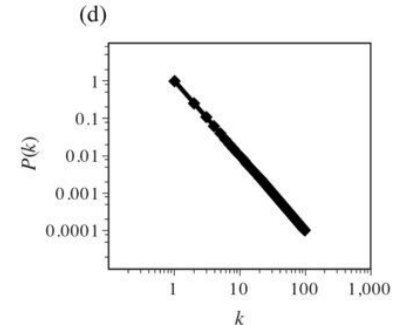
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Source: nestl . "The Rise of the Platform Economy." Accessed August 28, 2023.
<https://www.nesta.org.uk/blog/rise-platform-economy/>.



Random Network

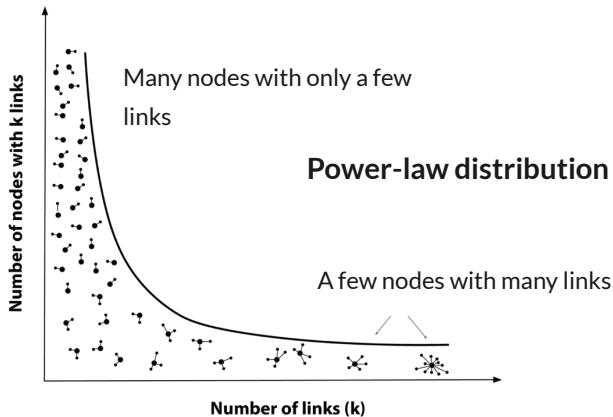


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 - **Scale-free** property



- Biological interpretation ?
 - Growth with preferential attachment (“rich get richer”) -> hub nodes
 - Robust to random attack, sensitive to targeted attacks

Are biological networks scale-free ?

Scale-Freeness and Biological Networks

Get access >

Masanori Arita ✉

The Journal of Biochemistry, Volume 138, Issue 1, Jul. 2005, Pages 1–4,

<https://doi.org/10.1093/jb/mvi094>

Published: 01 July 2005 Article history ▾

COMMENTARY | 01 NOVEMBER 2005

Scale-free networks in cell biology FREE

In collection: Metabolism

Réka Albert

+ Author and article information

J Cell Sci (2005) 118 (21): 4947–4957.

<https://doi.org/10.1242/jcs.02714>

> *J Comput Biol.* 2006 Apr;13(3):810-8. doi: 10.1089/cmb.2006.13.810.

- PPI
- Metabolic networks
- Regulatory networks

How scale-free are biological networks

Raya Khanin ¹, Ernst Wit

Affiliations + expand

PMID: 16706727 DOI: [10.1089/cmb.2006.13.810](https://doi.org/10.1089/cmb.2006.13.810)

Are biological networks scale-free ? A debate!

Scale-Freeness and Biological Networks

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The Journal of Biochemistry, Volume 138, Issue 1, Jul. 2005, Pages 1–4,

<https://doi.org/10.1093/jb/mvi094>

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COMMENTARY | 01 NOVEMBER 2005

Scale-free networks in cell biology FREE

In collection: Metabolism

Réka Albert

+ Author and article information

J Cell Sci (2005) 118 (21): 4947–4957.

<https://doi.org/10.1242/jcs.02714>

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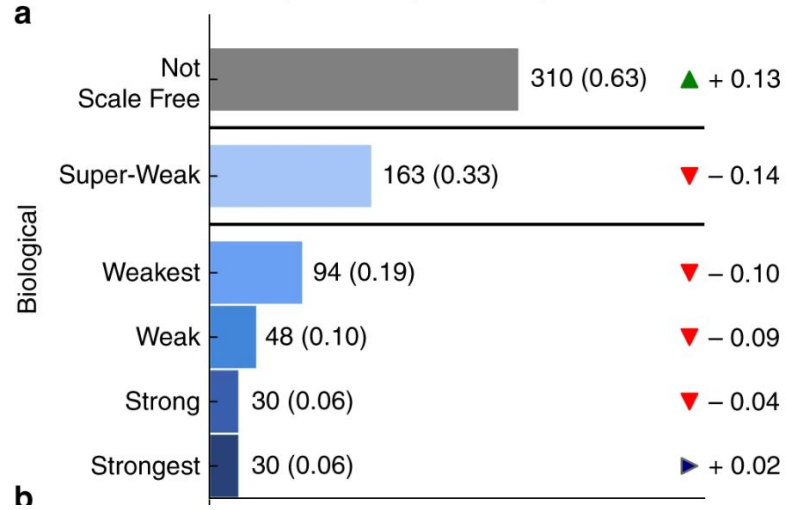
Article | [Open Access](#) | Published: 04 March 2019

Scale-free networks are rare

Anna D. Broido ✉ & Aaron Clauset ✉

Nature Communications 10, Article number: 1017 (2019) | [Cite this article](#)

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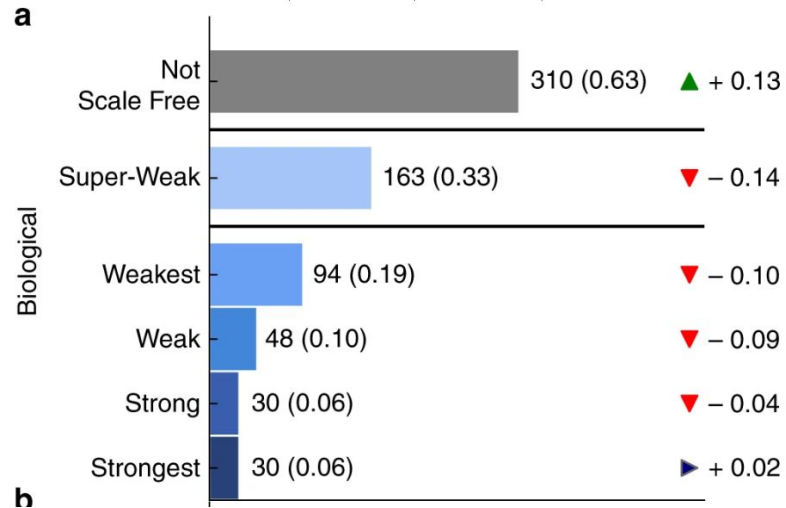
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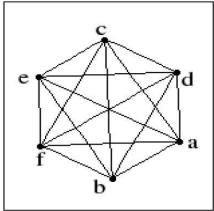
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- In practice, when inferring molecular networks (especially co-expression networks), **researchers often aim to obtain scale-free networks!** You'll do it yourself in the WGCNA hands-on!

Metrics in network analysis: **Density**

- The **density** of a network is the **ratio of the number of edges** with respect to the **maximum possible number of edges** (i.e. the number of edges if the network was **complete**).



Graphe complet K_n

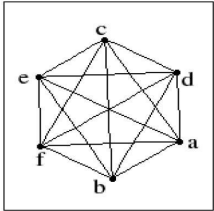
$$D(G) = \frac{|E|}{|E|_{K_n}}$$

$$D_G = 0 \Leftrightarrow |E| = 0$$

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- Are biological networks **dense** or **sparse**?

[Mol Syst Biol.](#) 2008; 4: 213.

Published online 2008 Aug 5. doi: [10.1038/msb.2008.52](https://doi.org/10.1038/msb.2008.52)

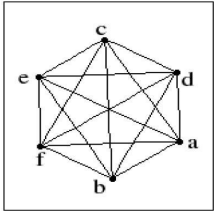
Survival of the sparsest: robust gene networks are parsimonious

[Robert D Leclerc](#)^{1,a}

“**Robustness** implies a parsimonious network structure that is sparsely connected and not unnecessarily complex”

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Source: Courtesy of Anaïs Baudot

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Explorability and the origin of network sparsity in living systems

[Daniel M. Busiello](#), [Samir Suweis](#), [Jorge Hidalgo](#) & [Amos Maritan](#) 

[Scientific Reports](#) 7, Article number: 12323 (2017) | [Cite this article](#)

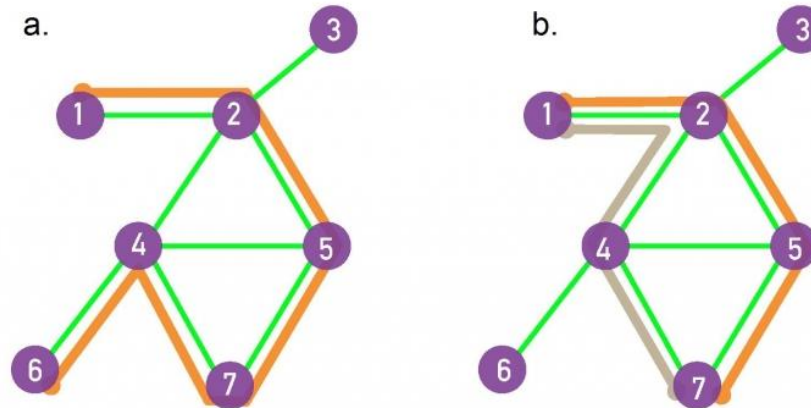
2428 Accesses | 23 Citations | 39 Altmetric | [Metrics](#)

“**Robustness** implies a parsimonious network structure that is sparsely connected and not unnecessarily complex”

“We show that sparsity is an emergent property resulting from optimising both **explorability and dynamical robustness**, i.e. the capacity of the system to remain stable after perturbations of the underlying dynamics”

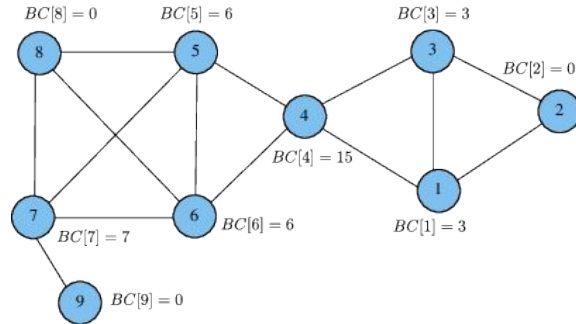
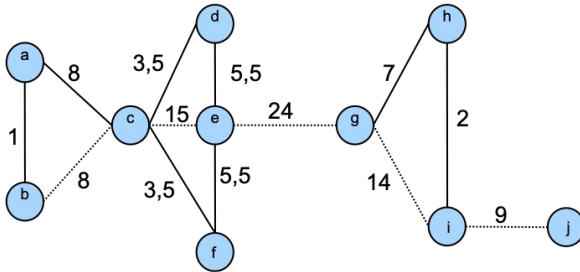
Metrics in network analysis: Distances and paths

- A **path** is a **sequence of edges** which join a sequence of nodes
- The **distance** between two nodes in a network is the **length** (i.e. number of edges) of the **shortest path** connecting them.
- The **diameter** of a network is the **greatest distance between any pair of nodes** in the network.



Metrics in network analysis: **Betweenness**

- The **edge betweenness** is the **number of shortest path** running through an edge
- The **node betweenness** is the **number of shortest path** running through a node
- High edge/node betweenness -> “**bottleneck**”



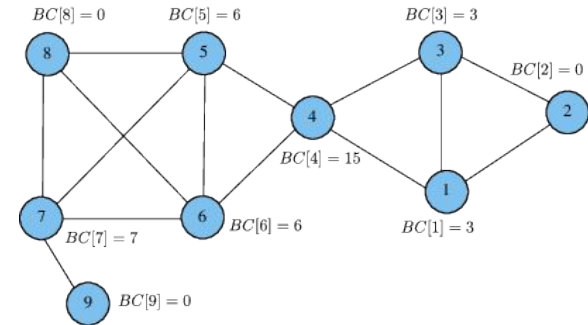
Source: Courtesy of Anaïs Baudot

Metrics in network analysis: **Betweenness**

The Importance of Bottlenecks in Protein Networks: Correlation with Gene Essentiality and Expression Dynamics

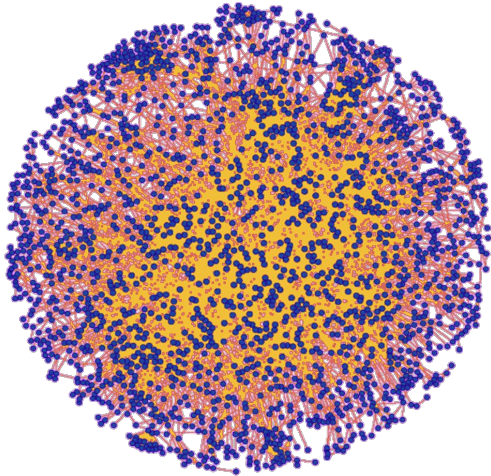
Haiyuan Yu , Philip M Kim , Emmett Sprecher, Valery Trifonov, Mark Gerstein 

Published: April 20, 2007 • <https://doi.org/10.1371/journal.pcbi.0030059>



- Bottleneck proteins are **more likely to be essential proteins**.
- Bottleneck-ness (betweenness) is a much more **significant indicator of essentiality** than hub-ness (degree).
- Bottleneck proteins are significantly less well coexpressed with their neighbors -> **the network's topology is intricately linked with the dynamics of gene expression**.

Outline



Source: <https://www3.nd.edu/~tmilenko/research.html>.

General Introduction, Key Concepts

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Data sources, Distances/Similarities, Correlation, ...

Network Analysis

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Degree, Centrality, Distances, ...

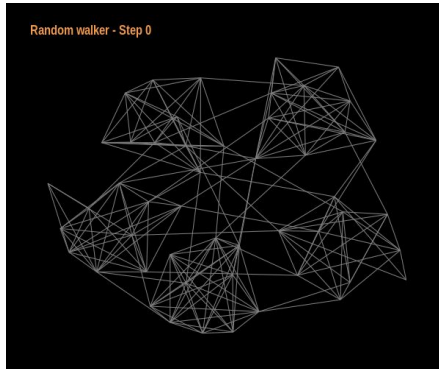
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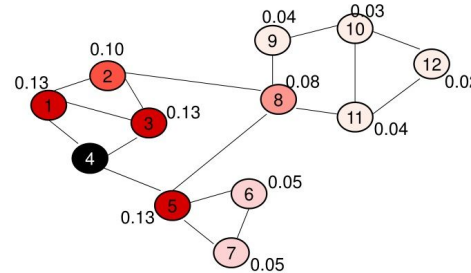
Multiplex Networks, Multilayer Networks, Knowledge Graphs, ...

Algorithms for network analysis: **Random Walk with Restart**



Source: "Script to Animate the Path of a Random Walk across a Graph - A Walker Starts at a Node and Takes Random Steps through the Graph, Tending to Get 'Stuck' in Dense Subgraphs." Gist. Accessed August 29, 2023 <https://gist.github.com/clairemwhite/7fb348acca2c84c464d751ba38ce72e1>.

- State of the art “**guilt-by-association**” approach
- Similarity between a **seed node** and all other nodes in the network
- Used for node prioritisation, network clustering, network embedding, etc...



Nearby nodes, higher scores
More red, more relevant

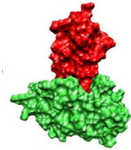
	Node 4
Node 1	0.13
Node 2	0.10
Node 3	0.13
Node 4	0.22
Node 5	0.13
Node 6	0.05
Node 7	0.05
Node 8	0.08
Node 9	0.04
Node 10	0.03
Node 11	0.04
Node 12	0.02

Ranking vector

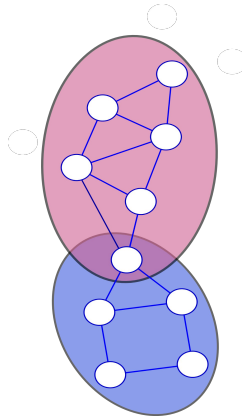
\vec{r}_4

Source: Fast Random Walk with Restart and Its Applications. Hanghang Tong, Christos Faloutsos and Jia-Yu (Tim) Pan. ICDM 2006 Dec. 18-22, HongKong

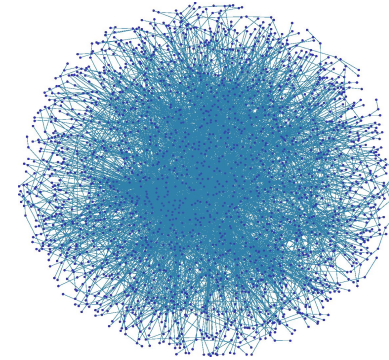
Algorithms for network analysis: **Community detection**



Binary interaction



Functional modules



Interaction Networks

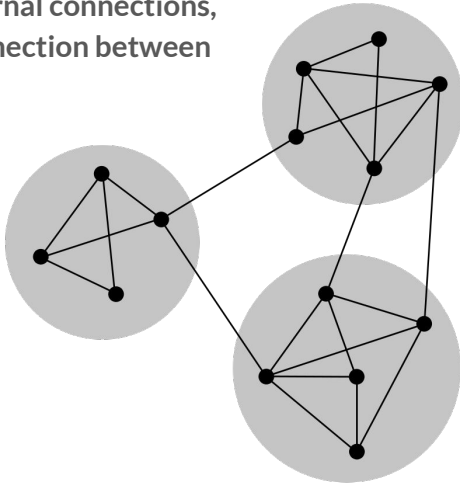
Precision

Comprehensiveness

Algorithms for network analysis: **Community detection**

- Community detection = **clustering** for networks!
- Find groups of nodes (**communities/modules/clusters**) that are **more similar to each other than to the other nodes**

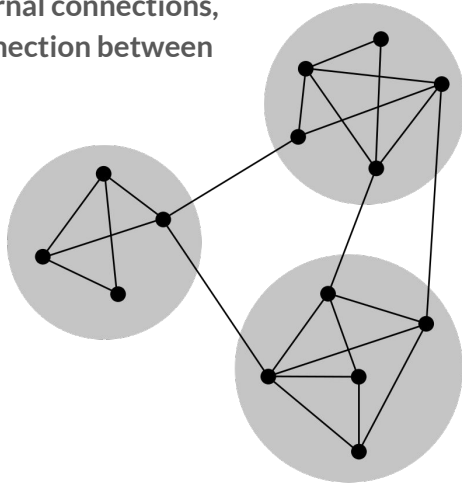
Dense internal connections,
sparse connection between
groups



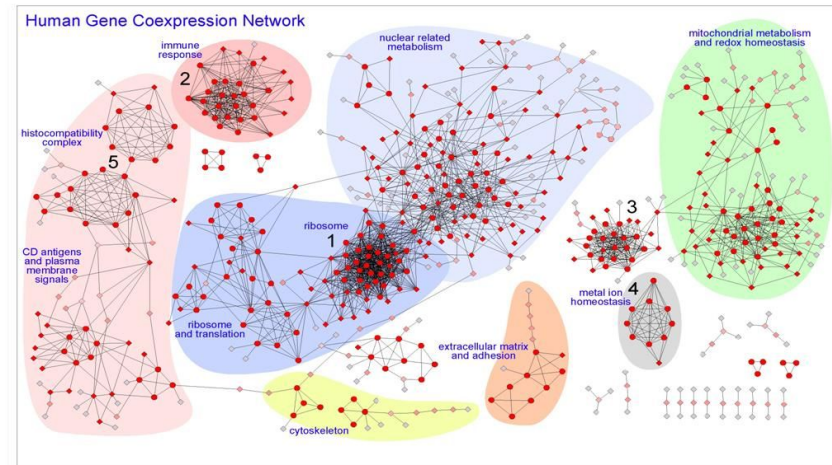
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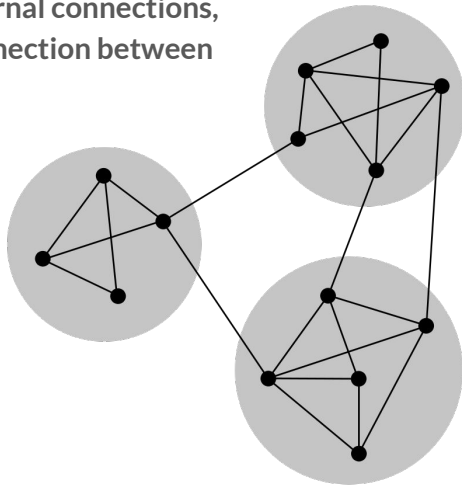
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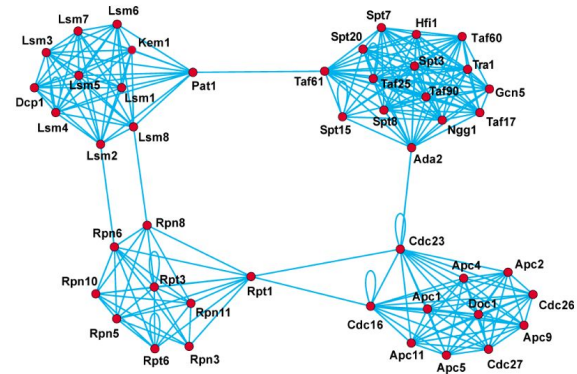
Dense internal connections,
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Source: "Community Structure." In Wikipedia, August 26, 2023.

Why performing Community detection in biological networks ?

● Protein complexes in a PPI network

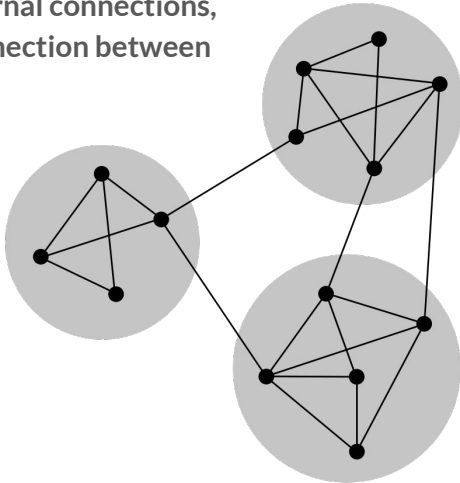


Source: Ngom, Dr Alioune. "NETWORK CLUSTERING METHODS," n.d.

Algorithms for network analysis: **Community detection**

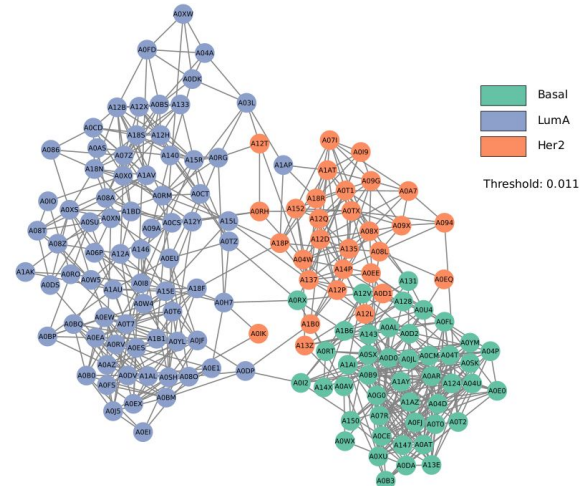
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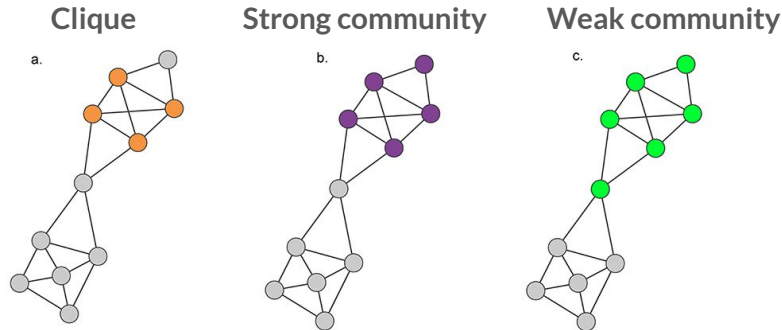


Source: Morgane Térézol - SNF tutorial

Algorithms for network analysis: **Community detection**

➤ **Clique-based** methods (e.g. CliquePercolation)

Cliques are **complete subgraphs**.

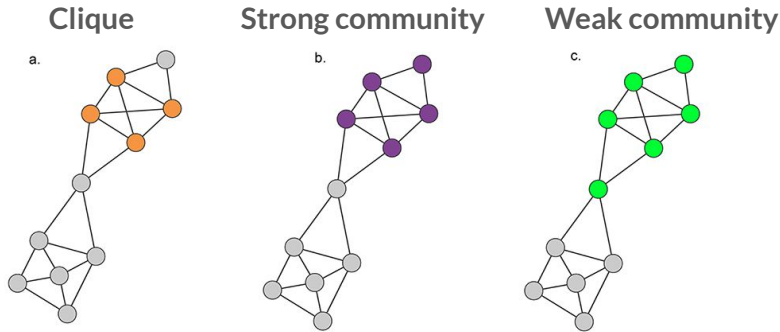


Source: Network Science by Albert-László Barabási. Accessed August 29, 2023.
<http://networksciencebook.com/>.

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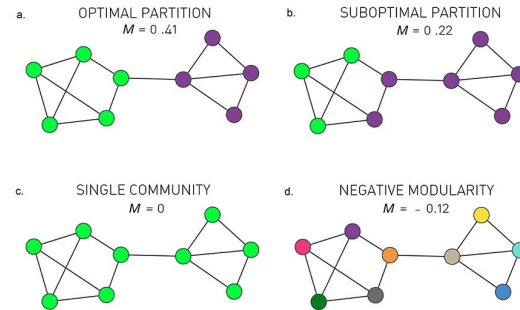
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➤ **Modularity** optimisation (e.g. Louvain Algorithm)

How much more **densely connected** the nodes within a community are, compared to how connected they would be in a random network.

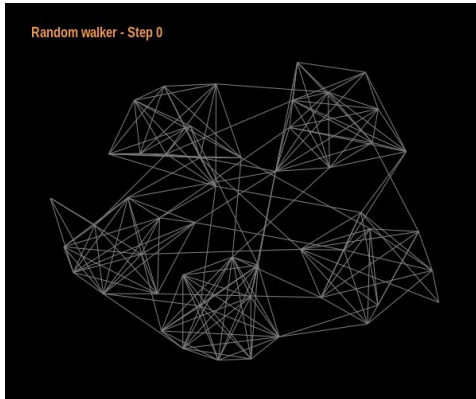


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Algorithms for network analysis: **Community detection**

➤ **Random-Walk based methods** (e.g. Walktrap)

Random walks on a graph tend to get **“trapped” into densely connected parts** corresponding to communities.



➤ **and many other...**

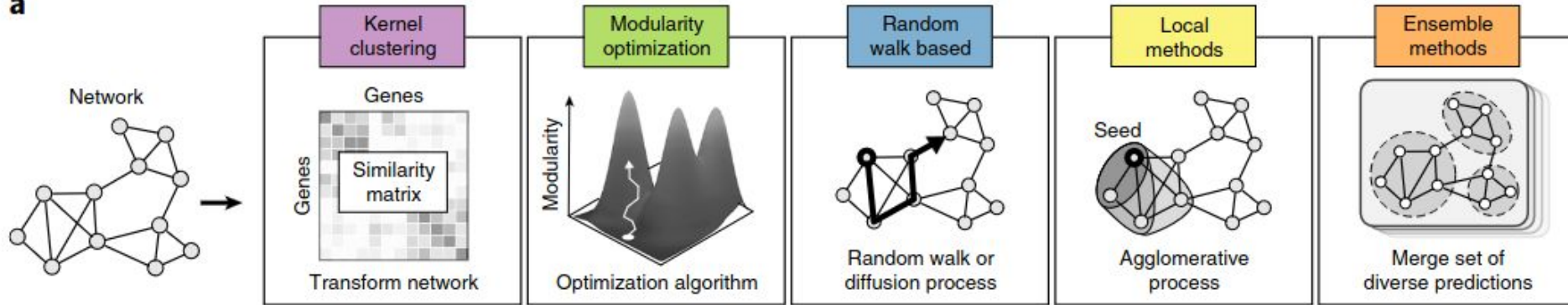
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Algorithms for network analysis: **Community detection**

a



Analysis | [Open Access](#) | [Published: 30 August 2019](#)

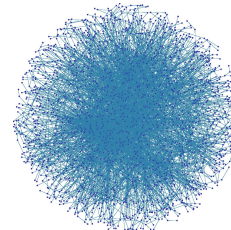
Assessment of network module identification across complex diseases

[Sarvenaz Choobdar](#), [Mehmet E. Ahsen](#), [Jake Crawford](#), [Mattia Tomasoni](#), [Tao Fang](#), [David Lamparter](#),
[Junyuan Lin](#), [Benjamin Hescott](#), [Xiaozhe Hu](#), [Johnathan Mercer](#), [Ted Natoli](#), [Rajiv Narayan](#), [The DREAM](#)
[Module Identification Challenge Consortium](#), [Aravind Subramanian](#), [Jitao D. Zhang](#), [Gustavo Stolovitzky](#),
[Zoltán Kutalik](#), [Kasper Lage](#), [Donna K. Slonim](#), [Julio Saez-Rodriguez](#), [Lenore J. Cowen](#), [Sven Bergmann](#) ✉
 & [Daniel Marbach](#) ✉

Nature Methods 16, 843–852 (2019) | [Cite this article](#)

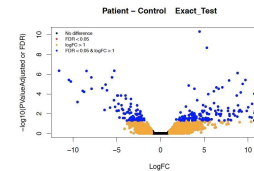
Algorithms for network analysis: **Active Modules**

Biological Network

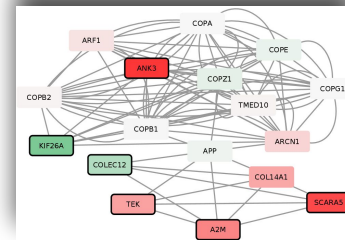


+

RNA-seq transcriptomics data



Find subnetworks of interest
aka “active modules”

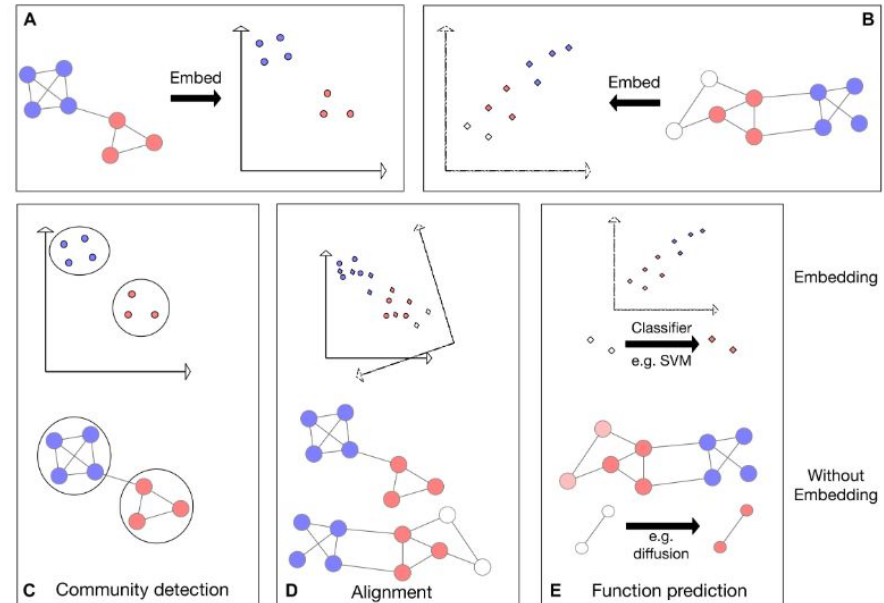


Source: Courtesy of Anaïs Baudot

Algorithms for network analysis: **Network Embedding**

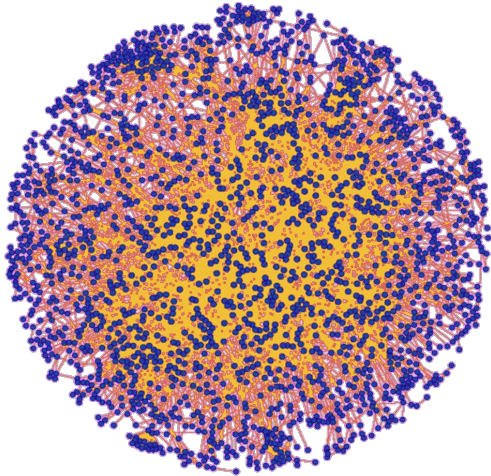
➤ Find a **low-dimensional representation of the nodes of a network**, while preserving the structural and relational information present in the original network.

- Matrix factorisation, random-walk based methods, auto-encoders, ...
- A variety of downstream analysis
- Easier analysis (low-dimensional, vector space)



Source: Nelson, Walter, et al. "To embed or not: network embedding as a paradigm in computational biology." *Frontiers in genetics* 10 (2019): 381.

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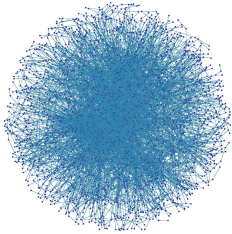
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Many Biological Networks

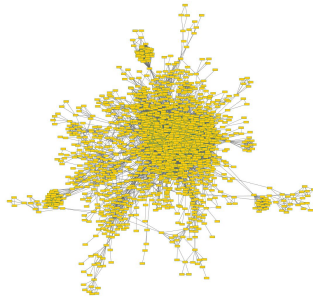
PPI



~60 000 edges

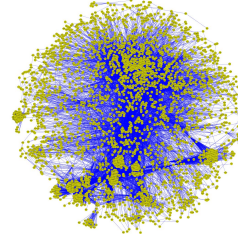
Experimental
networks

Complexes



~40 000 edges

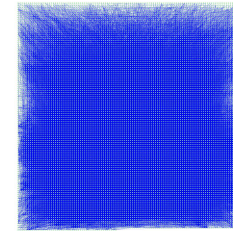
Pathways



~250 000 edges

Curated
networks

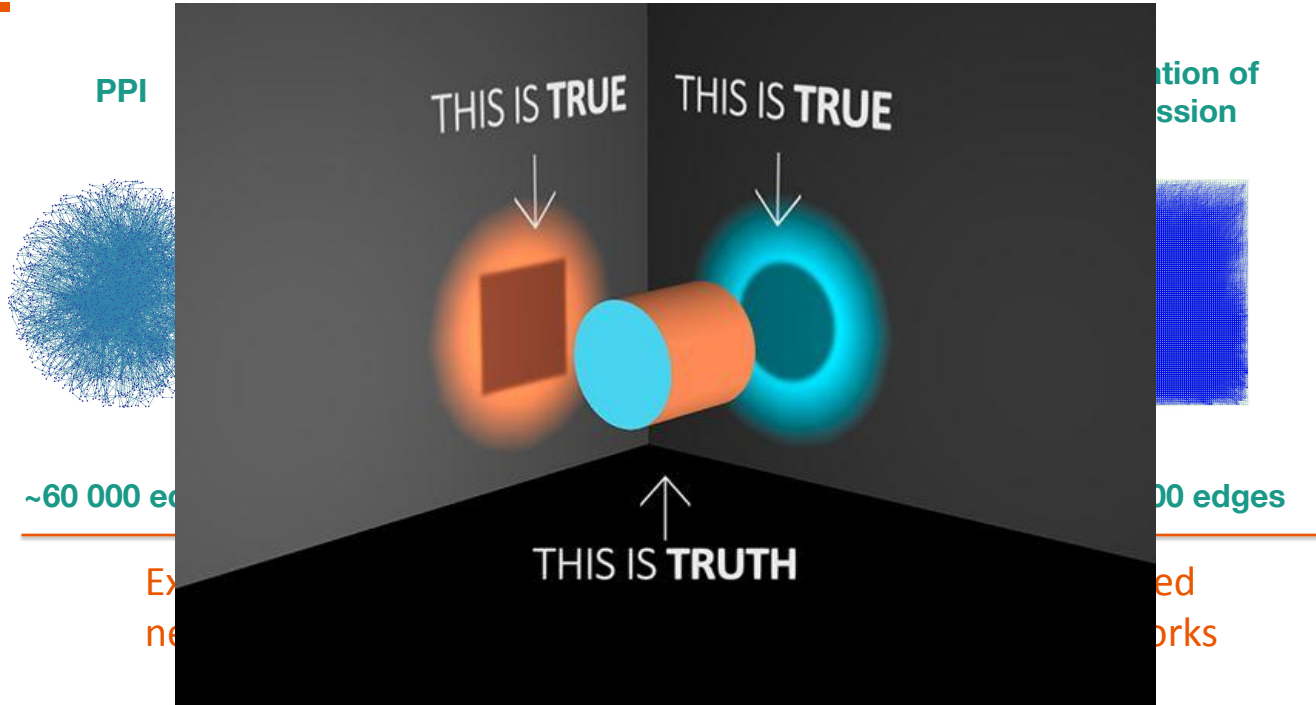
Correlation of
expression



~1 400 000 edges

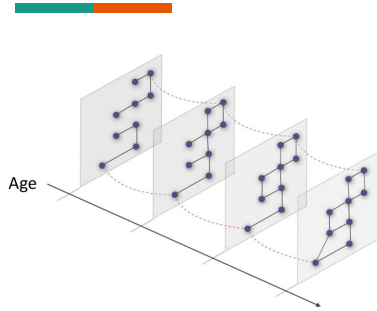
Inferred
networks

Many Biological Networks



Source: Courtesy of Anaïs Baudot

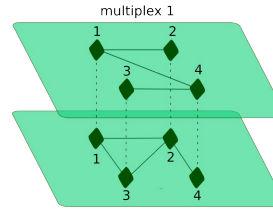
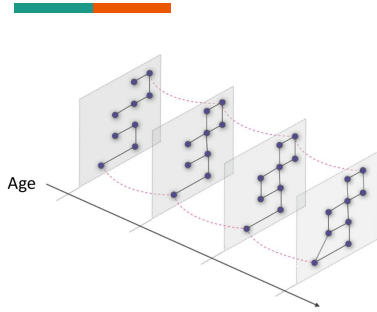
Networks can easily be **combined**



➤ Temporal networks

- Same nodes
- Same type of interactions
- Various time-points

Networks can easily be **combined**



Multiplex networks

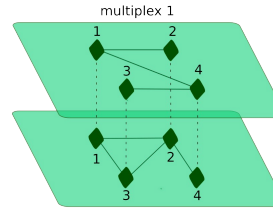
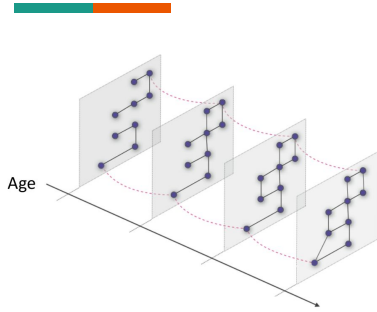
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Temporal networks

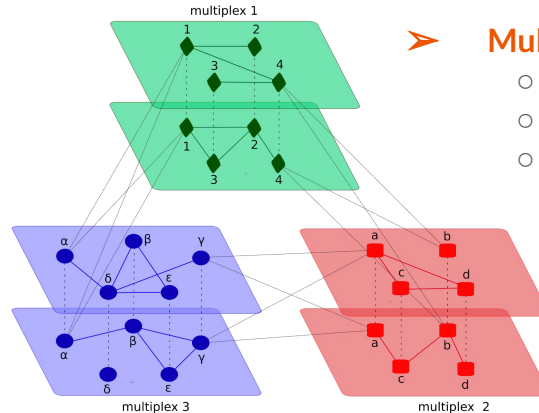
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Networks can easily be **combined**



- **Multiplex networks**
- Same nodes
 - Different types of interactions

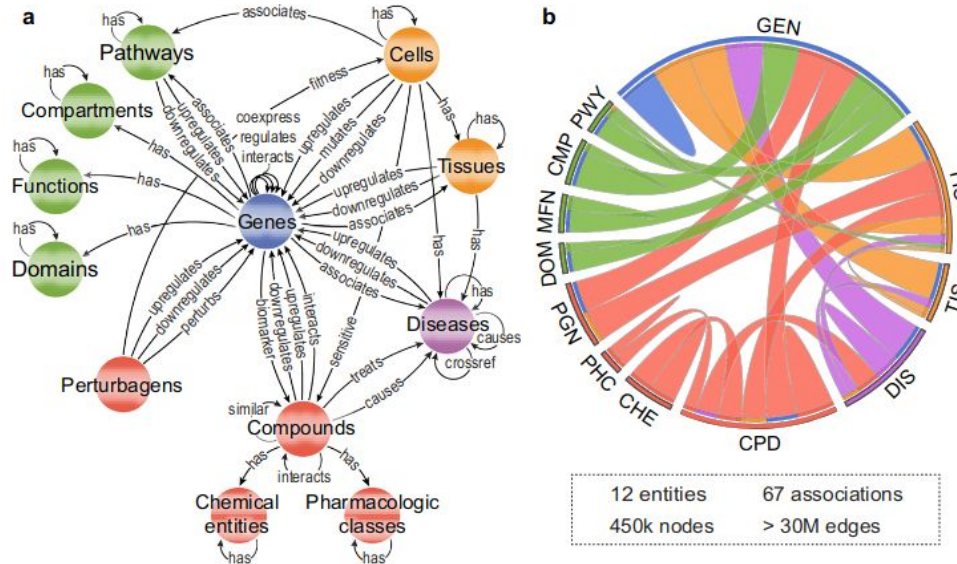
- **Temporal networks**
- Same nodes
 - Same type of interactions
 - Various time-points



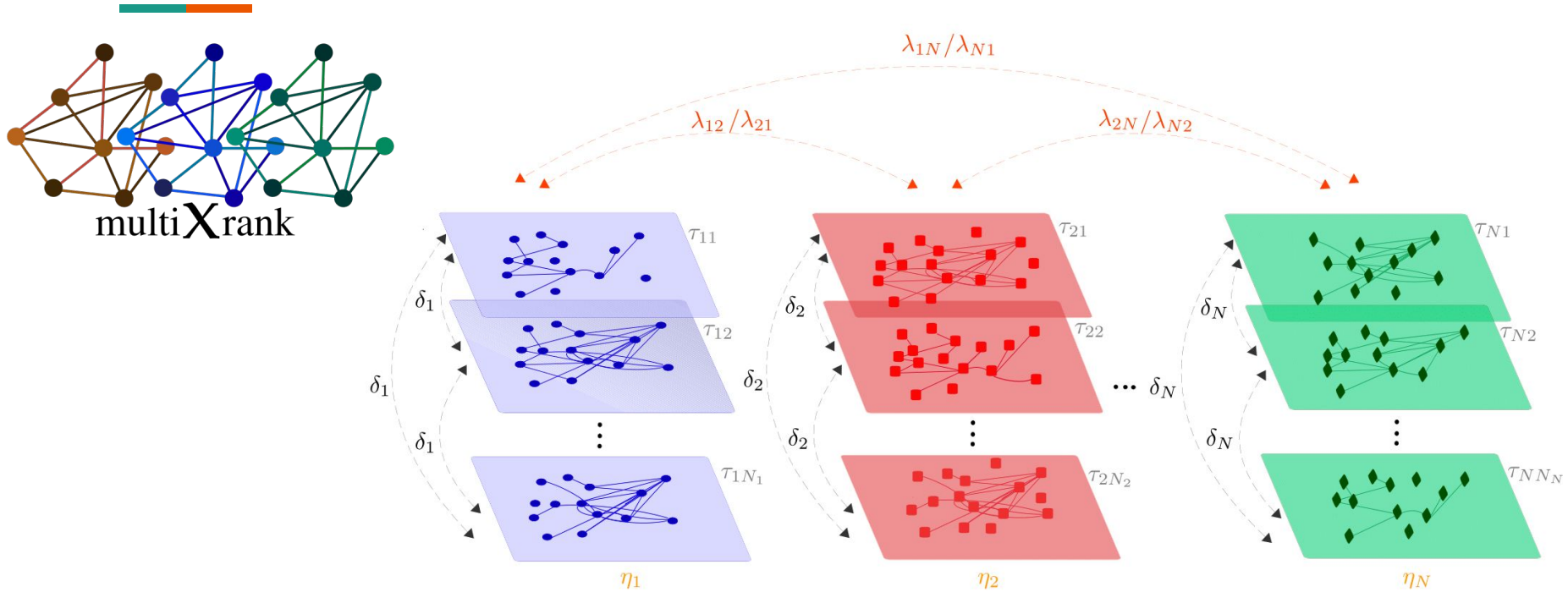
- **Multilayer networks**
- Various node types
 - Different types of interactions
 - Bipartite edges (across node types)

Networks can easily be combined: **Knowledge Graphs**

- **Knowledge graphs** ... are basically networks, but with semantic information
 - Represent real-world **facts** as a set of entities and relationships



Random Walk with Restart for multilayer network



Multiplex Community Detection

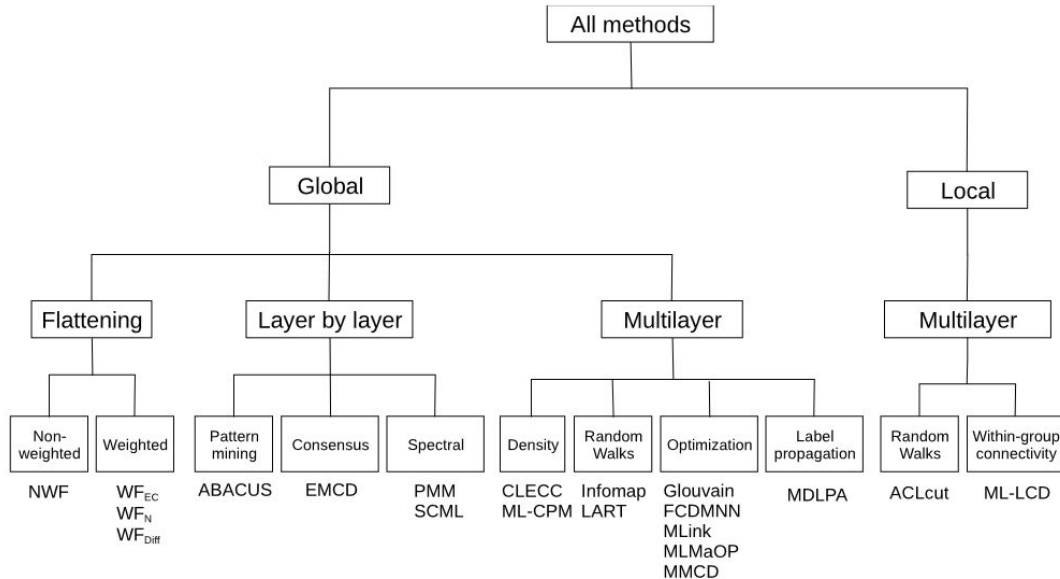
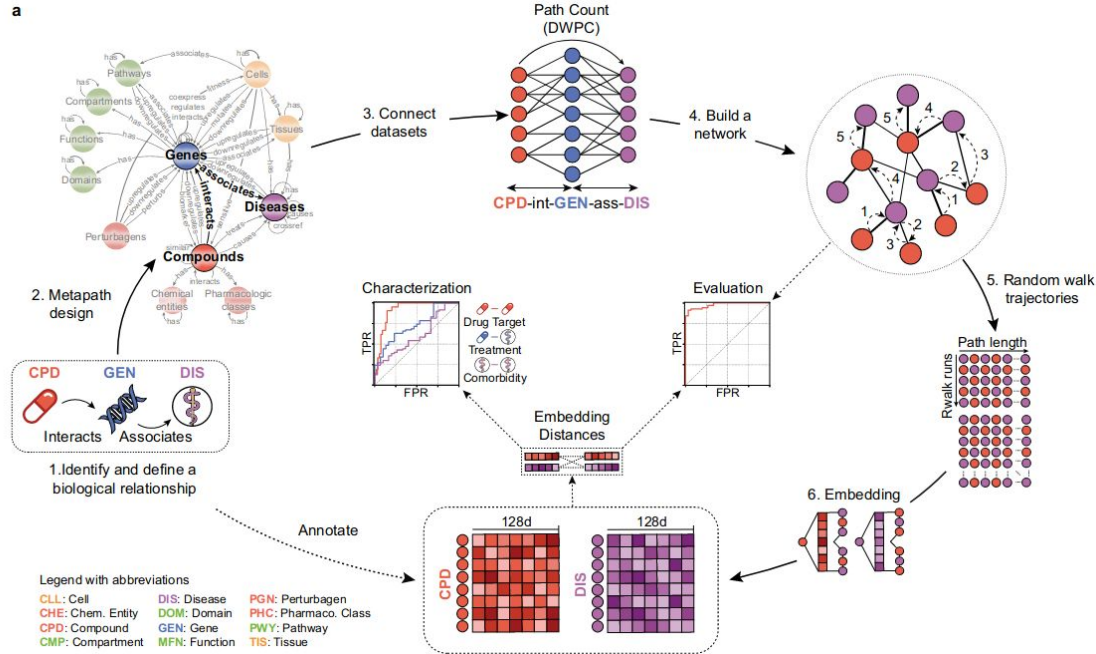
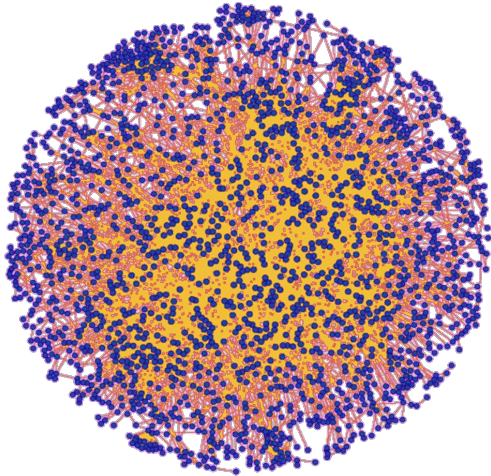


Figure 4: A taxonomy of multiplex community detection algorithms

Embedding for Knowledge Graphs



Outline



Source: <https://www3.nd.edu/~tmilenko/research.html>.

General Introduction, Key Concepts

Network Biology, Network Science, Complex Systems, ...

Network Construction/Inference

Data sources, Distances/Similarities, Correlation, ...

Network Analysis

Measures

Degree, Centrality, Distances, ...

Algorithms

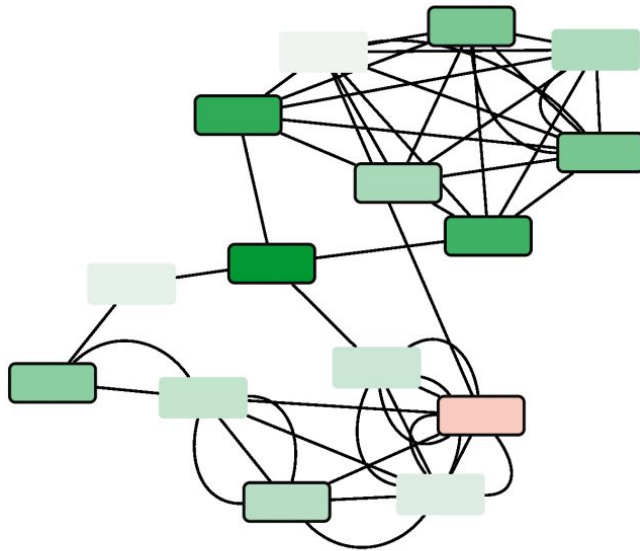
Diffusion, Clustering, Embedding, ...

Networks and Integration

Multiplex Networks, Multilayer Networks, Knowledge Graphs, ...

Conclusion

Networks are great

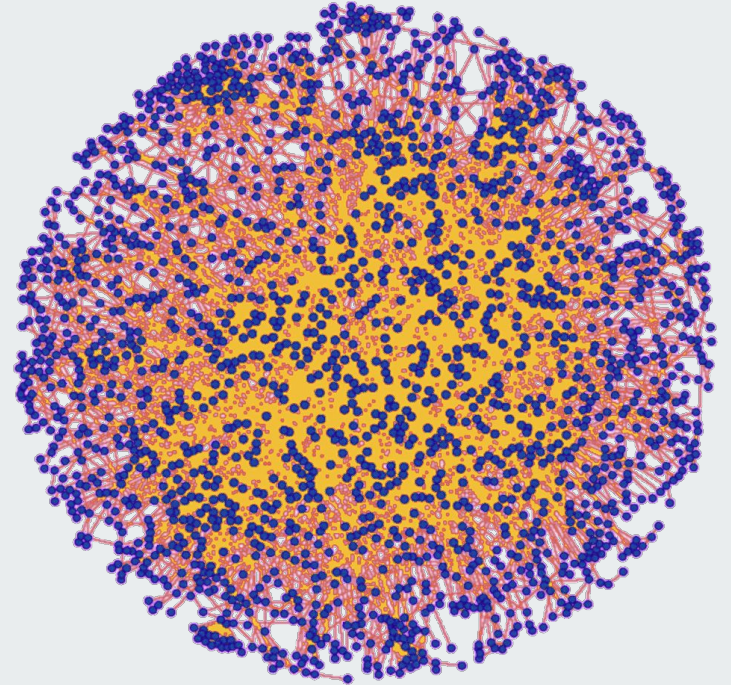


- Relationships
- Interpretable/Intuitive
- Scaffold for integration
 - heterogeneous data
 - previous knowledge
- Toolbox of graph theory



Hands-on : WGCNA

It's your turn now! Have fun!



Weighted Gene Correlation Network Analysis (WGCNA)

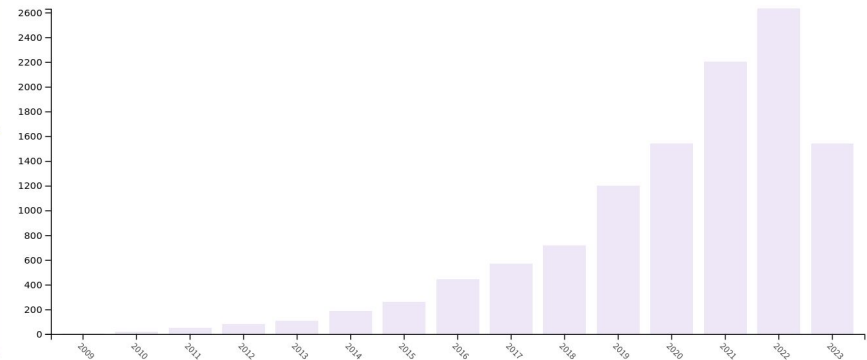
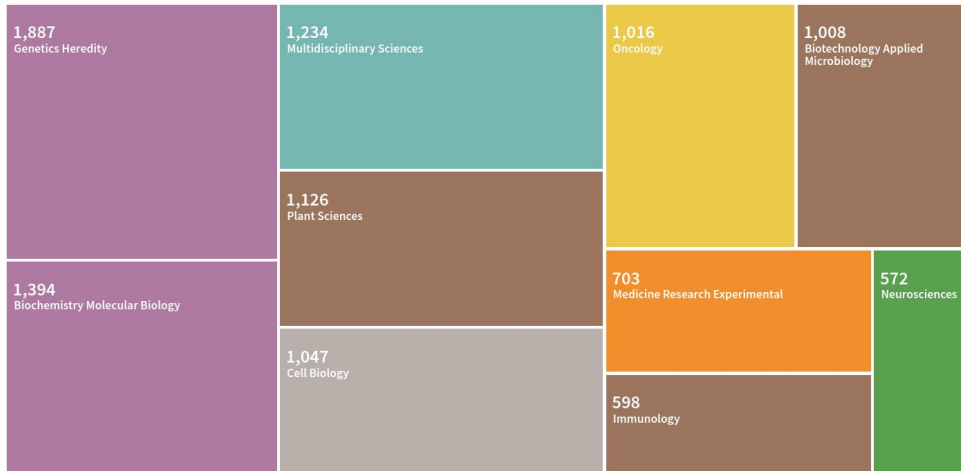
Software | [Open Access](#) | [Published: 29 December 2008](#)

WGCNA: an R package for weighted correlation network analysis

[Peter Langfelder](#) & [Steve Horvath](#) 

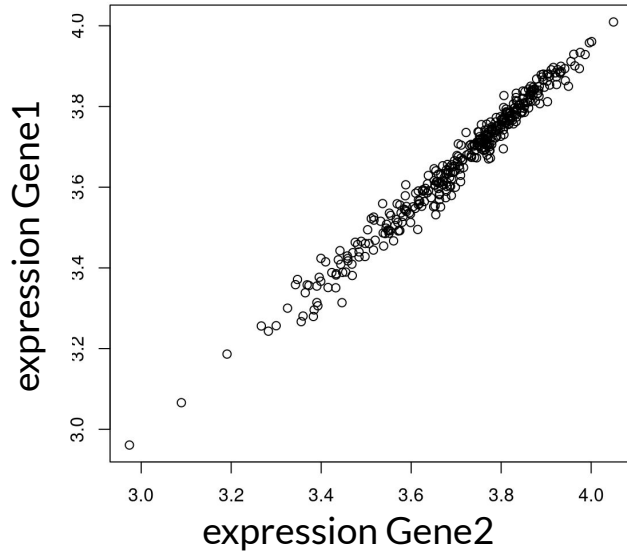
[BMC Bioinformatics](#) **9**, Article number: 559 (2008) | [Cite this article](#)

385k Accesses | **11547** Citations | **88** Altmetric | [Metrics](#)



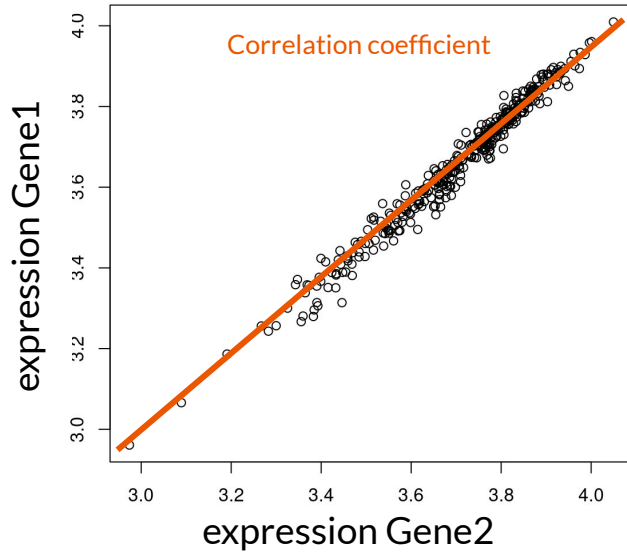
Weighted Gene Correlation Network Analysis (WGCNA)

➤ Gene co-expression



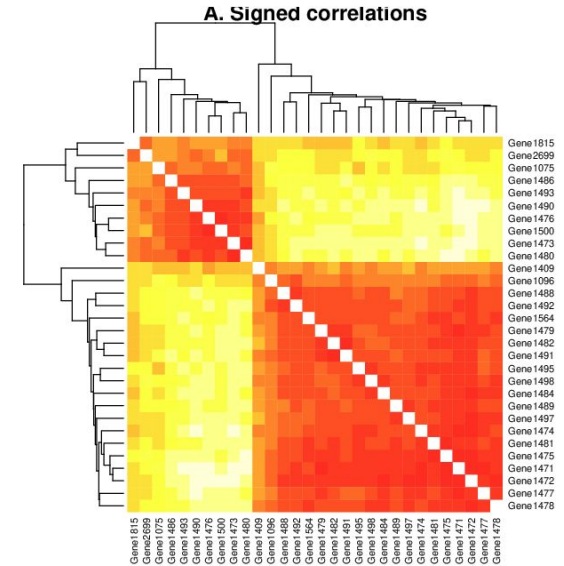
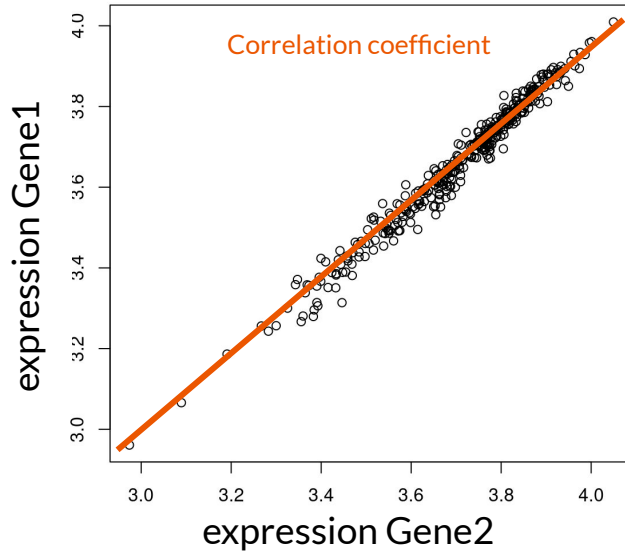
Weighted Gene Correlation Network Analysis (WGCNA)

➤ Gene co-expression



Weighted Gene Correlation Network Analysis (WGCNA)

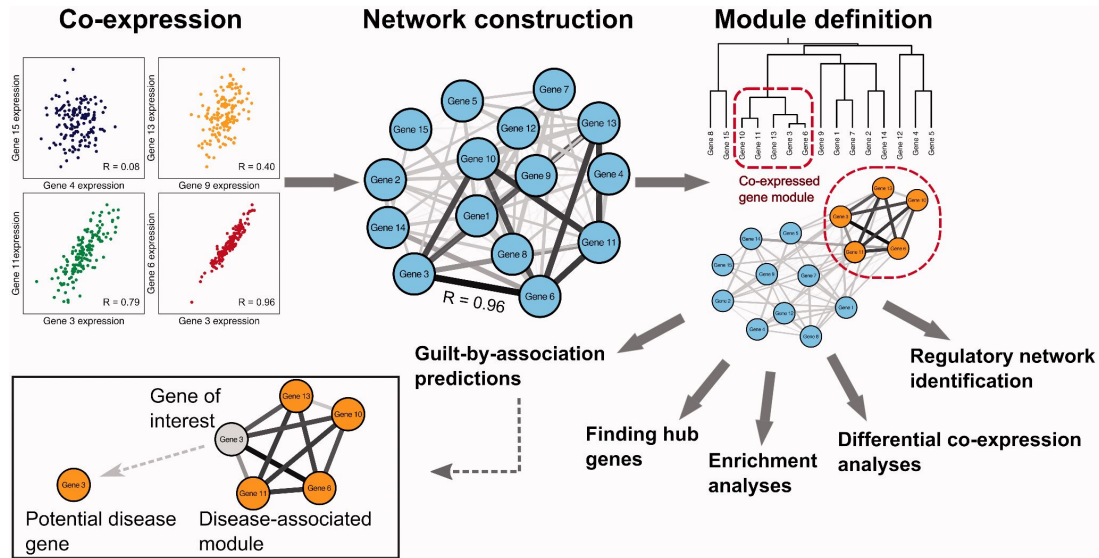
➤ Gene co-expression



Source: Horvath, S., and P. Langfelder. "Tutorial for the WGCNA Package for R" 2011.

Weighted Gene Correlation Network Analysis (WGCNA)

➤ Co-expressed gene modules



Source: Dam, Sipko van, Urmo Vösa, Adriaan van der Graaf, Lude Franke, and João Pedro de Magalhães. "Gene Co-Expression Analysis for Functional Classification and Gene-Disease Predictions." *Briefings in Bioinformatics* 19, no. 4 (July 20, 2018): 575–92. <https://doi.org/10.1093/bib/bbw139>.

Hands-on

Weighted Gene Co-expression Network Analysis (WGCNA)

Morgane Térézol - Galadriel
Brière
August 31, 2023

1 Libraries and environment

2 General principle of
WGCNA

3 Choose your dataset and
your modality

4 Biological context (Breast
cancer dataset)

5 Input data

6 Construction of the
correlation network

1 Libraries and environment

1.1 Environment

This report was generated using:

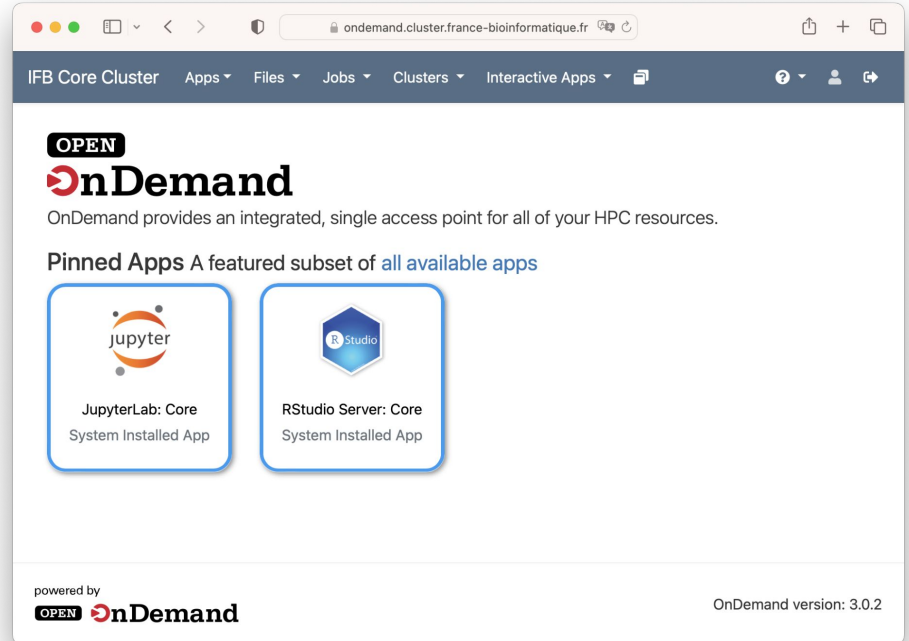
- R: **R version 4.3.1 (2023-06-16)**
- WGCNA: **1.72.1**
- pheatmap: **1.0.12**

You might also need the **compositions** library for data normalization.

1.2 Load libraries

DIY: Load the WGCNA and pheatmap libraries.

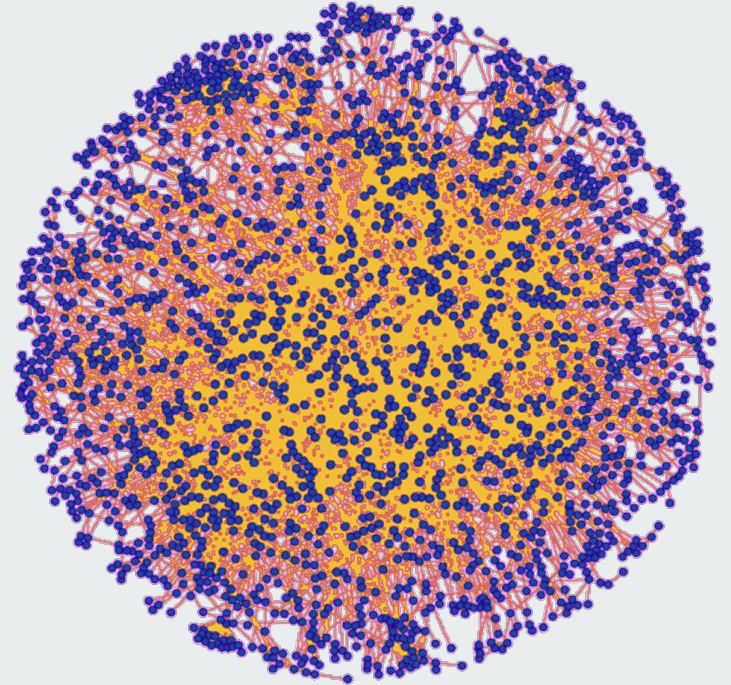
CODE






Hands-on : SNF

Galadriel Brière, Morgane Térézol, Benjamin Loire,
Anaïs Baudot, Samuel Chaffron



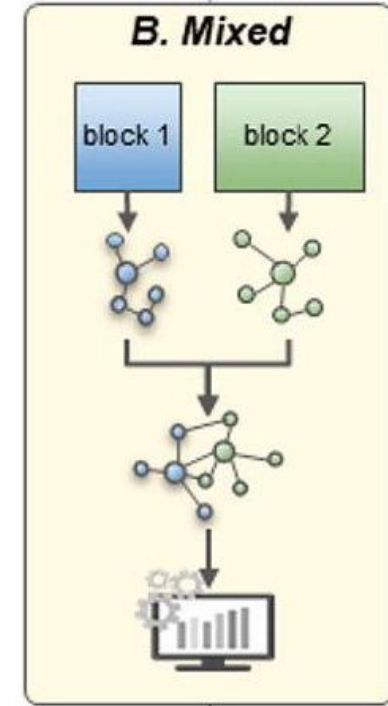
Similarity Network Fusion (SNF)



- Bo Wang *et al.*, Nature Methods. 2014

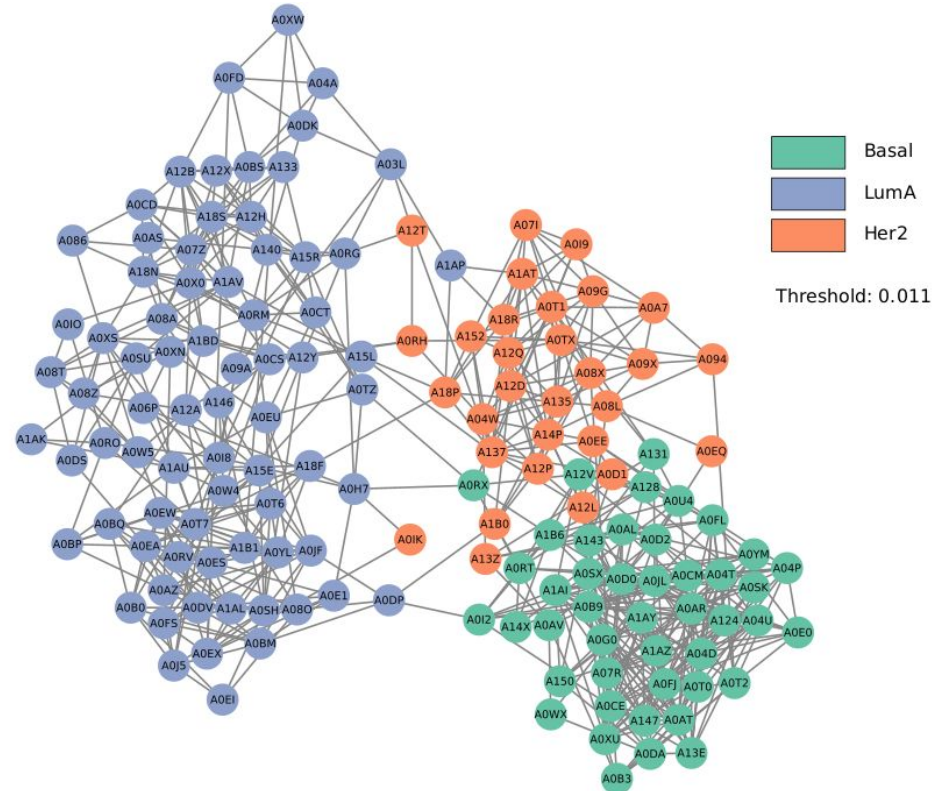
Similarity Network Fusion (SNF)

- Bo Wang *et al.*, Nature Methods. 2014
- Mixed integration method:
 - Sample **network** creation of each **data type**
 - **Fusion** of each data type networks



Similarity Network Fusion (SNF)

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- Mixed integration method:
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- **Sample network**



Similarity Network Fusion (SNF)



- Bo Wang *et al.*, Nature Methods. 2014
- **Mixed integration** method:
 - Sample **network** creation of each **data type**
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- **Sample network**
- Can manage:
 - **small number** of samples
 - noise
 - **data heterogeneity**
 - large number of features

Similarity Network Fusion (SNF)



- Bo Wang *et al.*, Nature Methods. 2014
- **Mixed integration** method:
 - Sample **network** creation of each **data type**
 - **Fusion** of each data type networks
- **Sample network**
- Can manage:
 - **small number** of samples
 - noise
 - **data heterogeneity**
 - large number of features
- Apply **measures** and **algorithms** for network on the fused network

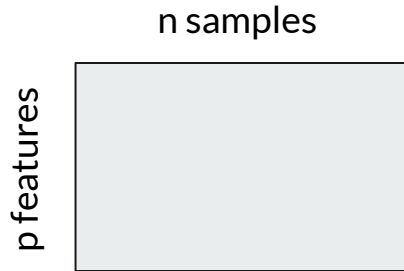
Similarity Network Fusion (SNF): Data preparation



- The most important step

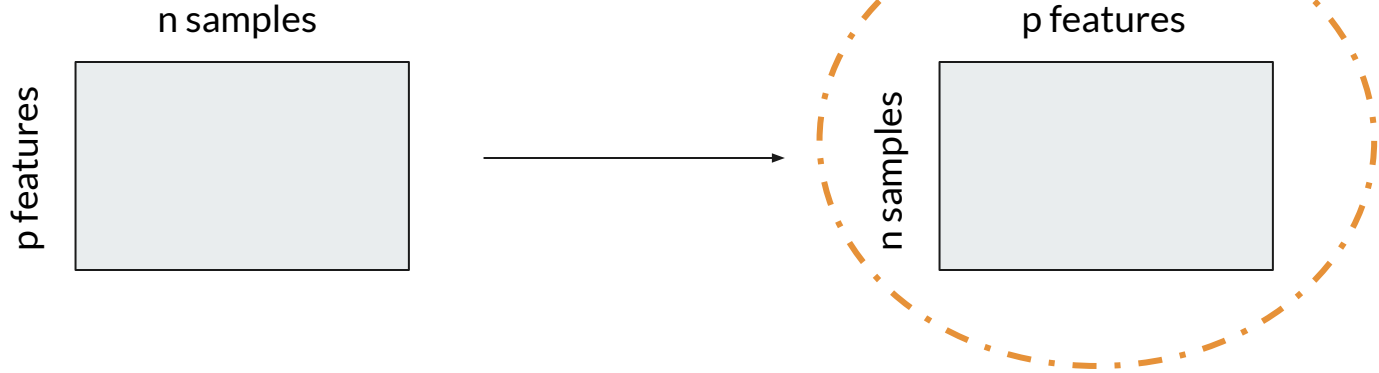
Similarity Network Fusion (SNF): Data preparation

- The most important step
- Pay attention on your data shape



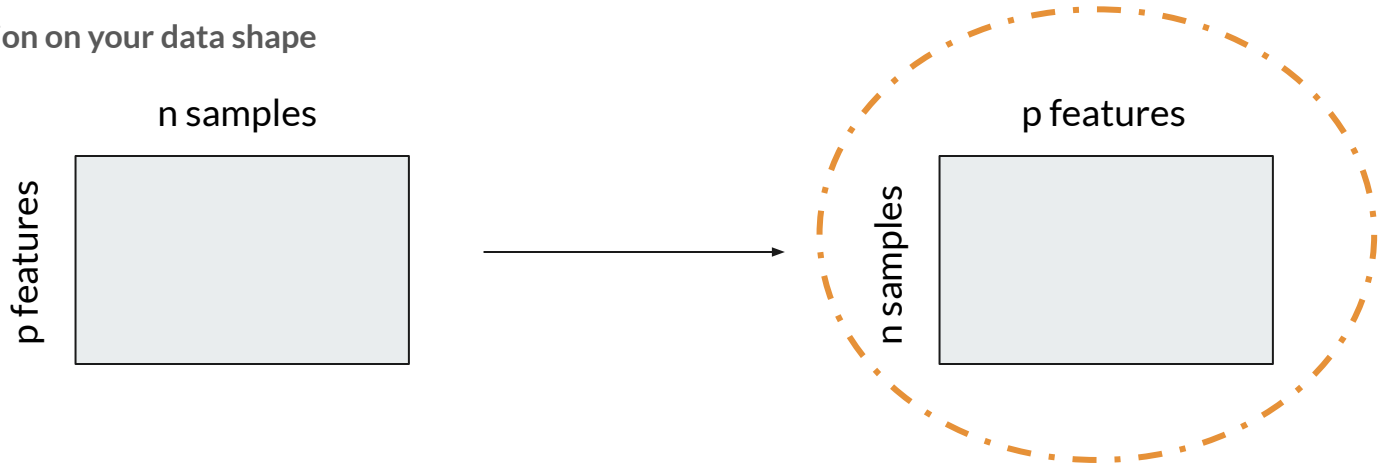
Similarity Network Fusion (SNF): Data preparation

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Similarity Network Fusion (SNF): Data preparation

- The most important step
- Pay attention on your data shape

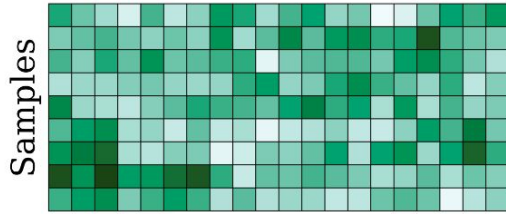


- **Normalization:** data should be normalized according to their type

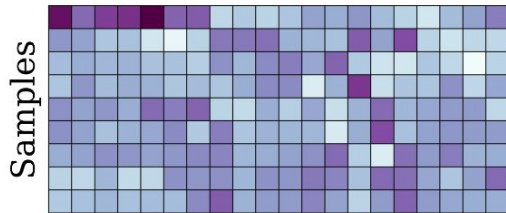
Similarity Network Fusion (SNF): Network creation



Data type 1



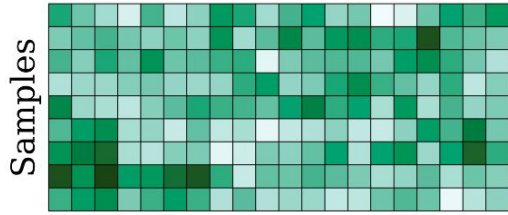
Data type 2



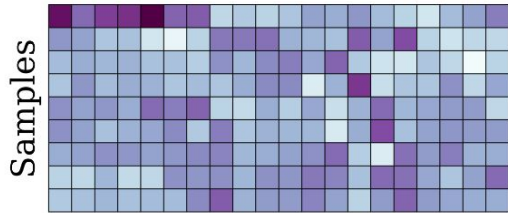
Similarity Network Fusion (SNF): Network creation



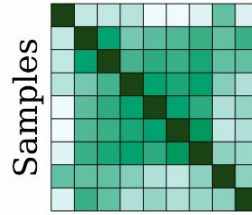
Data type 1



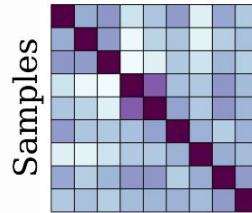
Data type 2



Samples



Samples



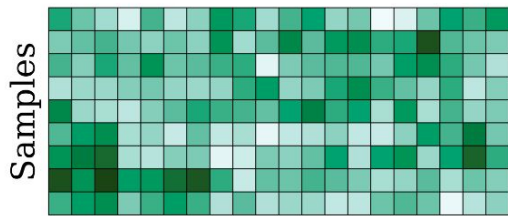
D

Distance matrix

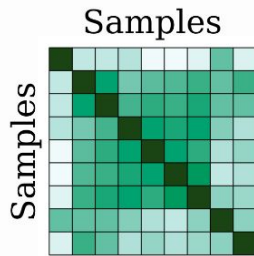
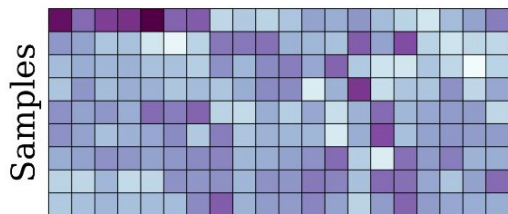
Similarity Network Fusion (SNF): Network creation



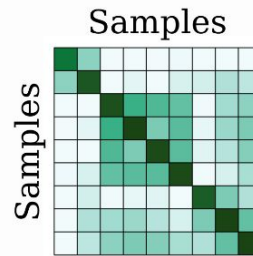
Data type 1



Data type 2



D
Distance matrix

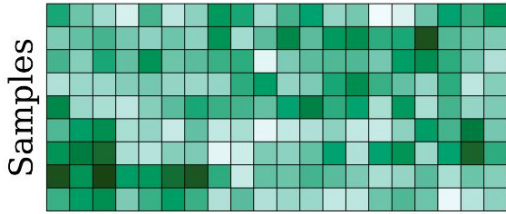


W
Similarity matrix

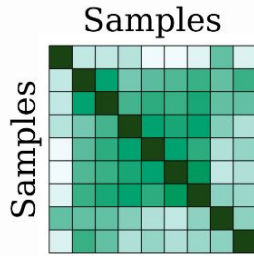
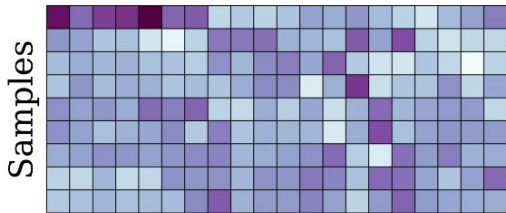
Similarity Network Fusion (SNF): Network creation



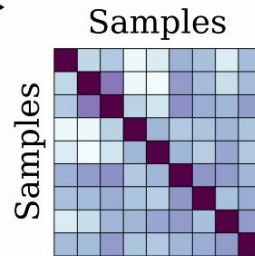
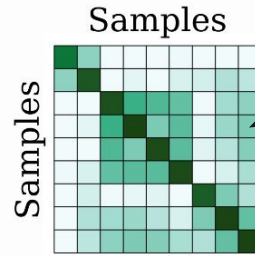
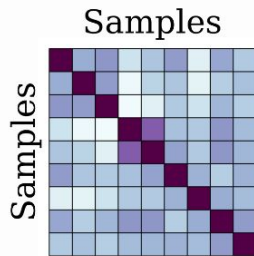
Data type 1



Data type 2

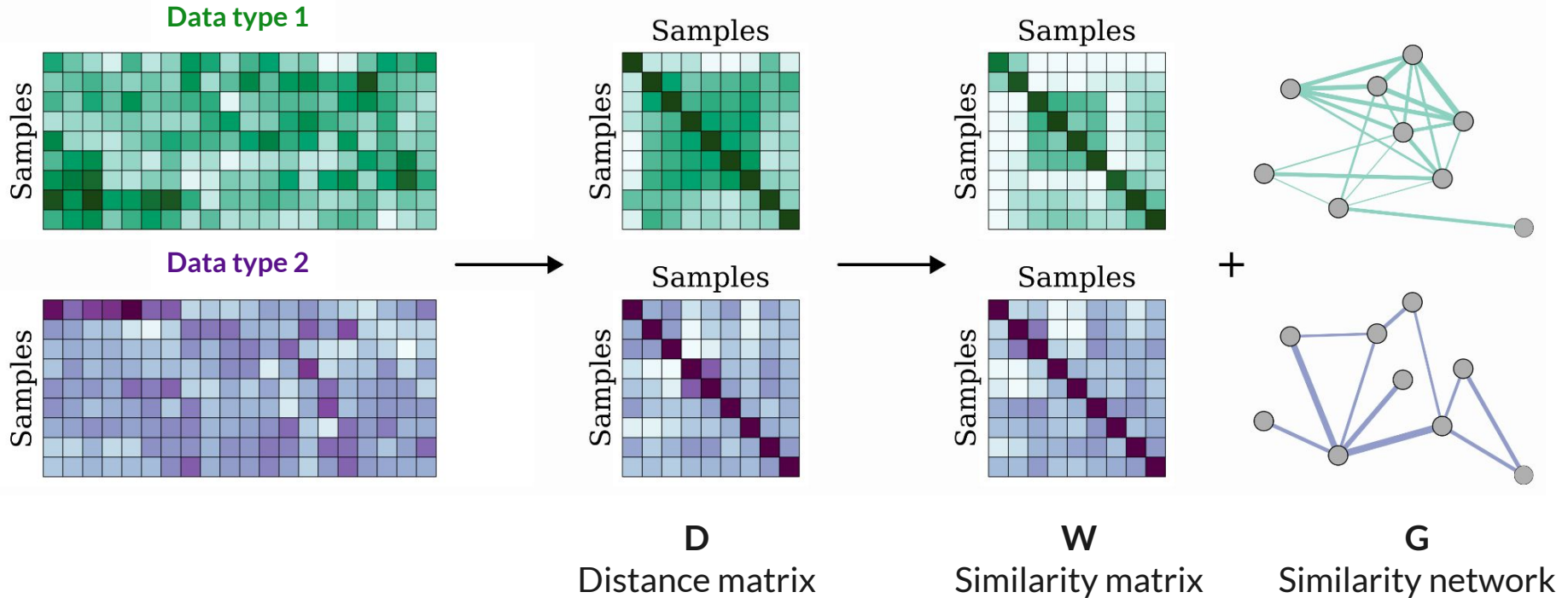


D
Distance matrix

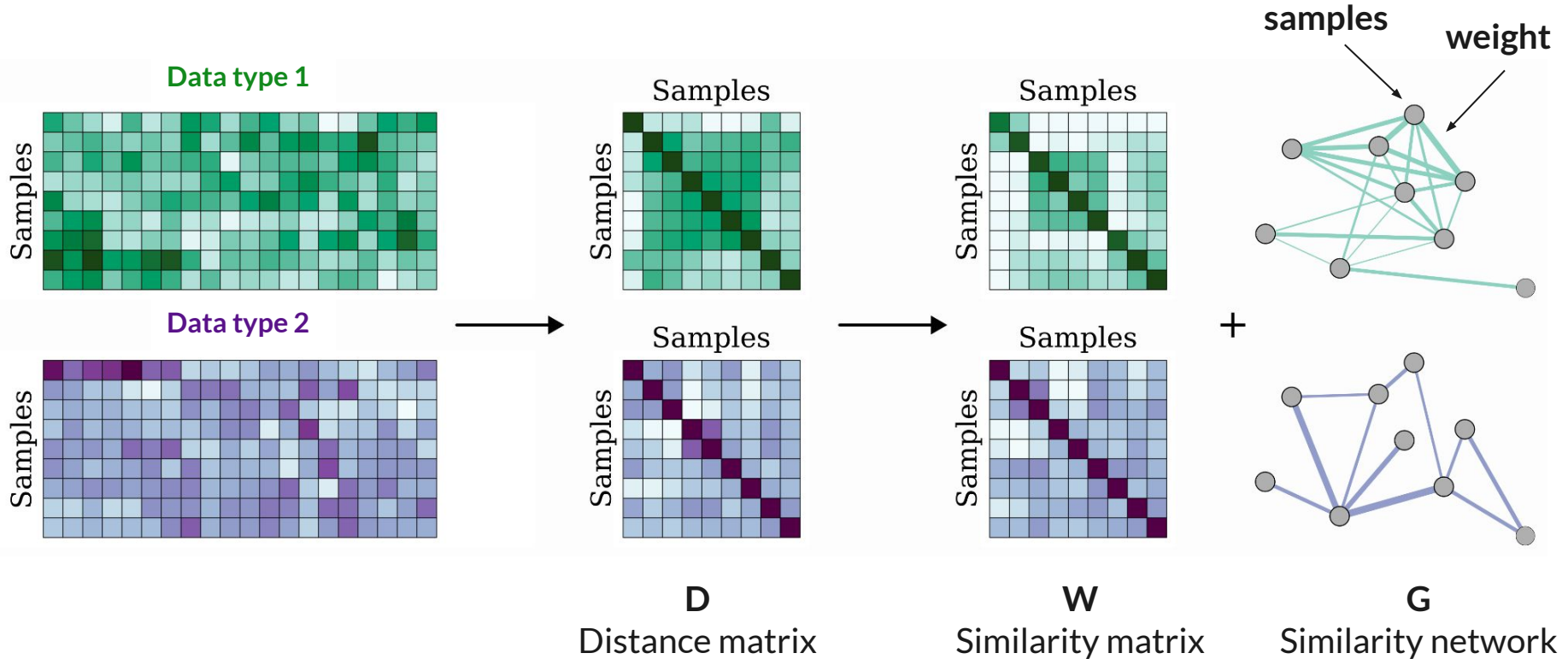


W
Similarity matrix

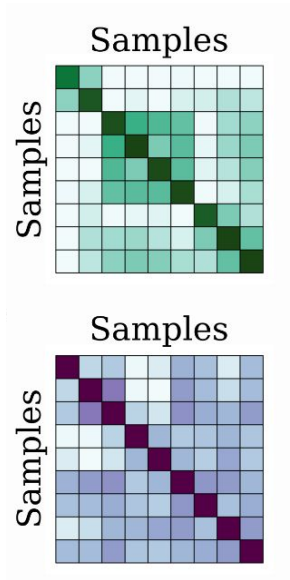
Similarity Network Fusion (SNF): Network creation



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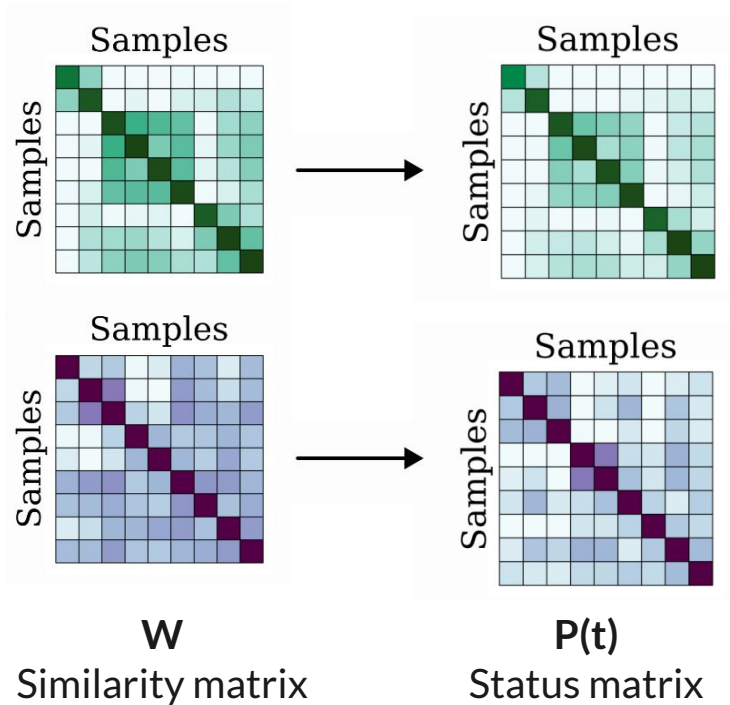
Similarity Network Fusion (SNF): Fusion



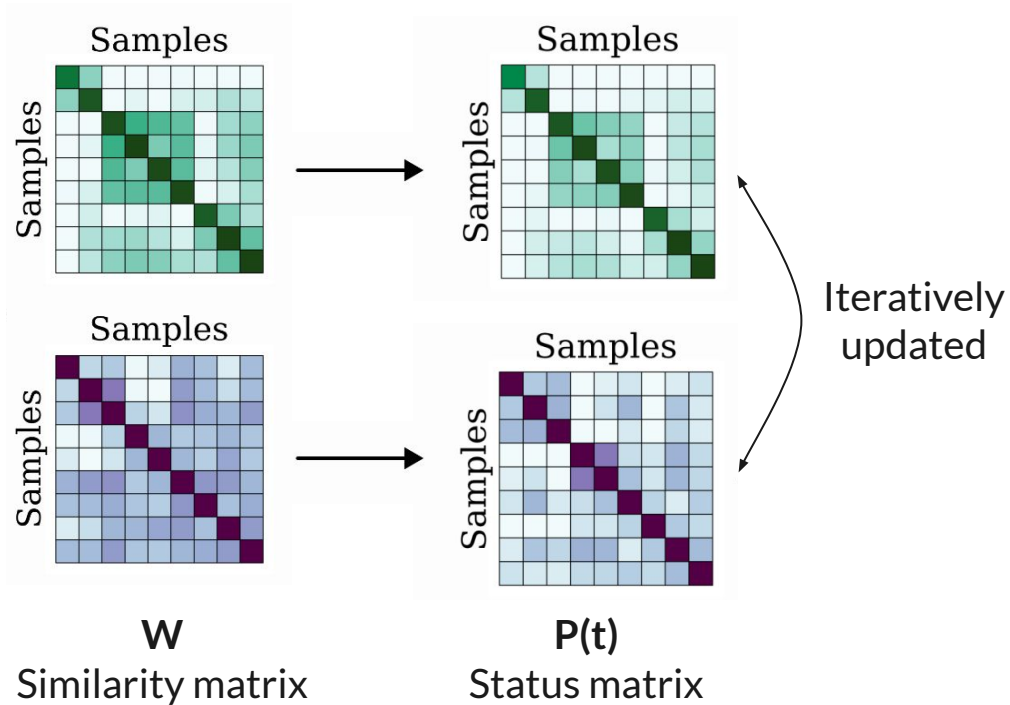
W

Similarity matrix

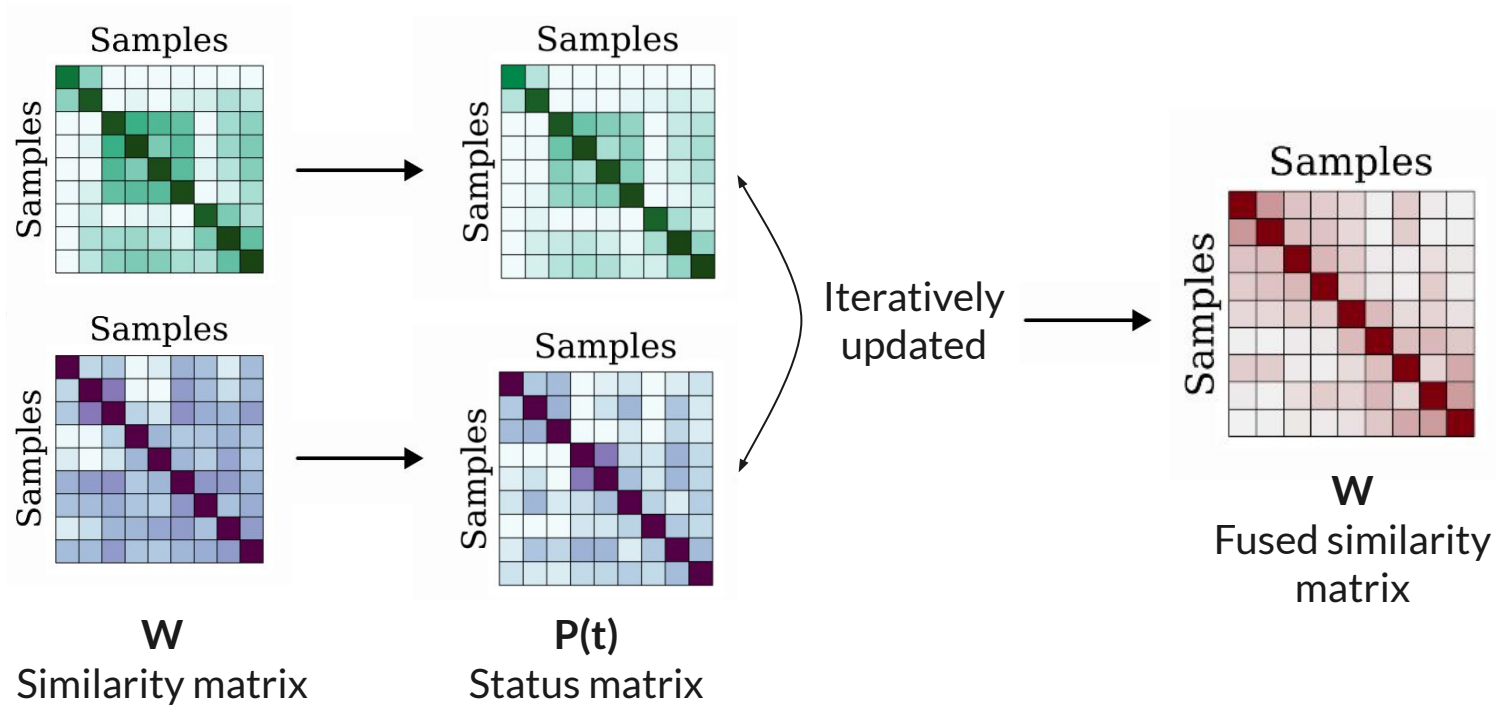
Similarity Network Fusion (SNF): Fusion



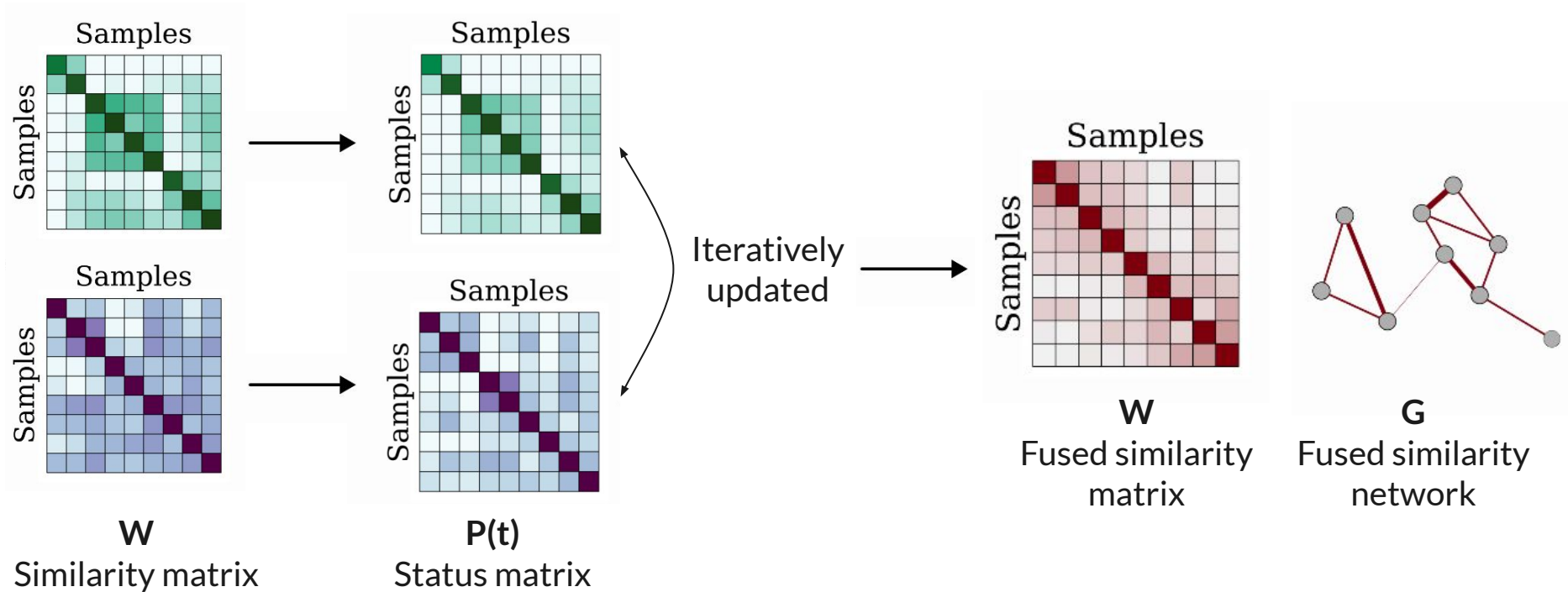
Similarity Network Fusion (SNF): Fusion



Similarity Network Fusion (SNF): Fusion



Similarity Network Fusion (SNF): Fusion



Hands-on

Hands-on in ETBII_2026_SNF.html

Similarity Network Fusion (SNF)
Morgane Térézol - Galadriel Brière
août 31, 2023

1 Libraries and environment

2 General principle of the SNF method

3 Choose your datasets

4 Input data

5 Similarity network

6 Fusion

1 Libraries and environment

1.1 Load environment

Libraries used to create and generate this report:

- R: R version 4.3.1 (2023-06-16)
- rmarkdown: 2.21
- knitr: 1.42
- rmdformats: 1.0.4
- bookdown: 0.34
- kableExtra: 1.3.4

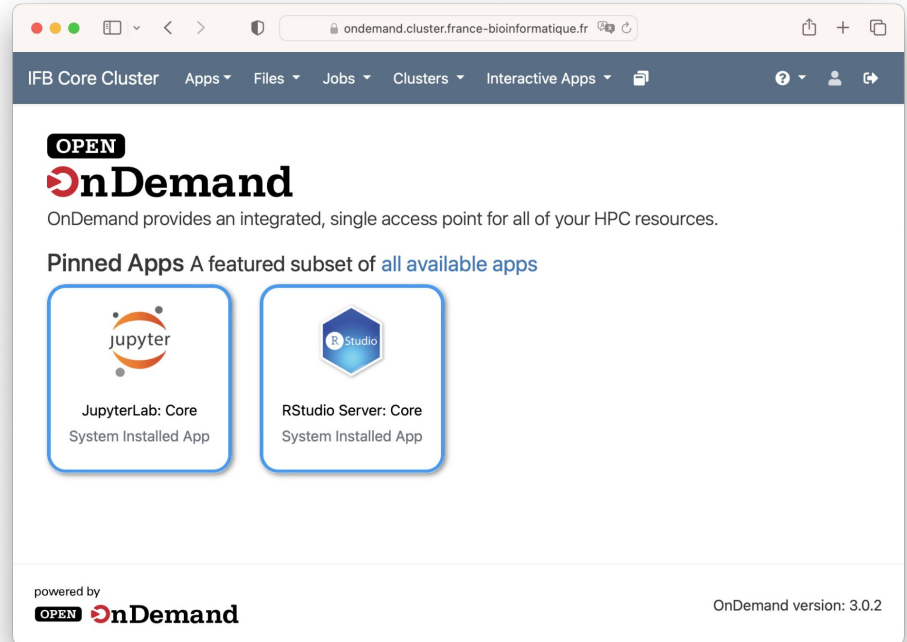
1.2 Load libraries

Libraries used to **analyse data**

```
library("SNFtool")
library("pheatmap")
library("igraph")
```

- SNFtool: 2.3.1
- pheatmap: 1.0.12
- igraph: 1.4.2

Libraries used to **load data**




IFB Core Cluster Apps Files Jobs Clusters Interactive Apps


OPEN
OnDemand

OnDemand provides an integrated, single access point for all of your HPC resources.

Pinned Apps A featured subset of [all available apps](#)



JupyterLab: Core
System Installed App



RStudio Server: Core
System Installed App

powered by **OPEN OnDemand** OnDemand version: 3.0.2

